

Daniel Riedel

Patrick Maletinsky, Quantum Sensing Group, University of Basel

Richard J. Warburton, Nano Optics Group, University of Basel

Enhancement of resonant transitions via coupling to a fully tunable Fabry-Pérot microcavity

DR et al., submitted (2017)

([arXiv:1703.00815](https://arxiv.org/abs/1703.00815))

Motivation



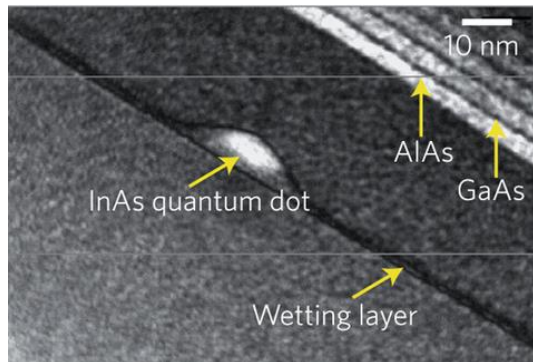
NV center: Optically addressable, highly coherent spin

Motivation



NV center: Optically addressable, highly coherent spin

Self assembled quantum dots



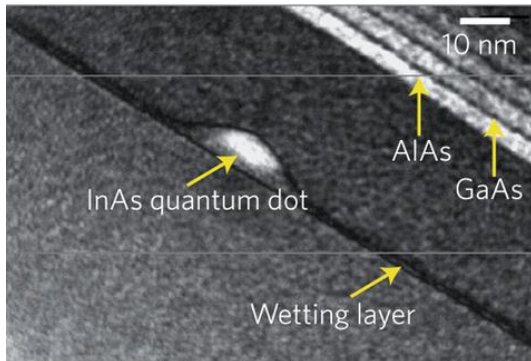
Warburton, Nat. Mater. **12**, 483 (2013)

Motivation



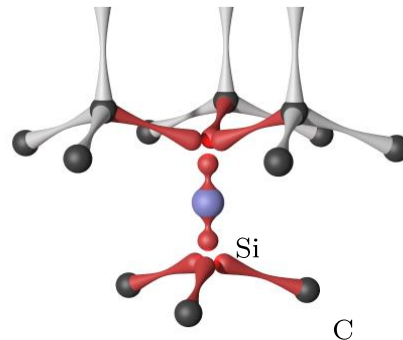
NV center: Optically addressable, highly coherent spin

Self assembled quantum dots



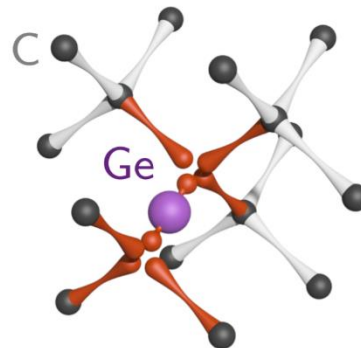
Warburton, Nat. Mater. **12**, 483 (2013)

diamond



SiV

Rogers et al. PRL **113**, 263602 (2014)
Sipahigil et. al, Science **354**, 847 (2016)



GeV

Siyushev et al., arXiv: 1612.02947
Bhaskar et al., arXiv: 1612.03036

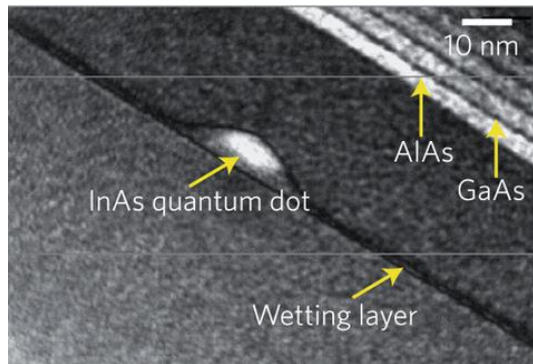
Colour centres

Motivation



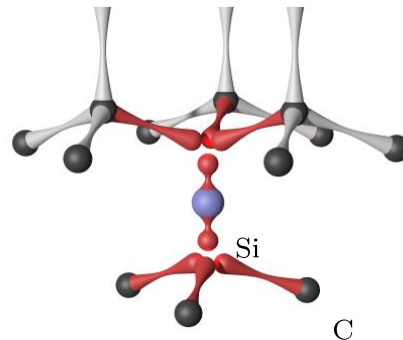
NV center: Optically addressable, highly coherent spin

Self assembled quantum dots



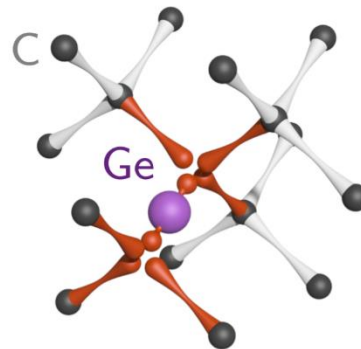
Warburton, Nat. Mater. **12**, 483 (2013)

diamond



SiV

Rogers et al. PRL **113**, 263602 (2014)
Sipahigil et. al, Science **354**, 847 (2016)

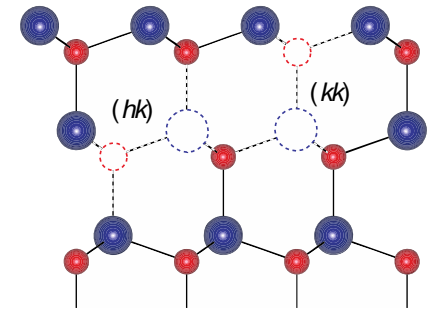


GeV

Siyushev et al., arXiv: 1612.02947
Bhaskar et al., arXiv: 1612.03036

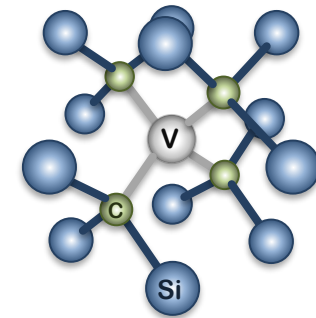
Colour centres

silicon carbide



$V_{Si}V_C$

Christle et al., Nat. Mater. **14**, 160 (2015)
Koehl et al., Nature **479**, 84 (2011)



V_{Si} / T_V

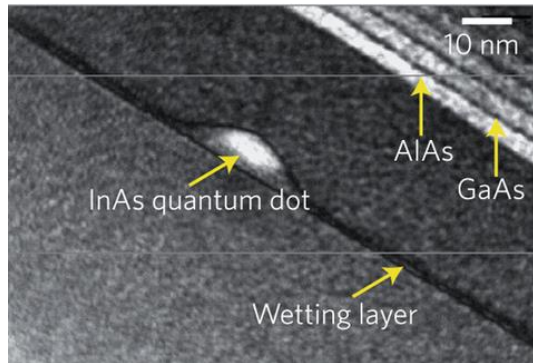
DR et al., PRL **109**, 226402 (2012)
Widmann et al., Nat. Mater. **14**, 164 (2015)

Motivation



NV center: Optically addressable, highly coherent spin

Self assembled quantum dots

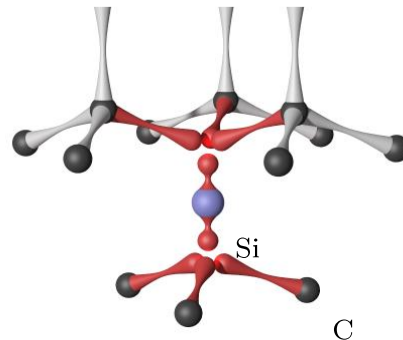


Warburton, Nat. Mater. **12**, 483 (2013)

Both spin and photon should be highly coherent

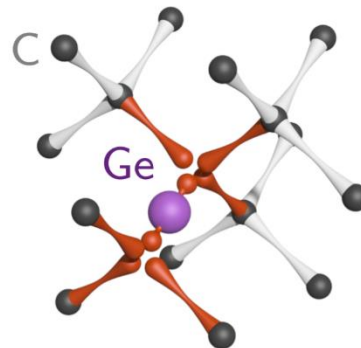
Colour centres

diamond



SiV

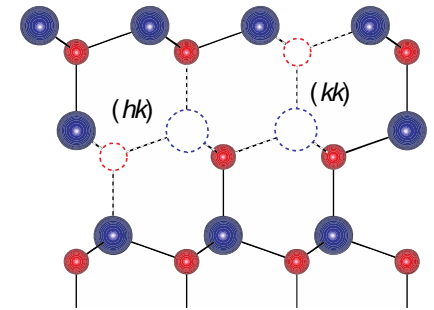
Rogers et al. PRL **113**, 263602 (2014)
Sipahigil et. al, Science **354**, 847 (2016)



GeV

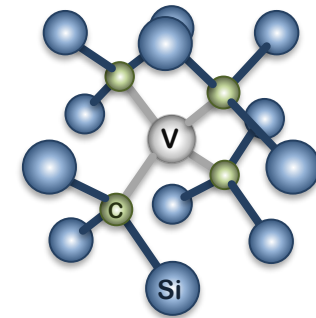
Siyushev et al., arXiv: 1612.02947
Bhaskar et al., arXiv: 1612.03036

silicon carbide



$V_{Si}V_C$

Christle et al., Nat. Mater. **14**, 160 (2015)
Koehl et al., Nature 479, 84 (2011)



V_{Si} / T_V

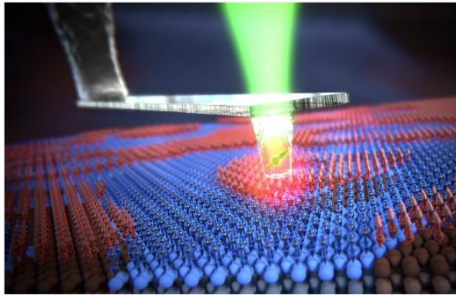
DR et al., PRL **109**, 226402 (2012)
Widmann et al., Nat. Mater. **14**, 164 (2015)

Motivation



NV center: Optically addressable, highly coherent spin

Magnetic sensing



Appel et al., New J. Phys. **17**, 112001 (2015)

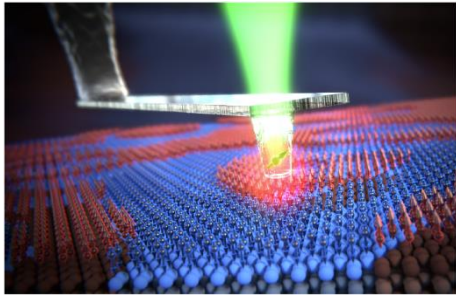
Thiel et al., Nat. Nanotechnol. **11**, 677 (2016)

Motivation



NV center: Optically addressable, highly coherent spin

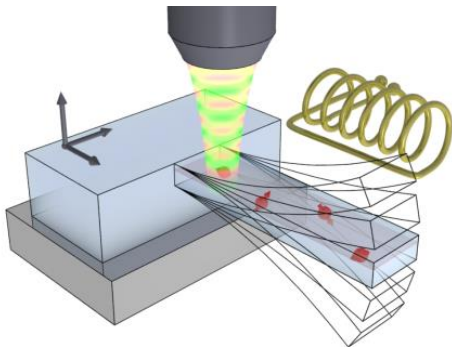
Magnetic sensing



Appel et al., New J. Phys. **17**, 112001 (2015)

Thiel et al., Nat. Nanotechnol. **11**, 677 (2016)

Optomechanics



Teissier et al., PRL **113**, 020503 (2014)

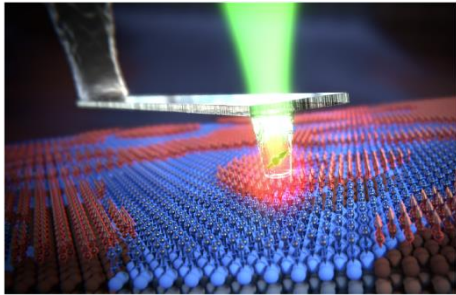
Barfuss et al., Nat. Phys. **11**, 820 (2015)

Motivation



NV center: Optically addressable, highly coherent spin

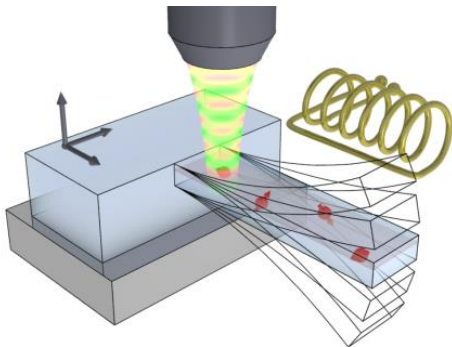
Magnetic sensing



Appel et al., *New J. Phys.* **17**, 112001 (2015)

Thiel et al., *Nat. Nanotechnol.* **11**, 677 (2016)

Optomechanics

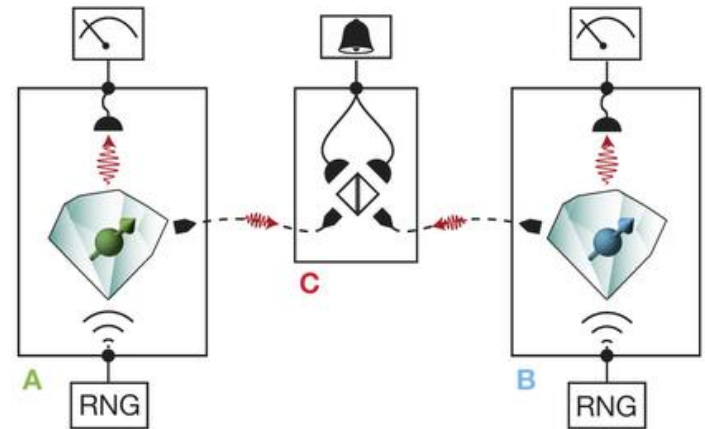


Teissier et al., *PRL* **113**, 020503 (2014)

Barfuss et al., *Nat. Phys.* **11**, 820 (2015)

Quantum information

Long distance spin-spin entanglement



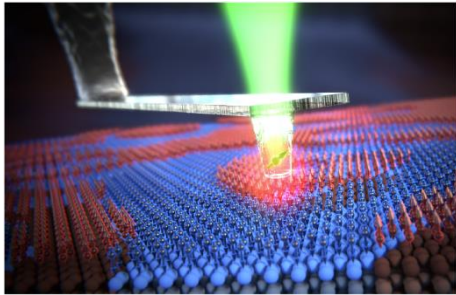
Hensen et al., *Nature* **526**, 682 (2015)

Motivation



NV center: Optically addressable, highly coherent spin

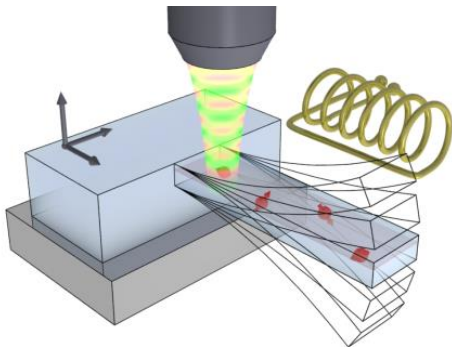
Magnetic sensing



Appel et al., New J. Phys. **17**, 112001 (2015)

Thiel et al., Nat. Nanotechnol. **11**, 677 (2016)

Optomechanics

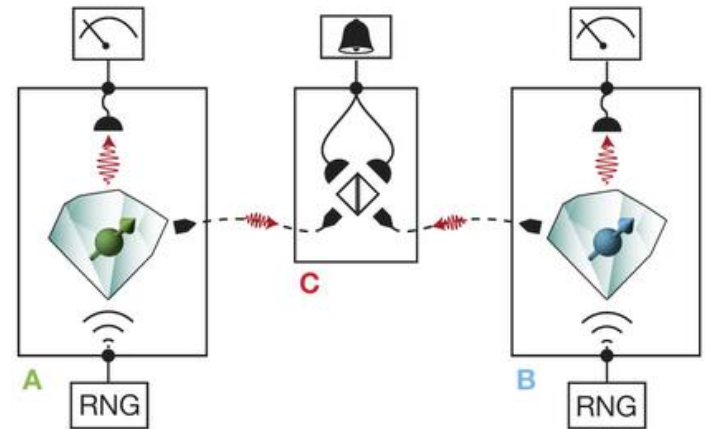


Teissier et al., PRL **113**, 020503 (2014)

Barfuss et al., Nat. Phys. **11**, 820 (2015)

Quantum information

Long distance spin-spin entanglement

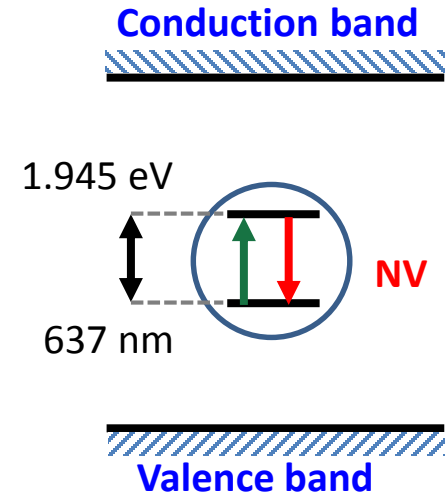
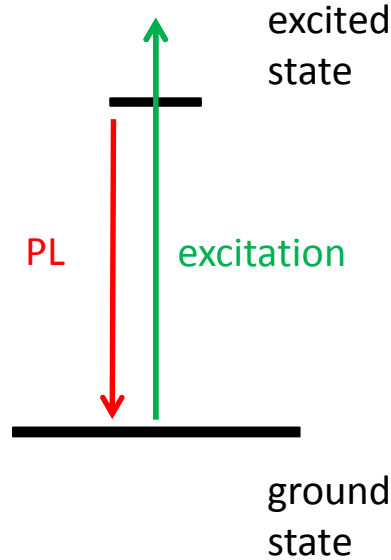
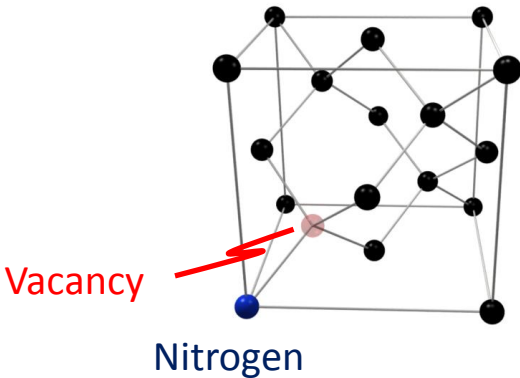


Hensen et al., Nature **526**, 682 (2015)

➤ **limited by the detection rate of coherent photons (~ mHz)**

- Motivation
- NV centres in diamond
- Optical cavities
- Fully tunable Fabry-Pérot microcavity
- Experimental results and analysis
- Summary and Outlook

NV centres in diamond - advantages



Key features:

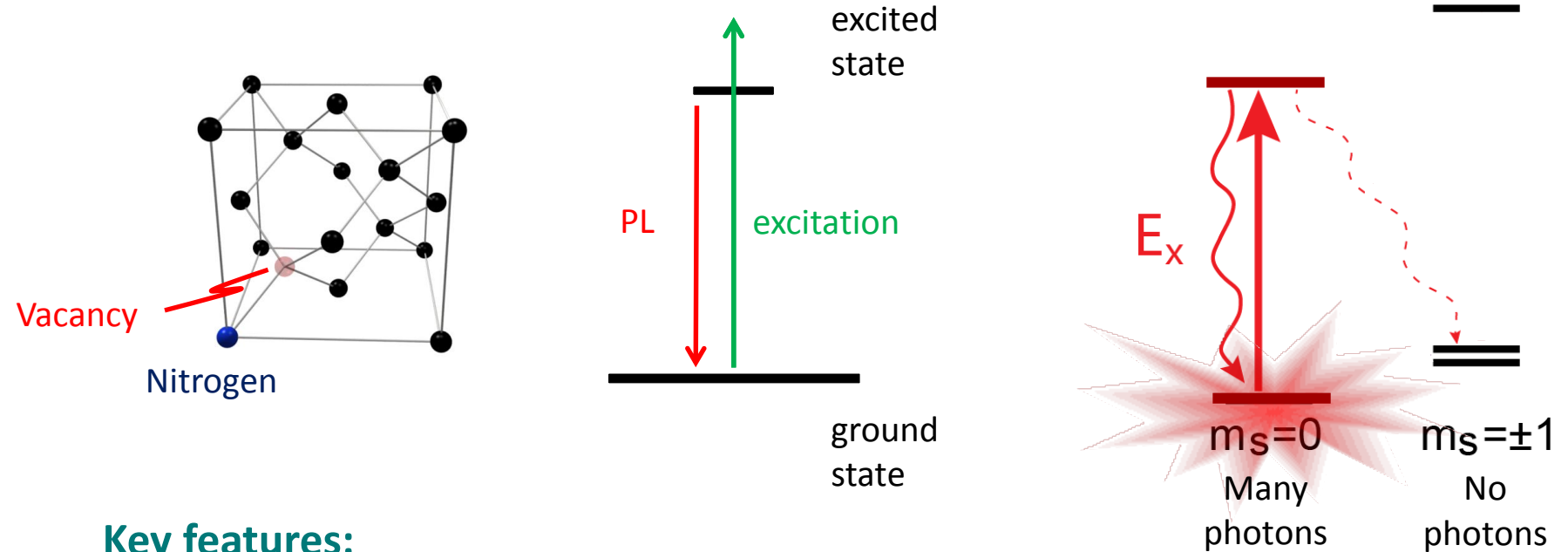
- long spin coherence times (> 1 ms)
 - nuclear quantum memory (> 1 s)
 - fast one- and two- qubit gates
 - ground state spin control via external fields
- } @RT

Balasubramanian et al., Nat. Mater. **8**, 383 (2009)

Maurer et al., Nature **8**, 383 (2009)

Fuchs et al., Science **326**, 1520 (2009)

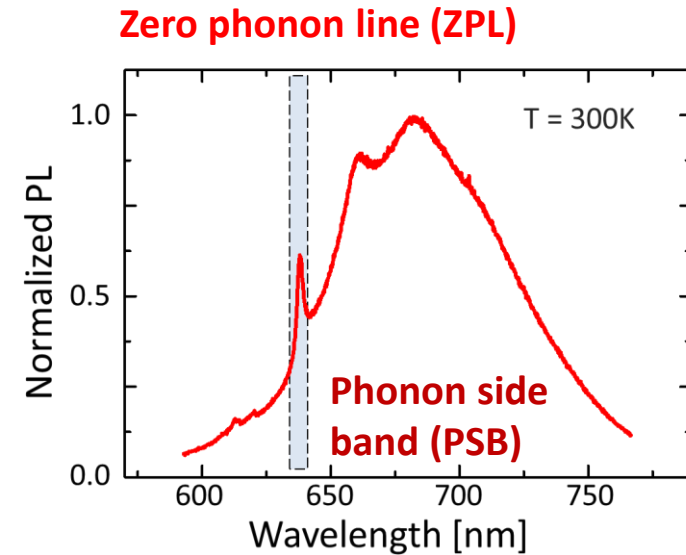
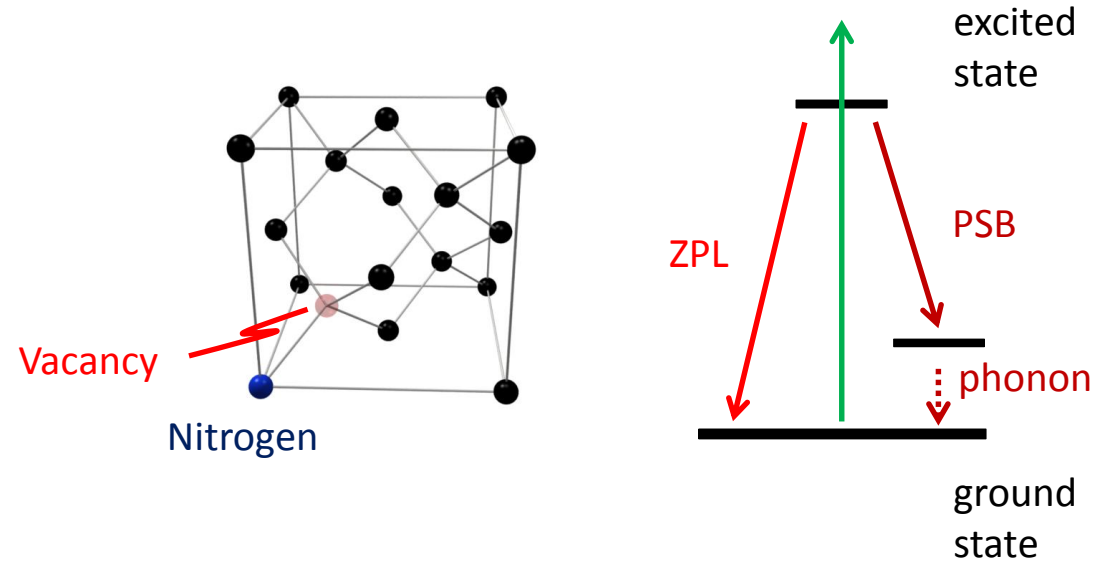
NV centres in diamond - advantages



Key features:

- spin-readout via spin-state dependent photoluminescence (PL) intensity
- spin-selective / cycling transitions
- optical lambda-system: requirement for spin-photon entanglement

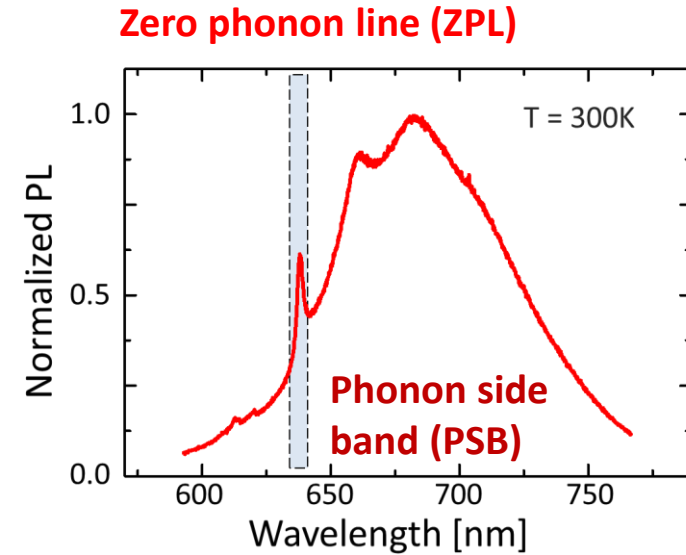
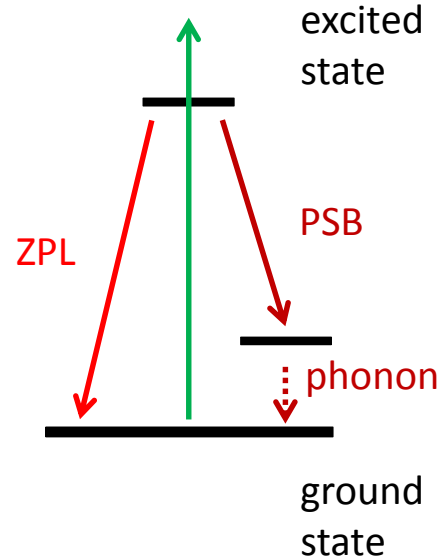
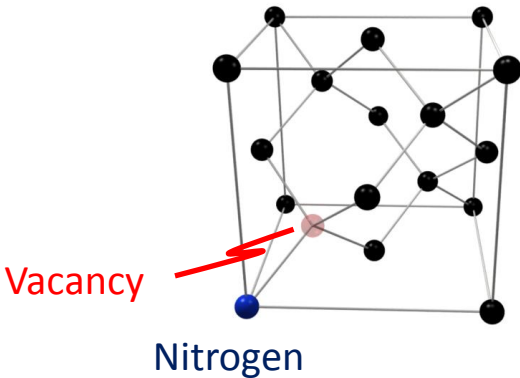
NV centres in diamond - challenges



Key challenge: light extraction

1. small extraction efficiency out of bulk diamond
2. long radiative lifetime: $\sim 12\text{ ns}$
3. small fraction of PL emission at ZPL (637 nm): $\sim 3\%$

NV centres in diamond - challenges



Key challenge: light extraction

1. small extraction efficiency out of bulk diamond
2. long radiative lifetime: ~ 12 ns
3. small fraction of PL emission at ZPL (637 nm): ~ 3%

→ solve all 3 problems with cavity

Transition rate for spontaneous emission:

$$\gamma_{12} = \frac{2\pi}{\hbar^2} \langle \vec{p} \cdot \vec{E}_{\text{vac}} \rangle^2 g(\omega)$$

Transition rate for spontaneous emission:

electric dipole

density of states

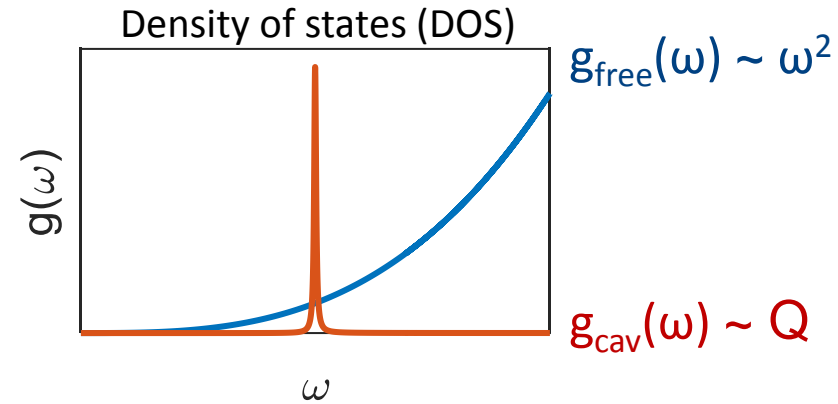
$$\gamma_{12} = \frac{2\pi}{\hbar^2} \langle \vec{p} \cdot \vec{E}_{\text{vac}} \rangle^2 g(\omega)$$

vacuum electric field

Transition rate for spontaneous emission:

$$\gamma_{12} = \frac{2\pi}{\hbar^2} \langle \vec{p} \cdot \vec{E}_{\text{vac}} \rangle^2 \boxed{g(\omega)}$$

$\sim Q$

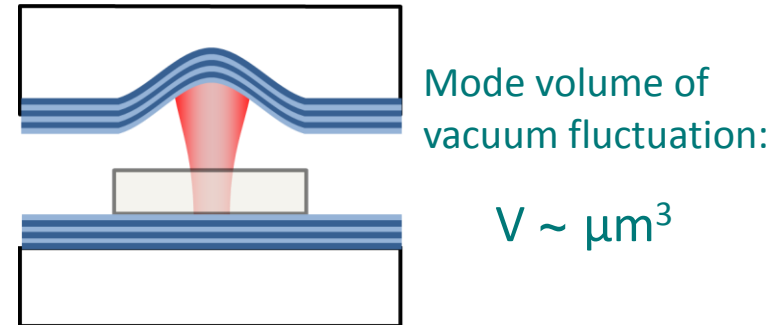
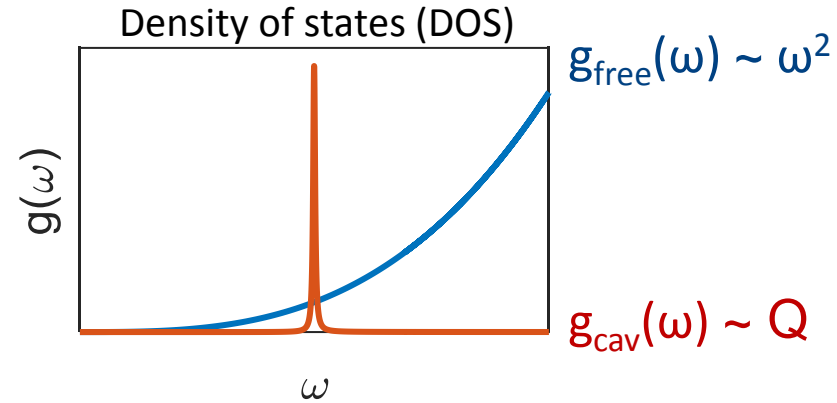


Optical cavity - Purcell enhancement

Transition rate for spontaneous emission:

$$\gamma_{12} = \frac{2\pi}{\hbar^2} \left\langle \vec{p} \cdot \vec{E}_{\text{vac}} \right\rangle^2 g(\omega)$$

$\sim 1/V$
 $\sim Q$



Energy of vacuum fluctuation:

$$\int \epsilon_0 \epsilon_R E^2 dV = \hbar\omega / 2$$

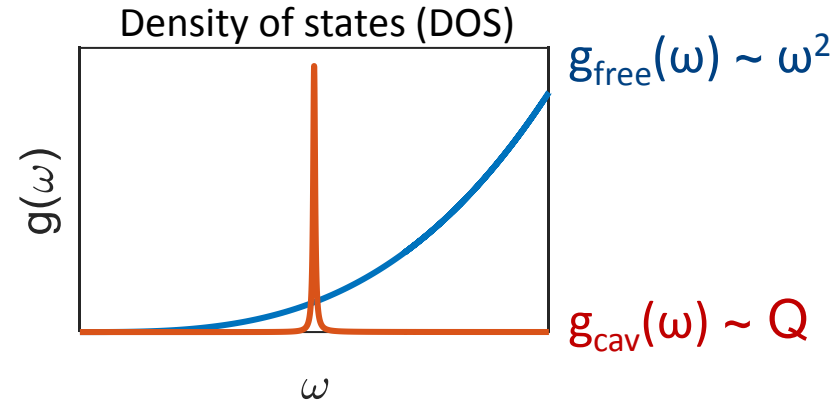
Optical cavity - Purcell enhancement

Transition rate for spontaneous emission:

$$\gamma_{12} = \frac{2\pi}{\hbar^2} \left\langle \vec{p} \cdot \vec{E}_{\text{vac}} \right\rangle^2 g(\omega)$$

$\sim 1/V$

$\sim Q$

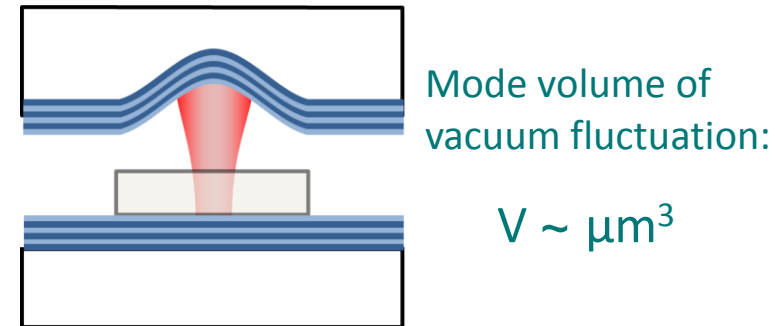


Relative transition rate enhancement:

$$\frac{\gamma_{\text{cav}}}{\gamma_{\text{free}}} \sim \frac{Q}{V} \quad (\text{Purcell enhancement})$$

constant

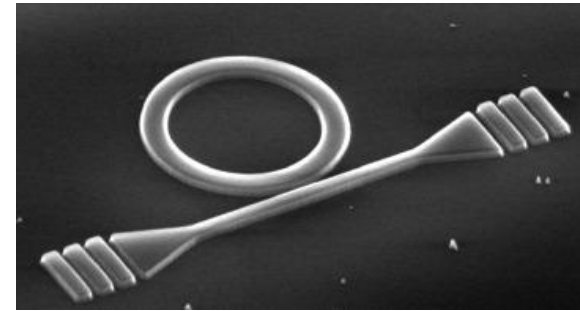
Increased DOS - High Q
 Confined E_{vac} - Small V



Energy of vacuum fluctuation:

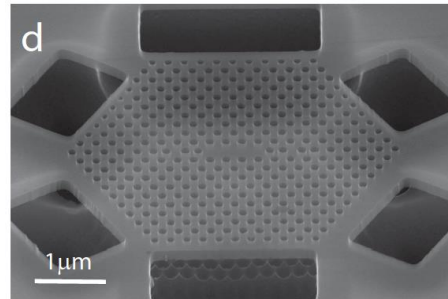
$$\int \epsilon_0 \epsilon_R E^2 dV = \hbar\omega / 2$$

micro-ring resonator



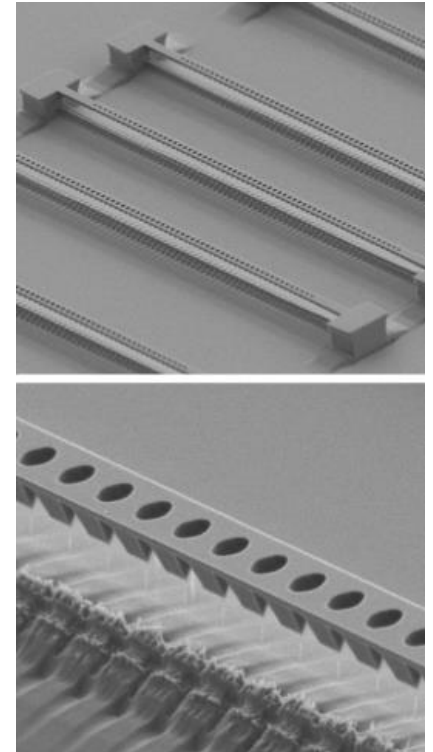
Faraon et al., *New J. Phys.* **15** 025010 (2013)
 Faraon et al., *Nat. Photon.* **5**, 301 (2011)

2D photonic crystal



Faraon et. al, *PRL* **109**, 033604 (2012)
 Riedrich-Möller et al.,
Appl. Phys. Lett. **106**, 221103 (2015)

nanobeam photonic crystal

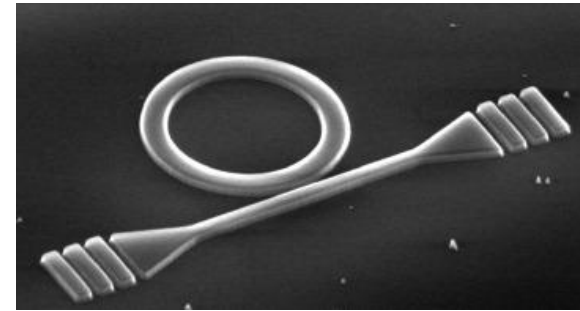


Hausmann et al., *Nano Lett.* **13**, 5791 (2013)
 Burek et al., *Nat. Commun.* **5**, 5718 (2014)
 Li et al., *Nat. Commun.* **6**, 6173 (2015)
 Sipahigil et. al, *Science* 354, **847** (2016)

Key result:

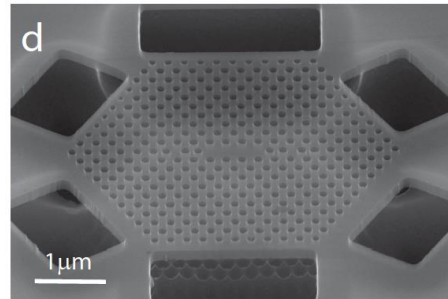
- up to 70-fold enhancement of emission rate

micro-ring resonator



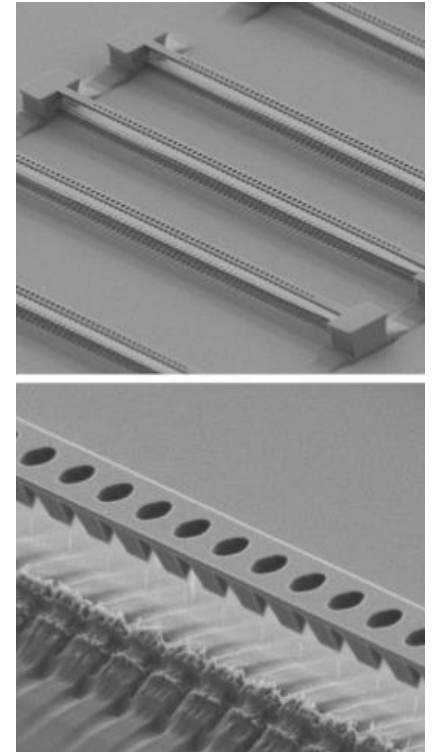
Faraon et al., *New J. Phys.* **15** 025010 (2013)
 Faraon et al., *Nat. Photon.* **5**, 301 (2011)

2D photonic crystal



Faraon et. al, *PRL* **109**, 033604 (2012)
 Riedrich-Möller et al.,
Appl. Phys. Lett. **106**, 221103 (2015)

nanobeam photonic crystal



Hausmann et al., *Nano Lett.* **13**, 5791 (2013)
 Burek et al., *Nat. Commun.* **5**, 5718 (2014)
 Li et al., *Nat. Commun.* **6**, 6173 (2015)
 Sipahigil et. al, *Science* 354, **847** (2016)

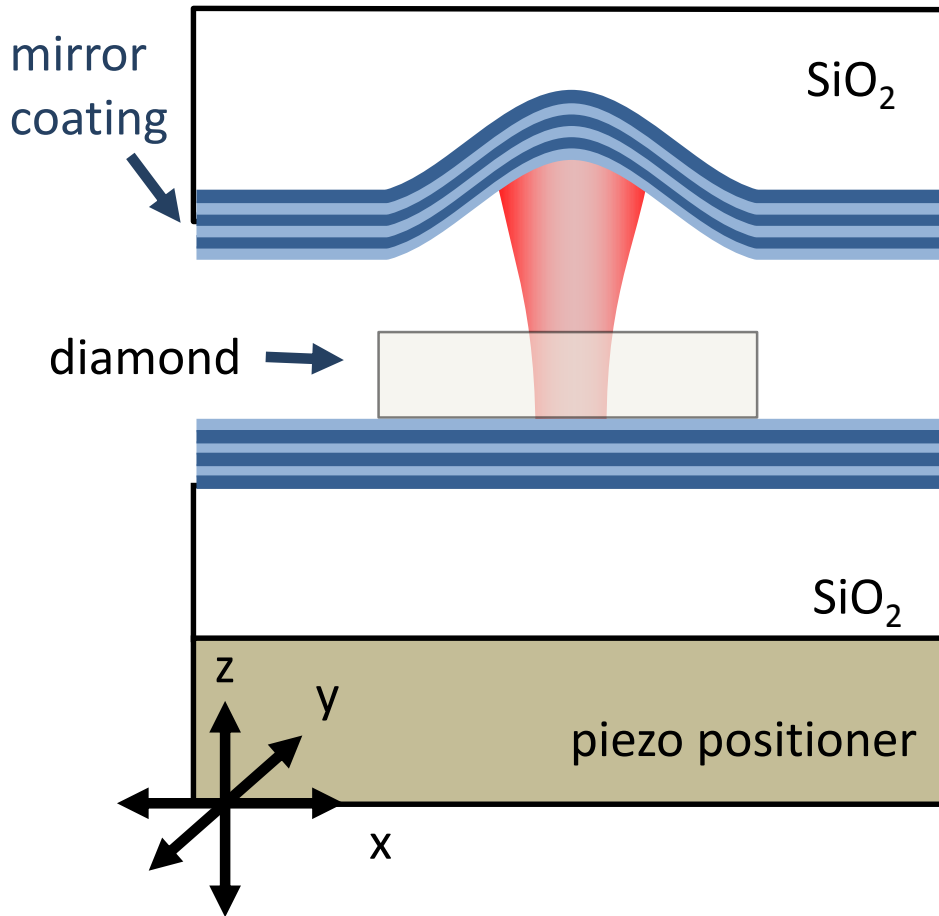
Key result:

- up to 70-fold enhancement of emission rate

Challenges:

- spatial and spectral overlap
- high Q-factors
- efficient outcoupling
- emitter stability

Fully tunable microcavity design



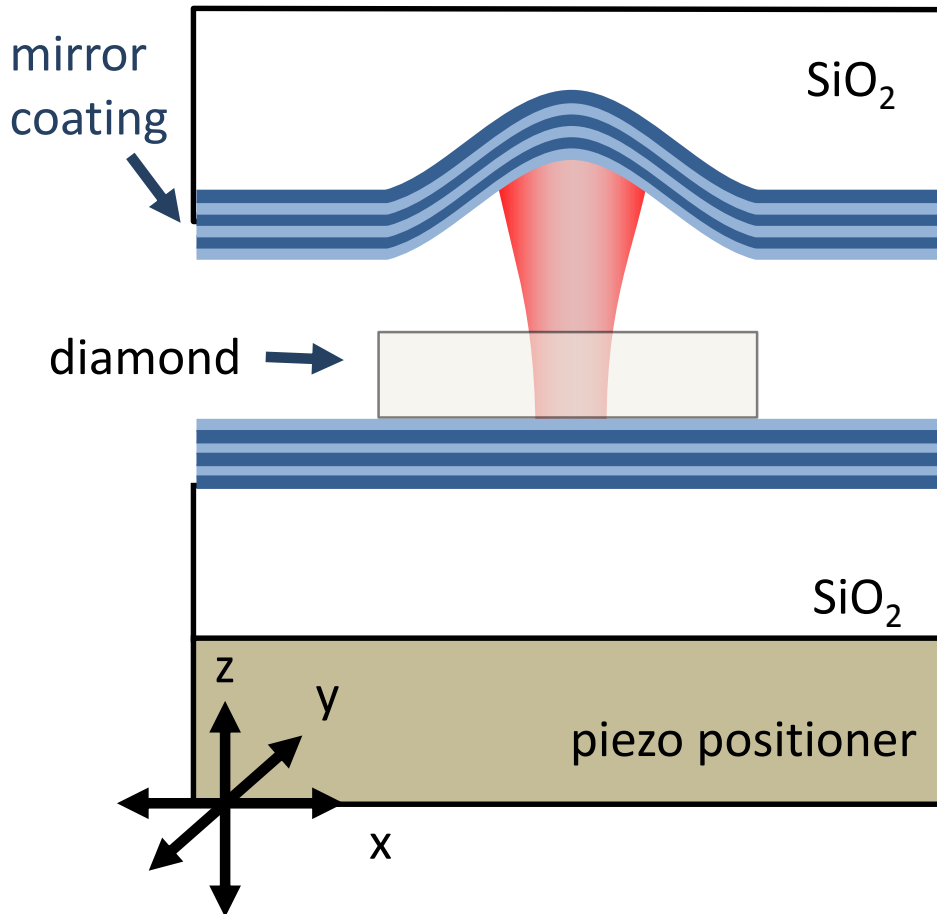
Experiments on quantum dots:

Barbour et al., J. Appl. Phys. **110**, 053107 (2011)

Greuter et al., Appl. Phys. Lett. **105**, 121105 (2014)

Greuter et al., Phys. Rev. B **92**, 045302 (2015)

Fully tunable microcavity design



Advantages of microcavity design:

- minimal diamond processing (low spectral fluctuations)
- well-defined Gaussian output mode
- full *in situ* tunability:
 - resonance wavelength
 - spatial overlap
 - select favourable NV
- small mode volume V
- high Q factor

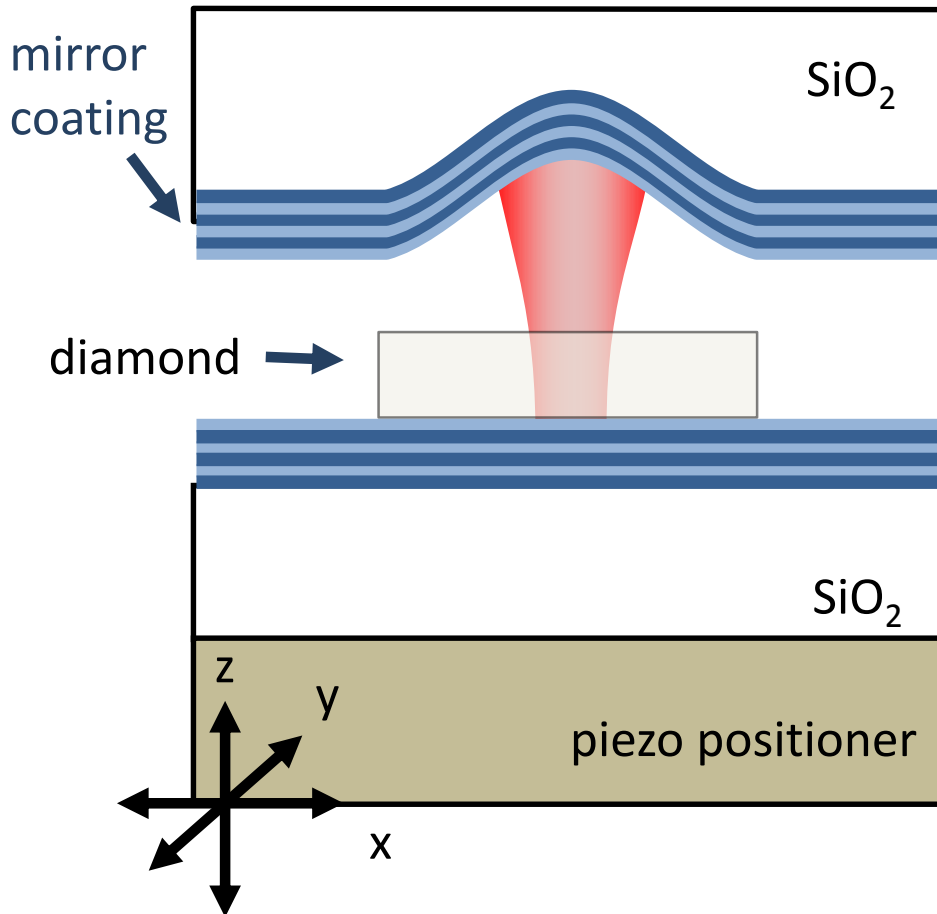
Experiments on quantum dots:

Barbour et al., J. Appl. Phys. **110**, 053107 (2011)

Greuter et al., Appl. Phys. Lett. **105**, 121105 (2014)

Greuter et al., Phys. Rev. B **92**, 045302 (2015)

Fully tunable microcavity design



Advantages of microcavity design:

- minimal diamond processing (low spectral fluctuations)
- well-defined Gaussian output mode
- full *in situ* tunability:
 - resonance wavelength
 - spatial overlap
 - select favourable NV
- small mode volume V
- high Q factor

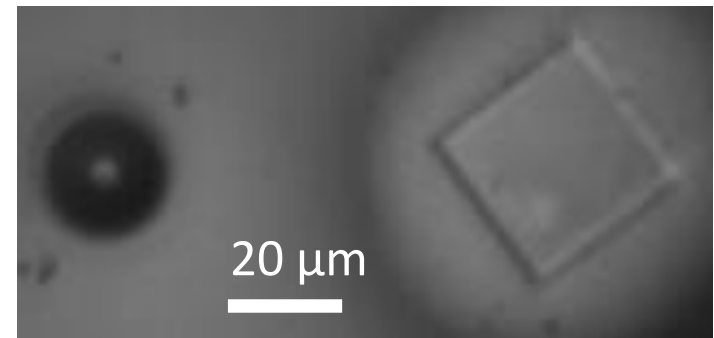
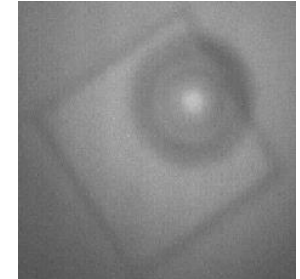
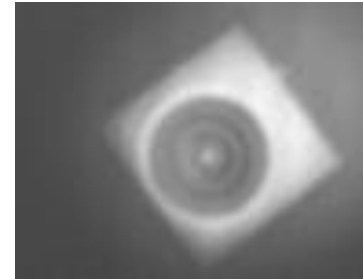
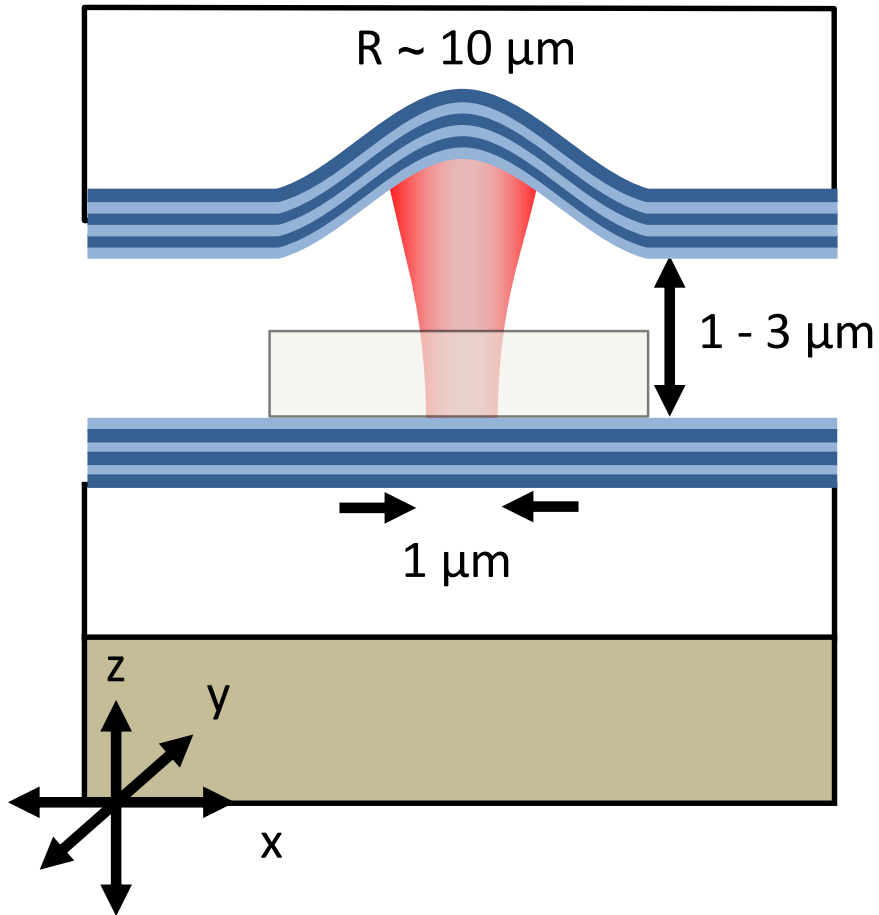
Experiments on quantum dots:

Barbour et al., J. Appl. Phys. **110**, 053107 (2011)
 Greuter et al., Appl. Phys. Lett. **105**, 121105 (2014)
 Greuter et al., Phys. Rev. B **92**, 045302 (2015)

Proof of concept using nanodiamonds:

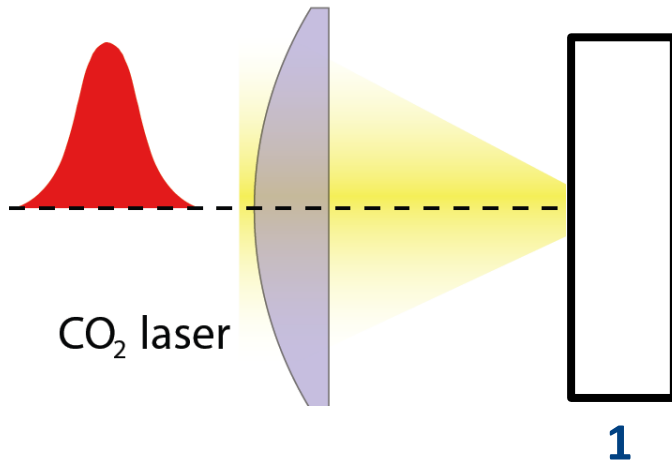
Albrecht et al., PRL **110**, 243602 (2013)
 Johnson et al., New J. Phys. **17**, 122003 (2015)
 Kaupp et al., Phys. Rev. Applied **6**, 054010 (2016)

Fully tunable microcavity design



Integration of a microscopic diamond membrane into microcavity

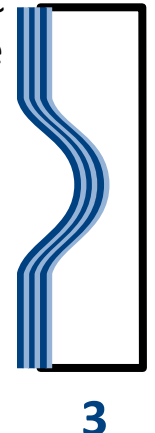
Fabrication of curved mirror templates



Concave depression:
R ~ 5 ... 500 μm



Dielectric reflective coating



Pulsed CO₂ – laser radiation:

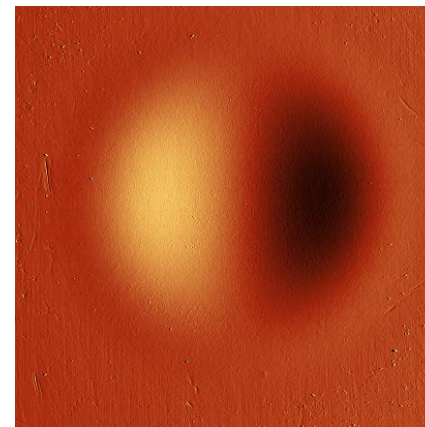
- surface atomically smooth

high Q factor

- small radius of curvature

small mode volume V

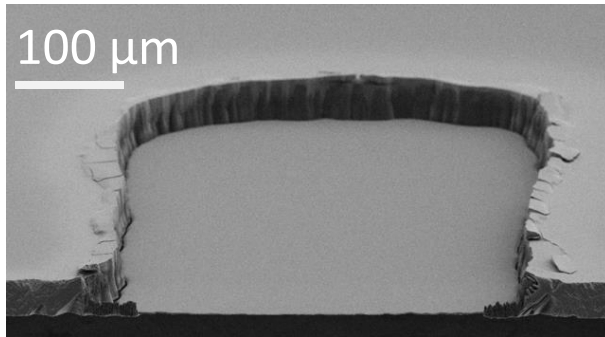
Hunger et al., AIP Adv. **2**, 012119 (2012)
Najer et al., Appl. Phys. Lett. **110**, 011101 (2017)



AFM – phase image

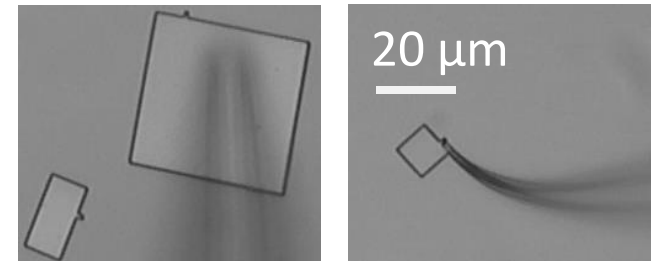
Fabrication of diamond membranes

Commercially available diamond and nitrogen implantation + annealing

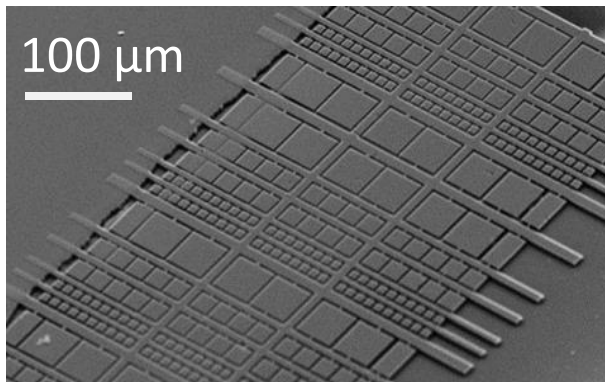


ICP
etching

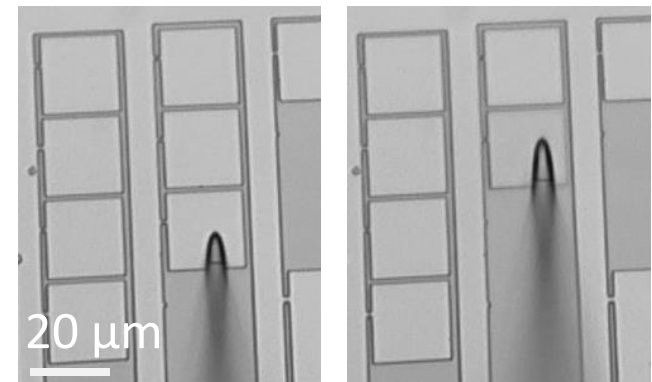
van der Waals bonding



electron beam
lithography



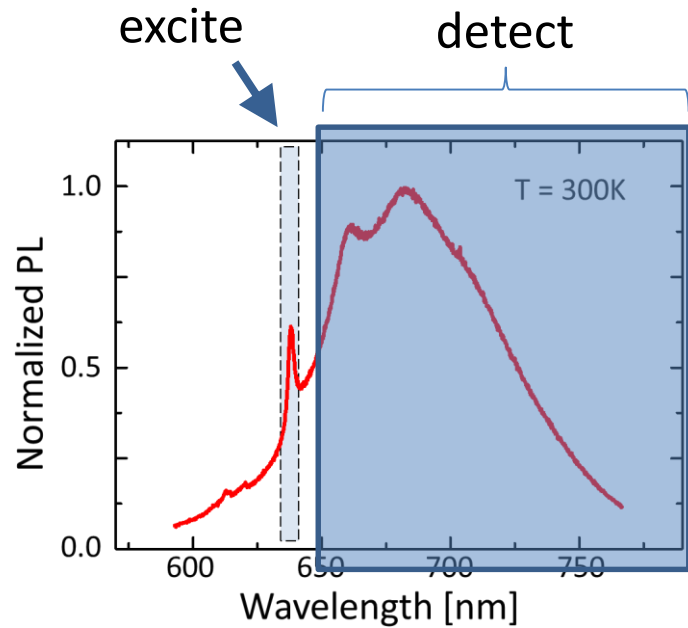
micro
manipulator



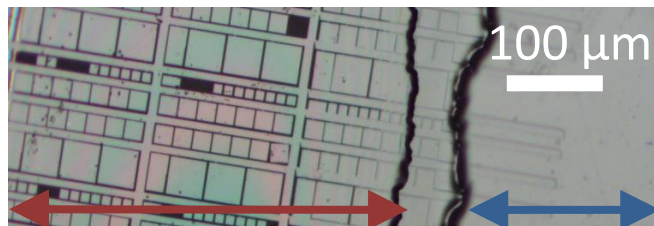
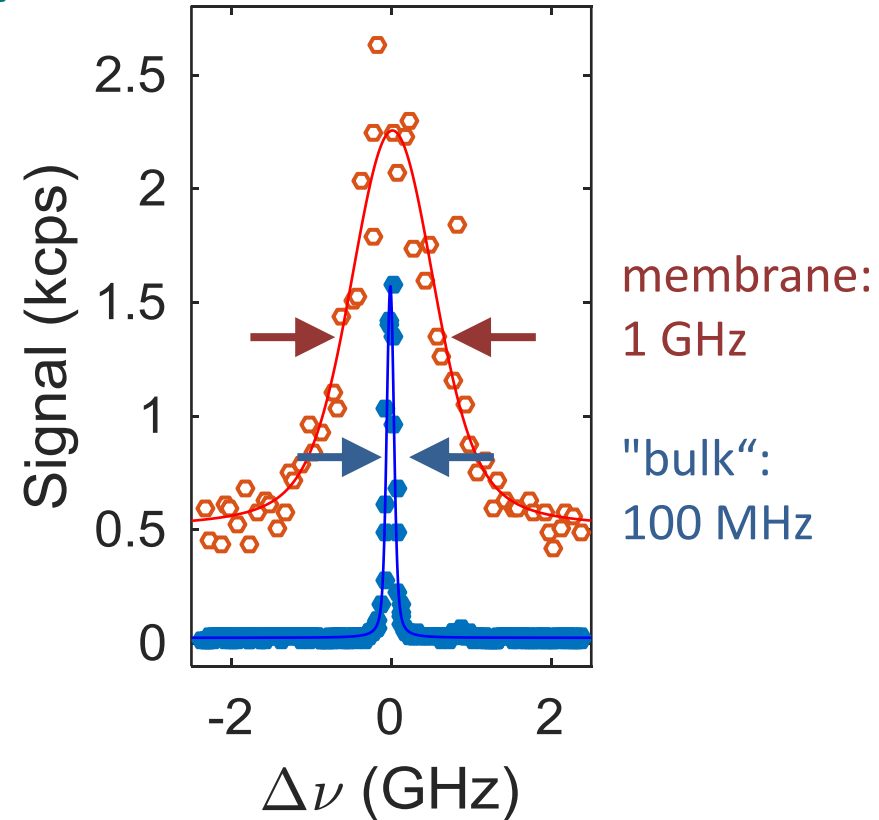
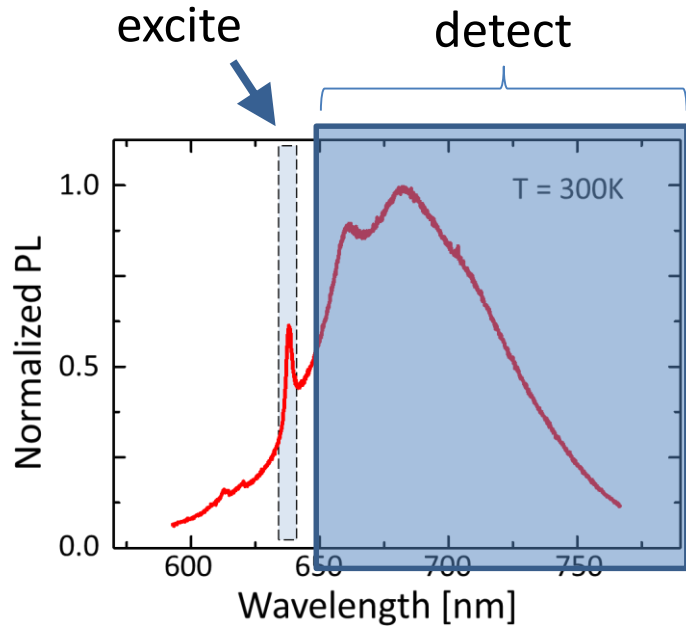
Appel et al., Rev. Sci. Instrum. **87**, 063703 (2016)
Maletinsky et al., Nat. Nanotechnol. **7**, 320 (2012)

DR et al., Phys. Rev. Appl. **2**, 064011 (2014)

Photoluminescence excitation measurement



Photoluminescence excitation measurement

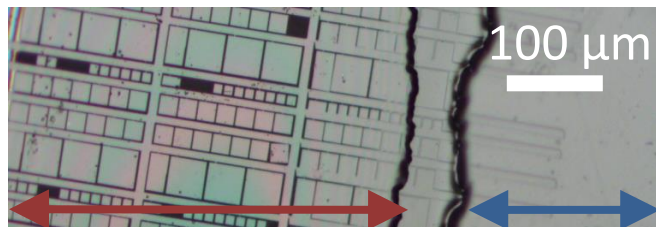
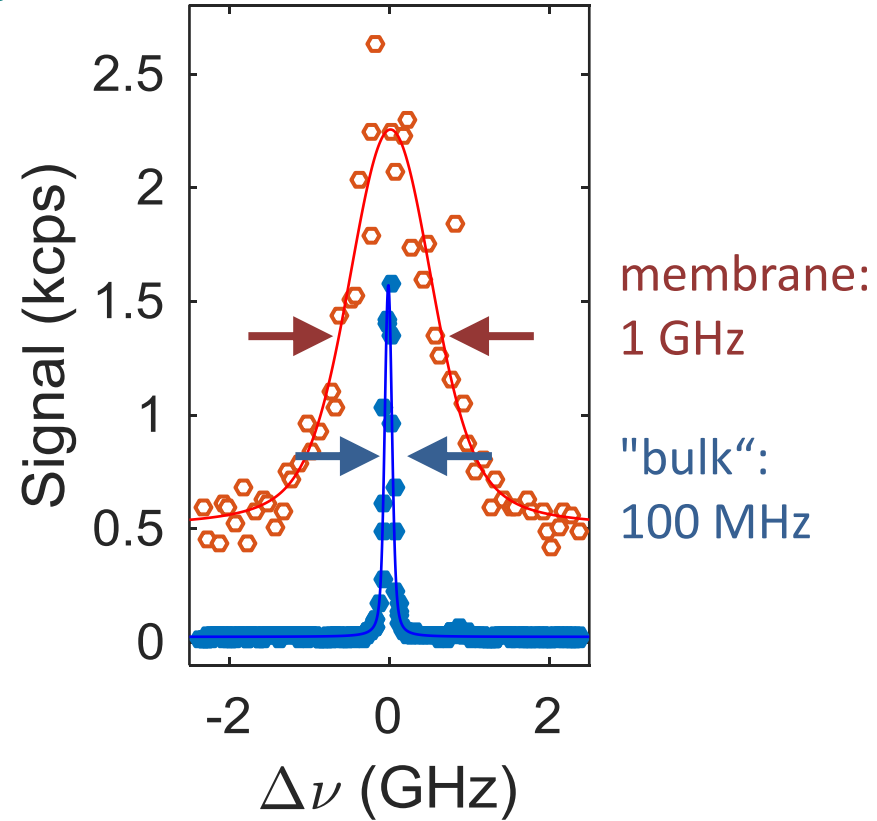
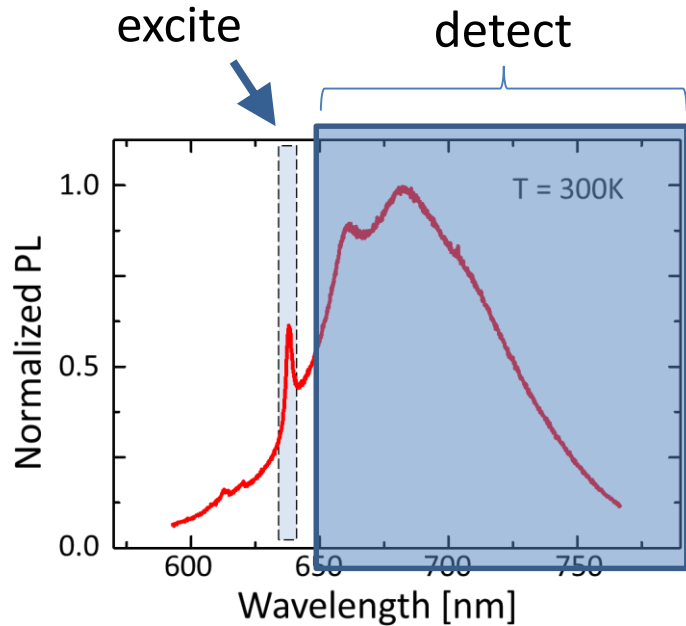


membrane
d ~ 1 μm

"bulk"
d ~ 40 μm

Linewidth measurements

Photoluminescence excitation measurement

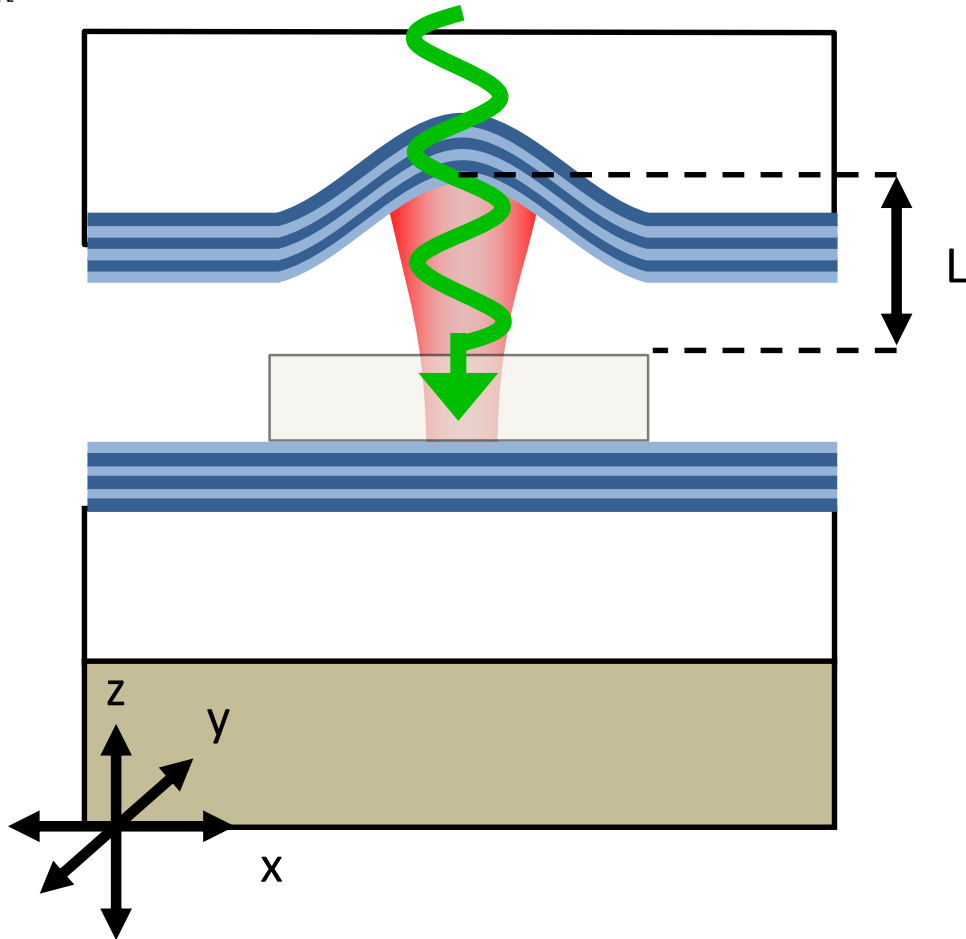


membrane
d ~ 1 μm

"bulk"
d ~ 40 μm

linewidth smaller than ground
state spin splitting: 2.87 GHz

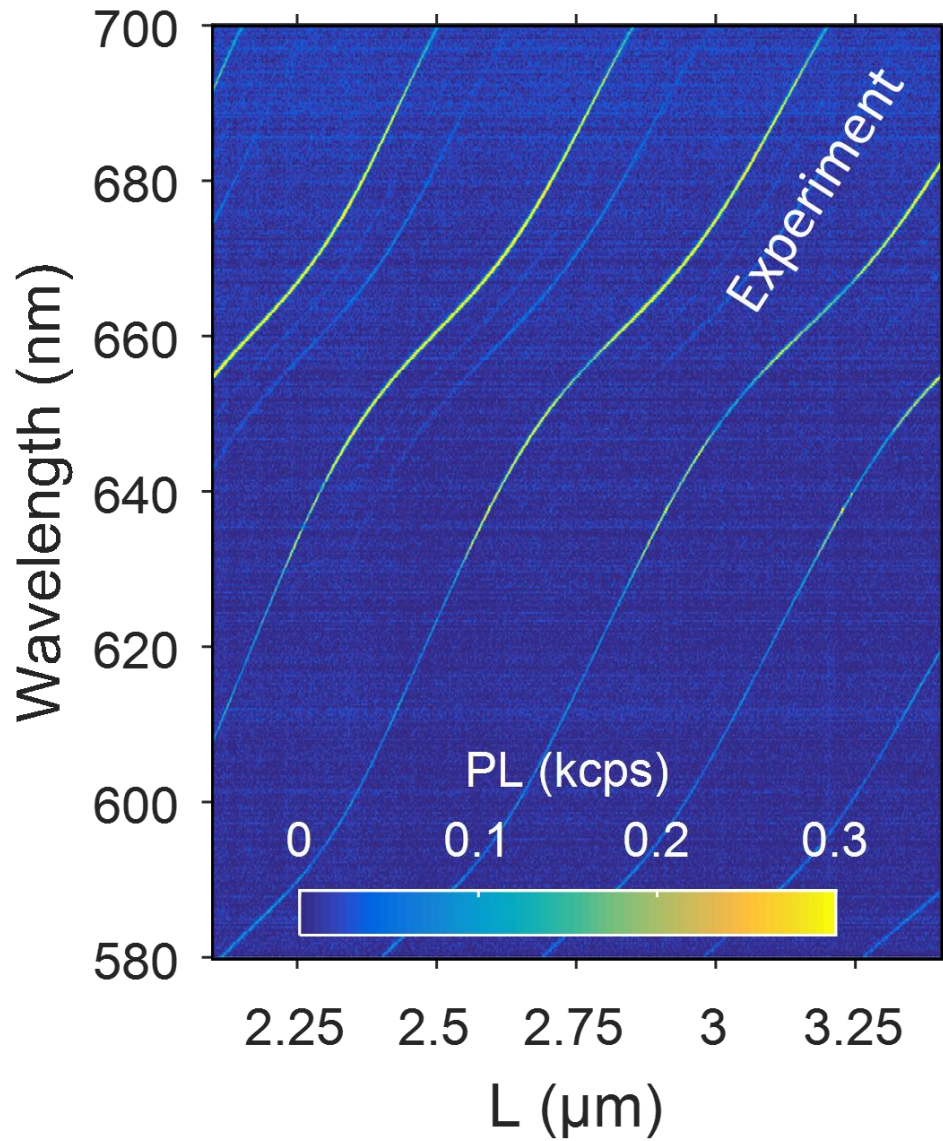
Cavity characterization



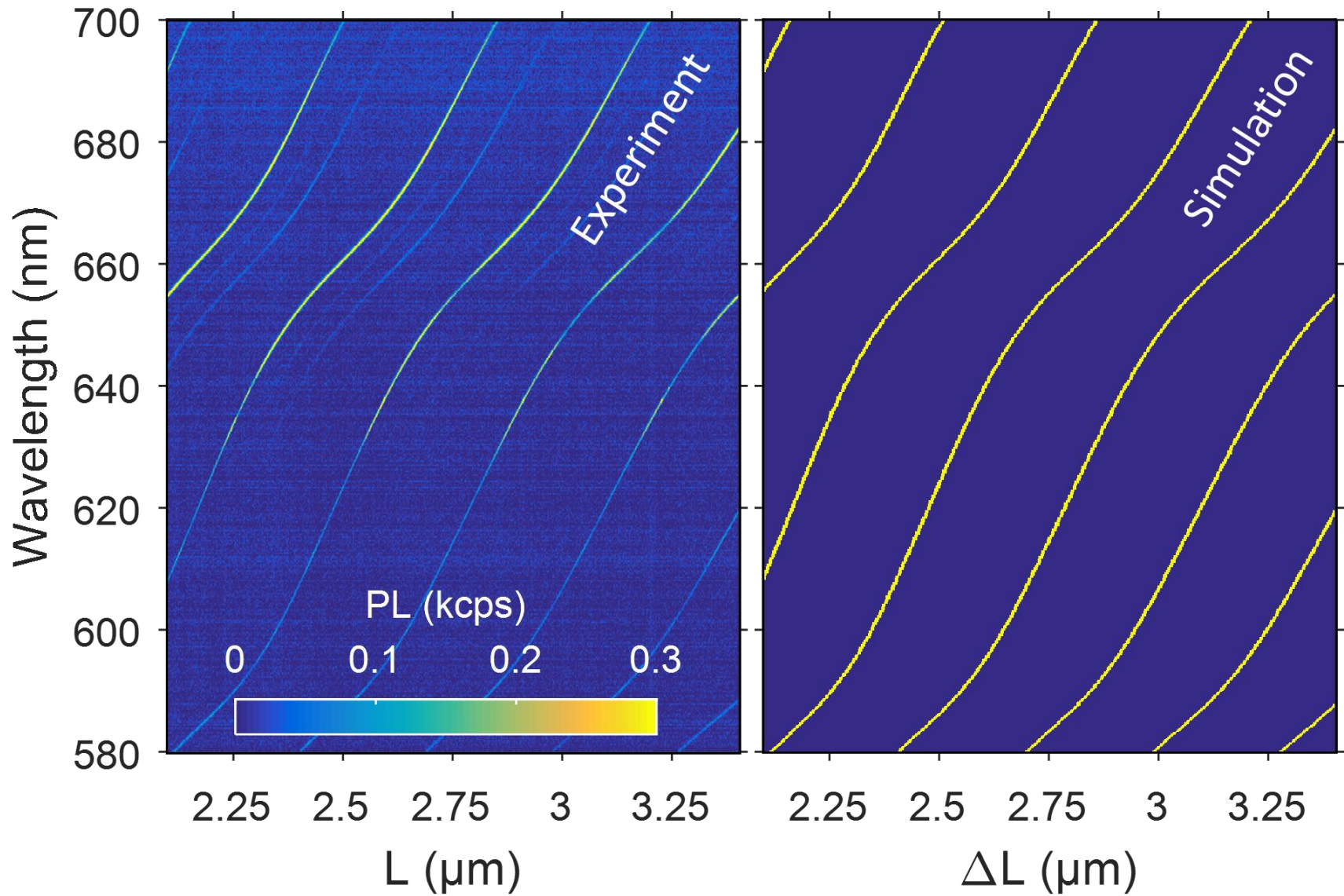
Analyze cavity mode structure:

- couple green laser
- tune width of air gap L
- record photoluminescence (PL) spectra for different L

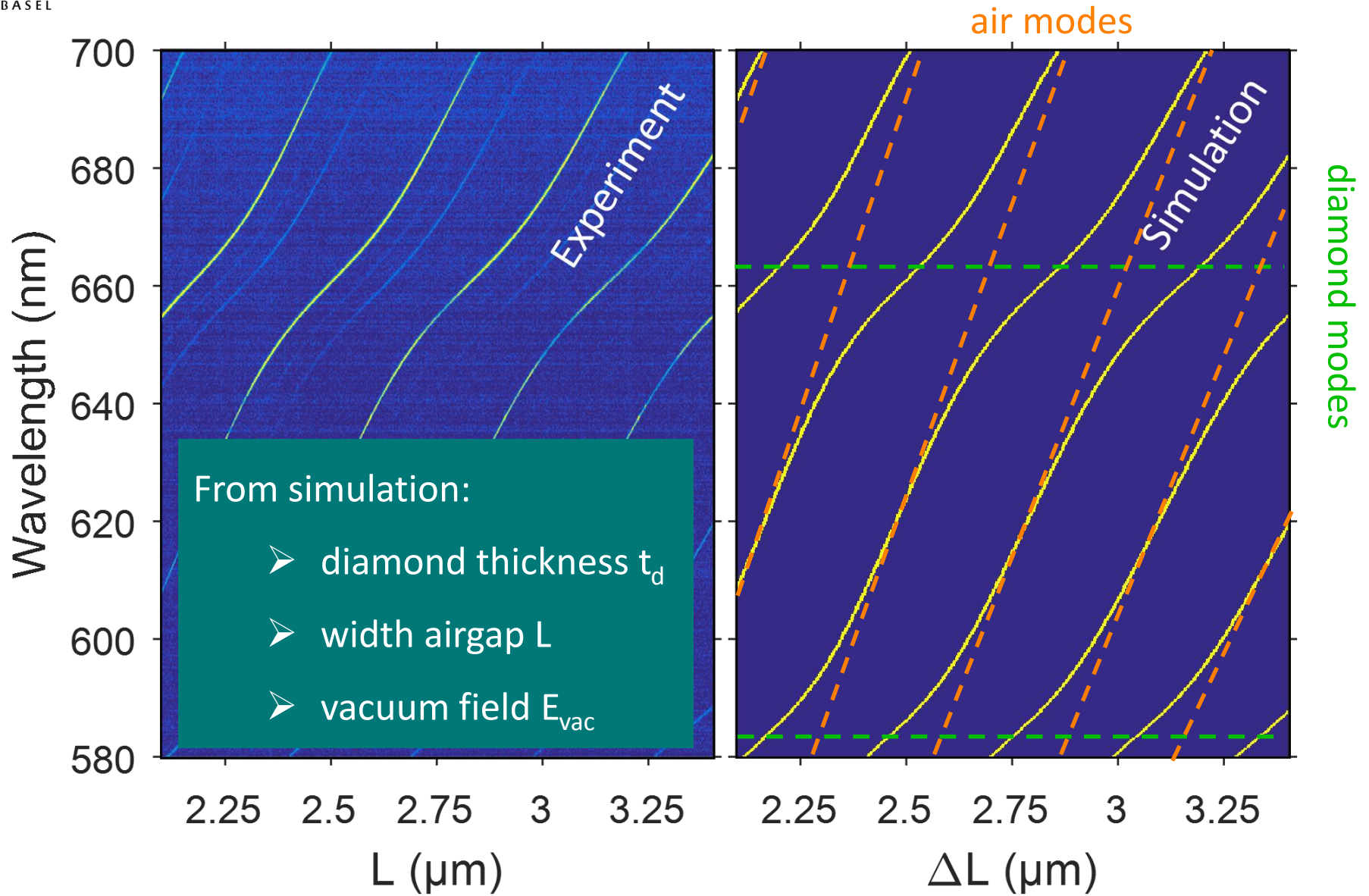
PL vs. air gap width L



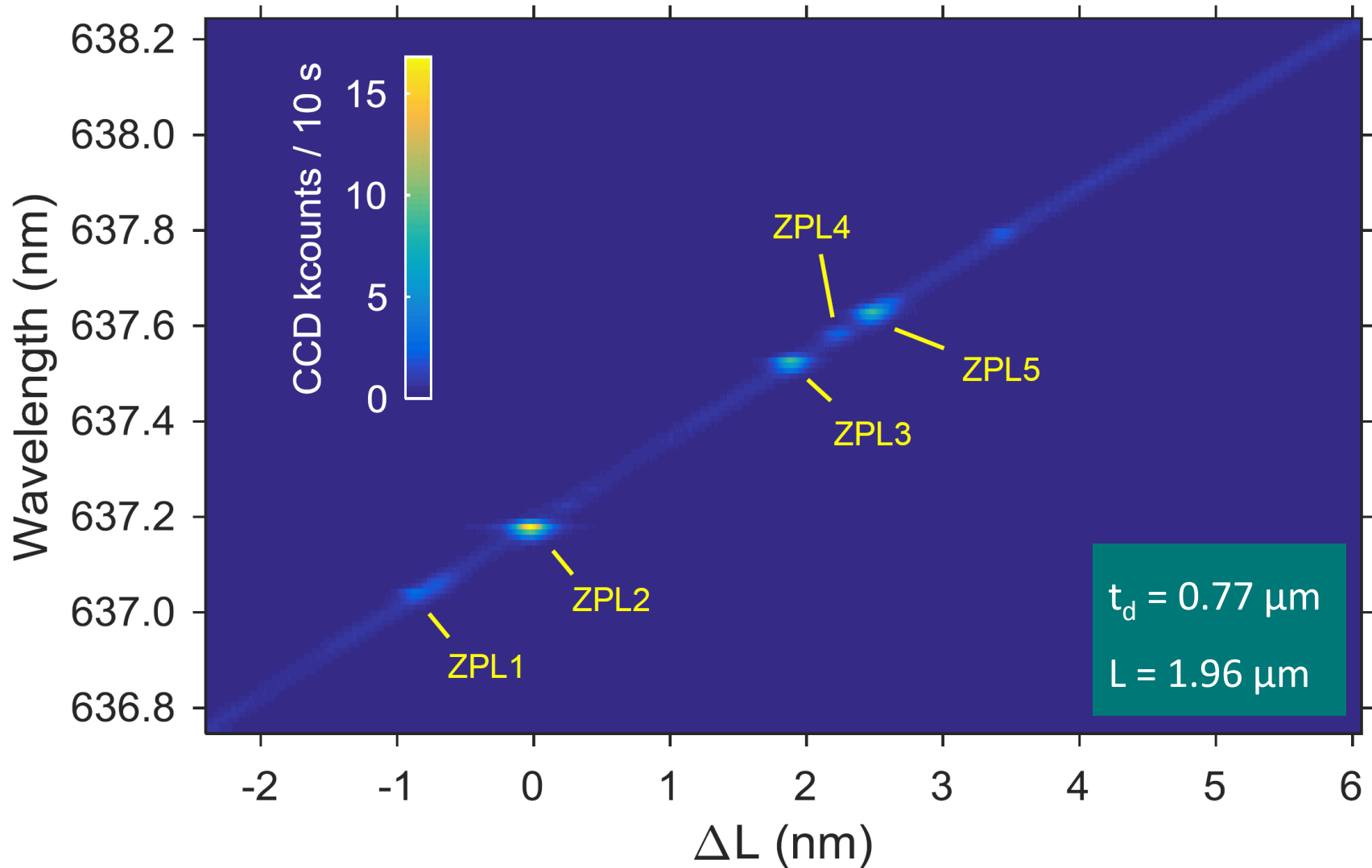
PL vs. air gap width L



PL vs. air gap width L

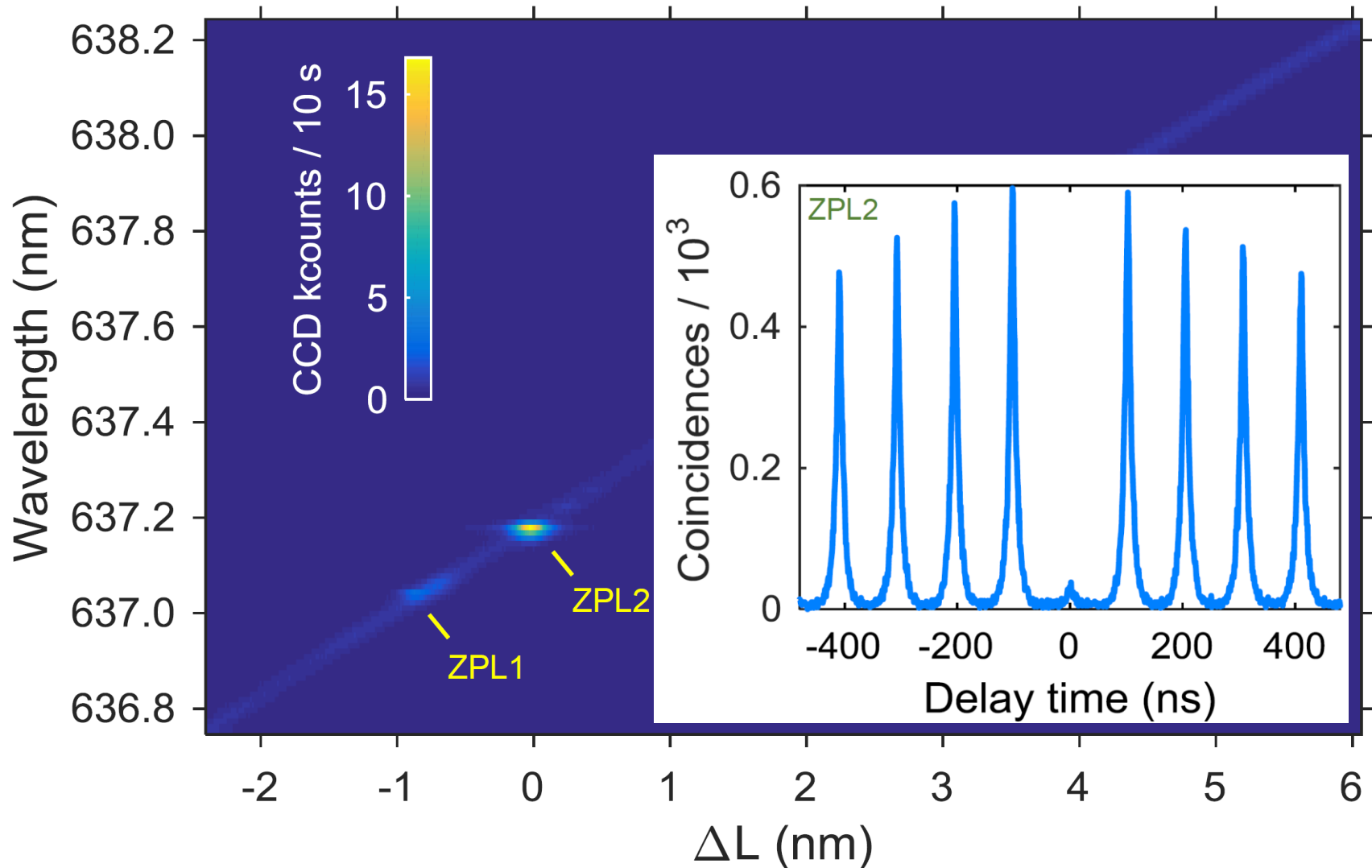


PL vs. relative detuning ΔL



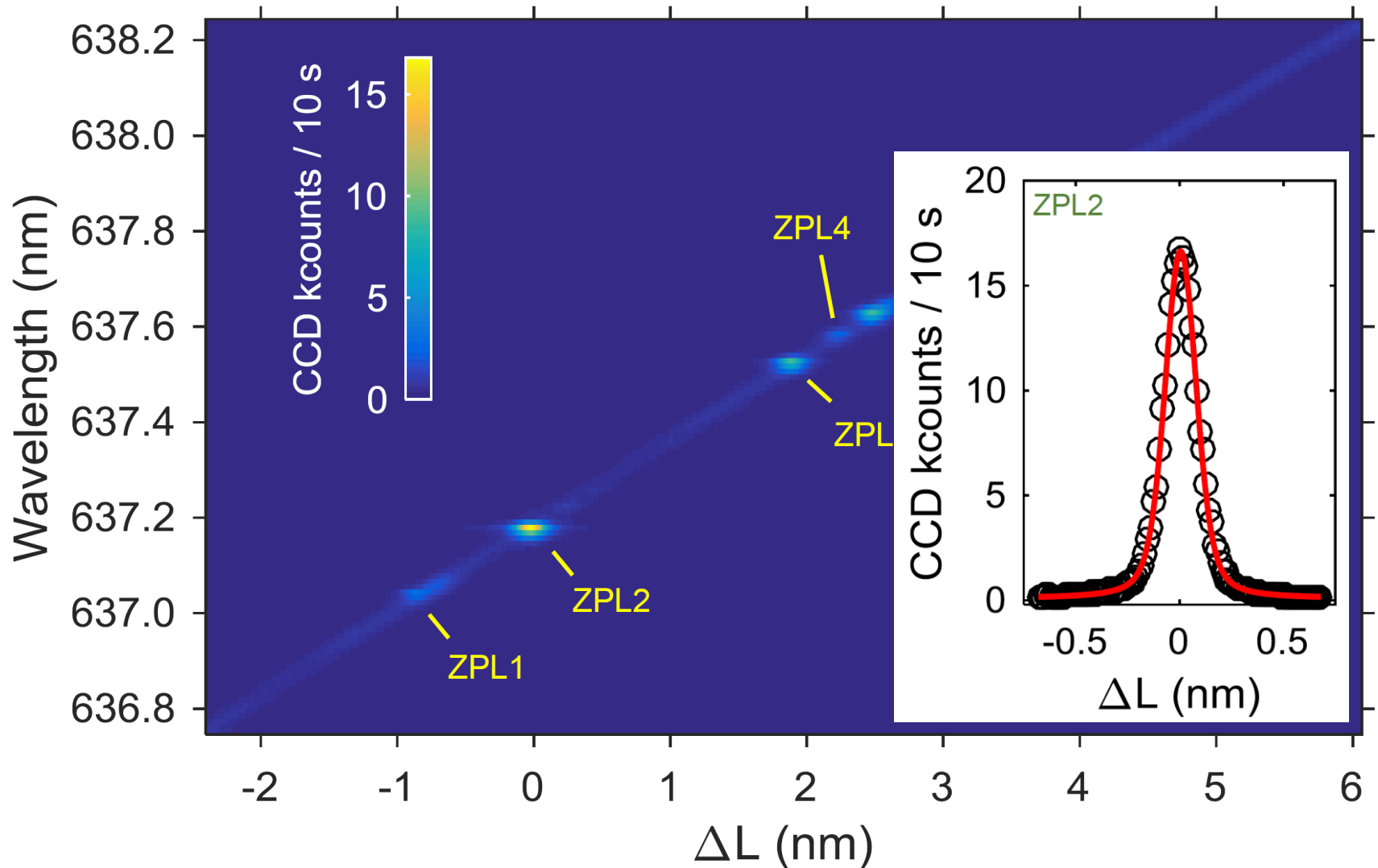
PL vs. relative detuning ΔL

➤ Clear single emitter signature in photon autocorrelation

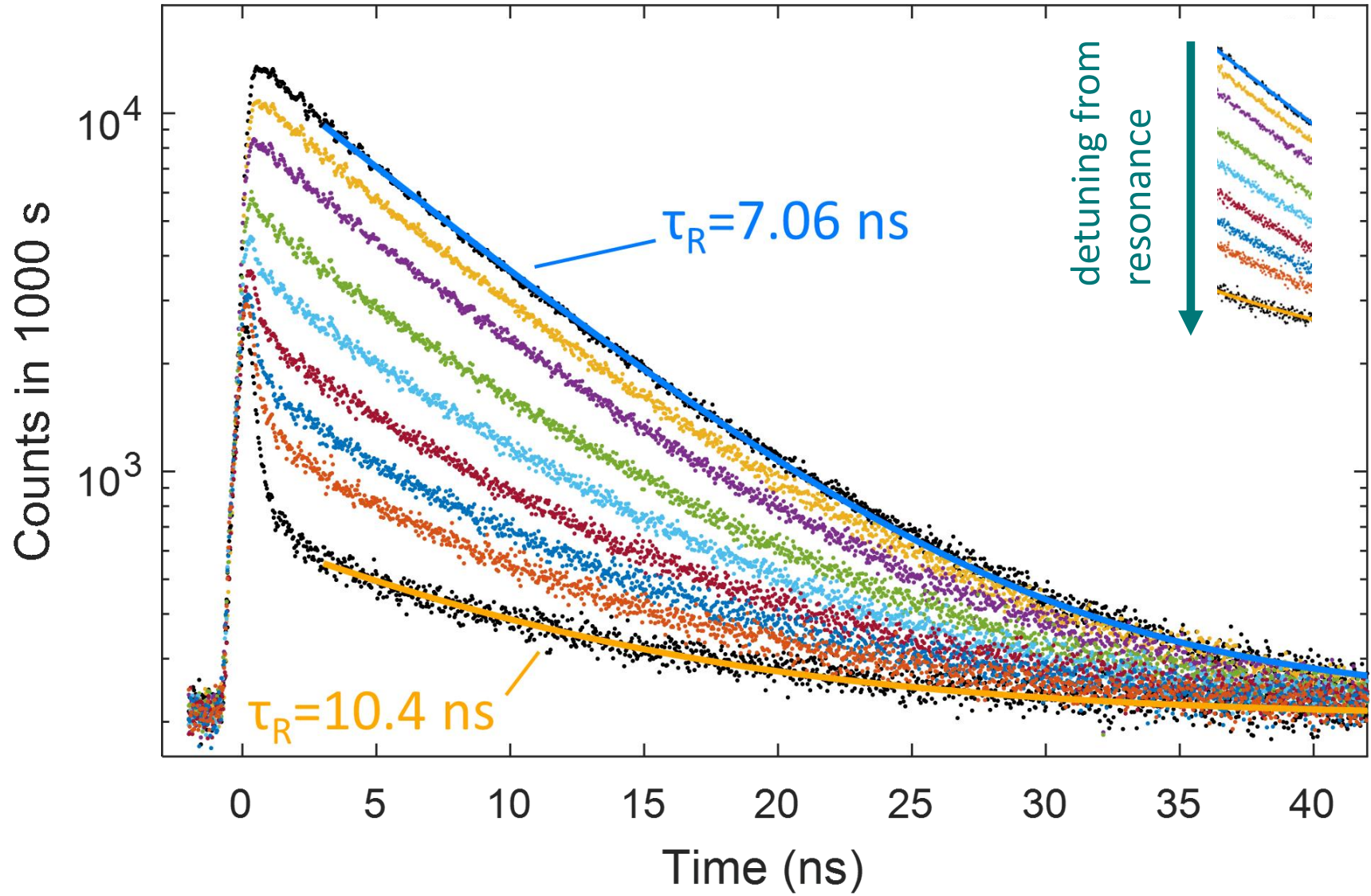


PL vs. relative detuning ΔL

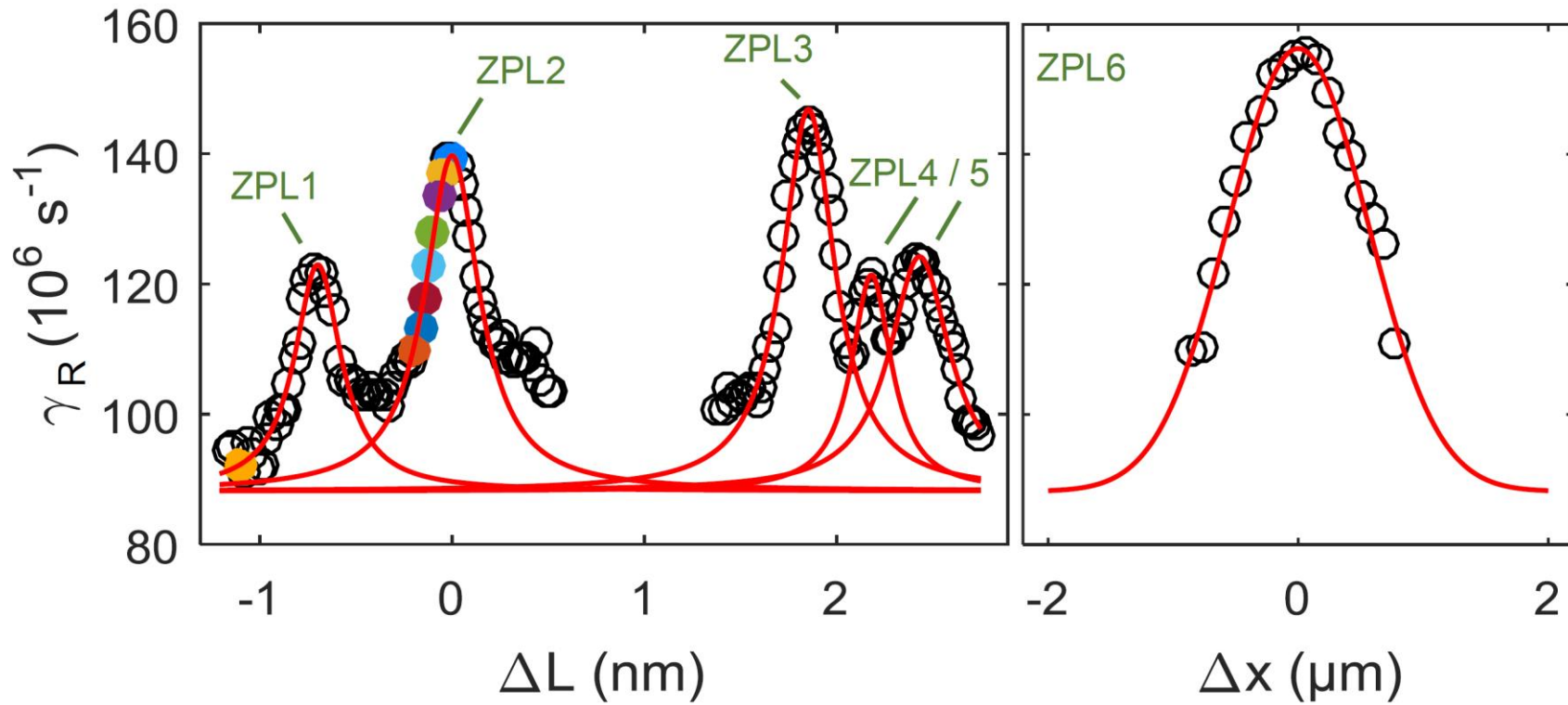
➤ Q factor: 58500 $\kappa = \omega / Q = 5.06 \cdot 10^{10} \text{ s}^{-1}$



Lifetime NV2: spectral detuning

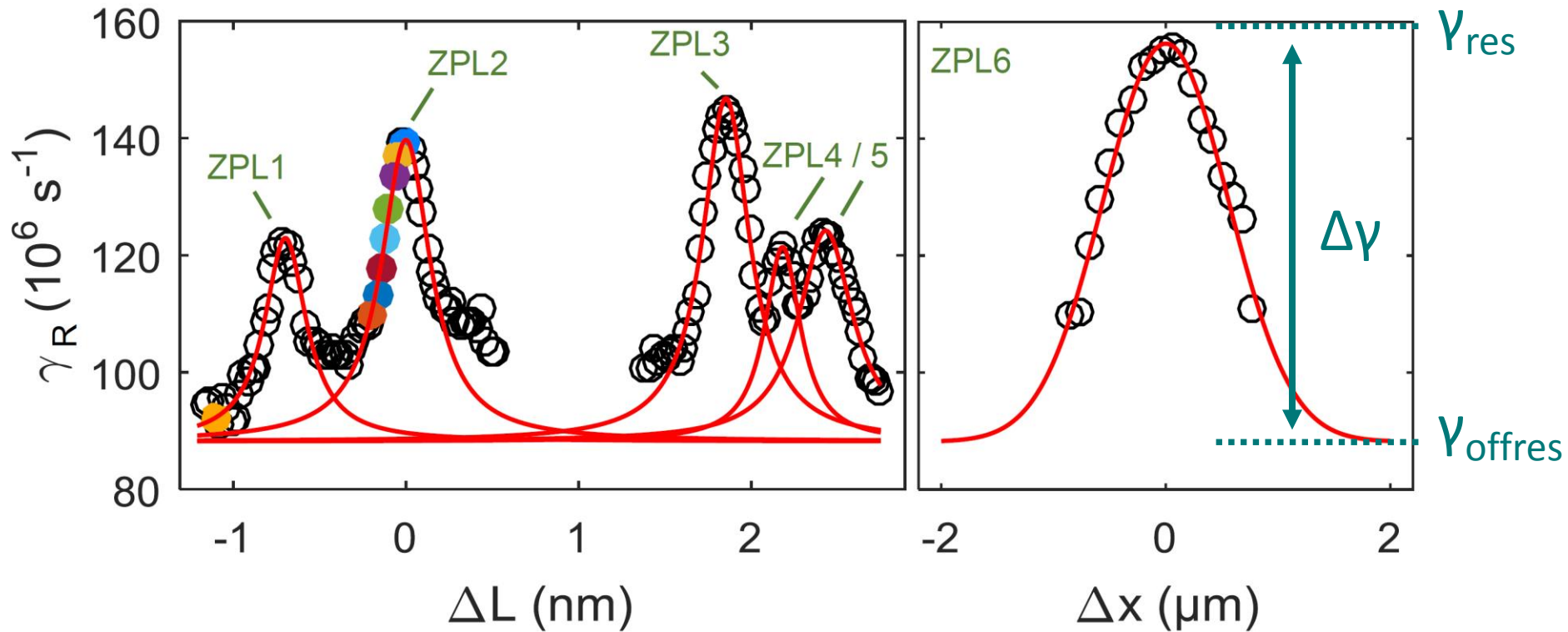


Lifetime NV2: spectral + spatial detuning



Full *in situ* control of the cavity system

Lifetime NV2: spectral + spatial detuning



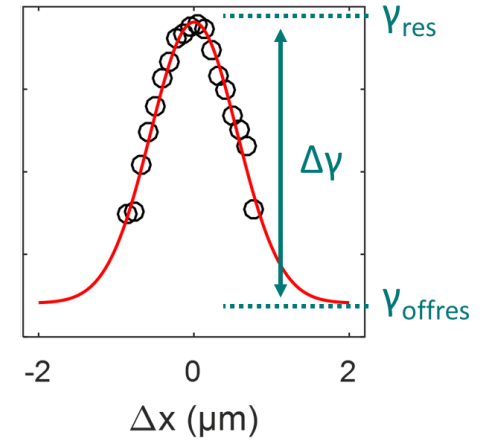
Full *in situ* control of the cavity system

$$\gamma_{\text{res}} = 158 \cdot 10^6 \text{ s}^{-1} \quad \gamma_{\text{offres}} = 88.2 \cdot 10^6 \text{ s}^{-1} \quad \Delta\gamma = 69.8 \cdot 10^6 \text{ s}^{-1}$$

Experimental results:

$$\gamma_{\text{res}} = 158 \cdot 10^6 \text{ s}^{-1}, \gamma_{\text{offres}} = 88.2 \cdot 10^6 \text{ s}^{-1}, \Delta\gamma = 69.8 \cdot 10^6 \text{ s}^{-1}$$

$$\gamma_{\text{NV}} = 79.4 \cdot 10^6 \text{ s}^{-1} \text{ (measurement without top mirror)}$$



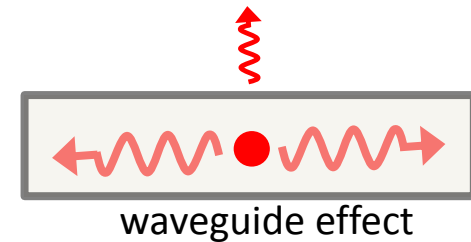
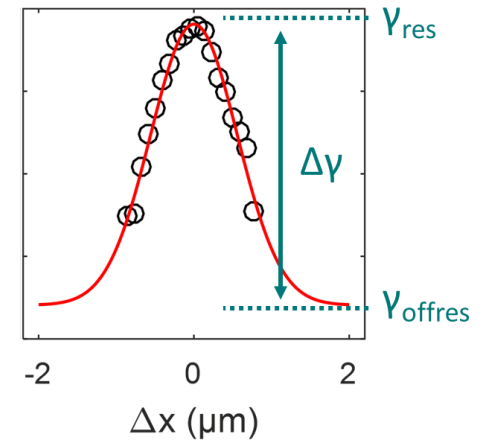
Experimental results:

$$\gamma_{\text{res}} = 158 \cdot 10^6 \text{ s}^{-1}, \gamma_{\text{offres}} = 88.2 \cdot 10^6 \text{ s}^{-1}, \Delta\gamma = 69.8 \cdot 10^6 \text{ s}^{-1}$$

$$\gamma_{\text{NV}} = 79.4 \cdot 10^6 \text{ s}^{-1} \text{ (measurement without top mirror)}$$

Overall enhancement:

$$F_P = \gamma_{\text{res}} / \gamma_{\text{NV}} = 2.0$$



Results

Experimental results:

$$\gamma_{\text{res}} = 158 \cdot 10^6 \text{ s}^{-1}, \gamma_{\text{offres}} = 88.2 \cdot 10^6 \text{ s}^{-1}, \Delta\gamma = 69.8 \cdot 10^6 \text{ s}^{-1}$$

$$\gamma_{\text{NV}} = 79.4 \cdot 10^6 \text{ s}^{-1} \text{ (measurement without top mirror)}$$

Overall enhancement:

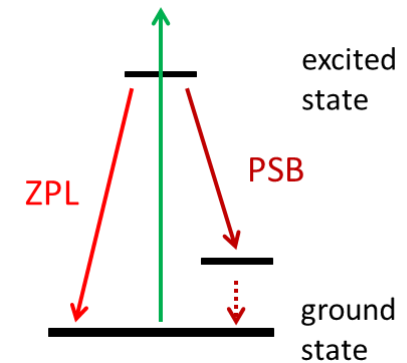
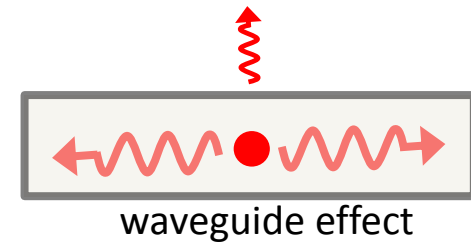
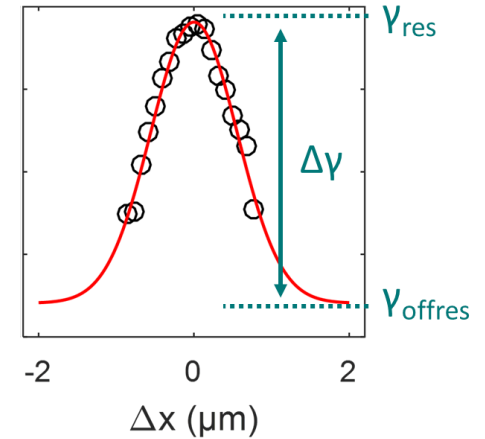
$$F_P = \gamma_{\text{res}} / \gamma_{\text{NV}} = 2.0$$

Purcell enhancement of ZPL:

Fraction of ZPL emission in bulk: $\sim 3\%$

$$\gamma_{\text{ZPL}} = 2.38 \cdot 10^6 \text{ s}^{-1}$$

$$F_{P,\text{ZPL}} = \Delta\gamma / \gamma_{\text{ZPL}} + 1 = 30.3$$



Experimental results:

$$\gamma_{\text{res}} = 158 \cdot 10^6 \text{ s}^{-1}, \gamma_{\text{offres}} = 88.2 \cdot 10^6 \text{ s}^{-1}, \Delta\gamma = 69.8 \cdot 10^6 \text{ s}^{-1}$$

$$\gamma_{\text{NV}} = 79.4 \cdot 10^6 \text{ s}^{-1} \text{ (measurement without top mirror)}$$

Overall enhancement:

$$F_P = \gamma_{\text{res}} / \gamma_{\text{NV}} = 2.0$$

Purcell enhancement of ZPL:

Fraction of ZPL emission in bulk: $\sim 3\%$

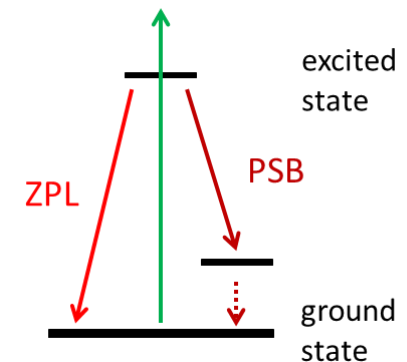
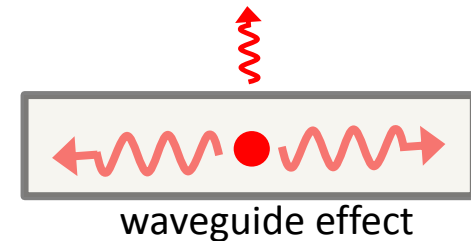
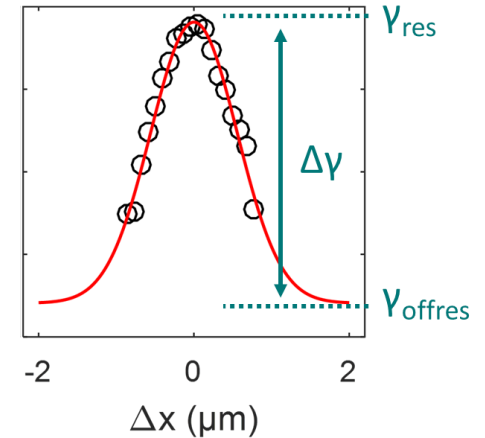
$$\gamma_{\text{ZPL}} = 2.38 \cdot 10^6 \text{ s}^{-1}$$

$$F_{P,ZPL} = \Delta\gamma / \gamma_{\text{ZPL}} + 1 = 30.3$$

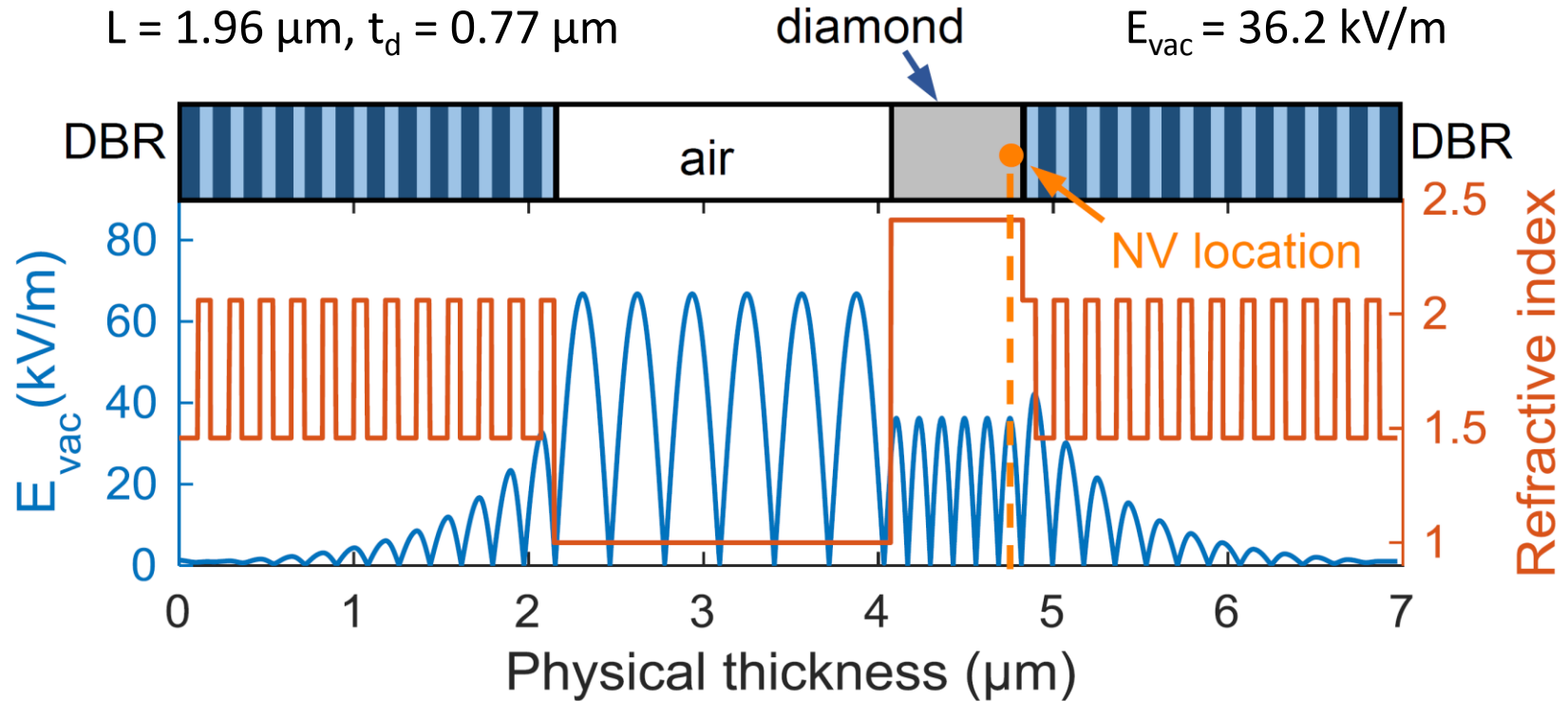
Fraction of ZPL emission in cavity:

$$\eta = (\Delta\gamma + \gamma_{\text{ZPL}}) / \gamma_{\text{res}} = 45.7\%$$

before: $\sim 3\%$

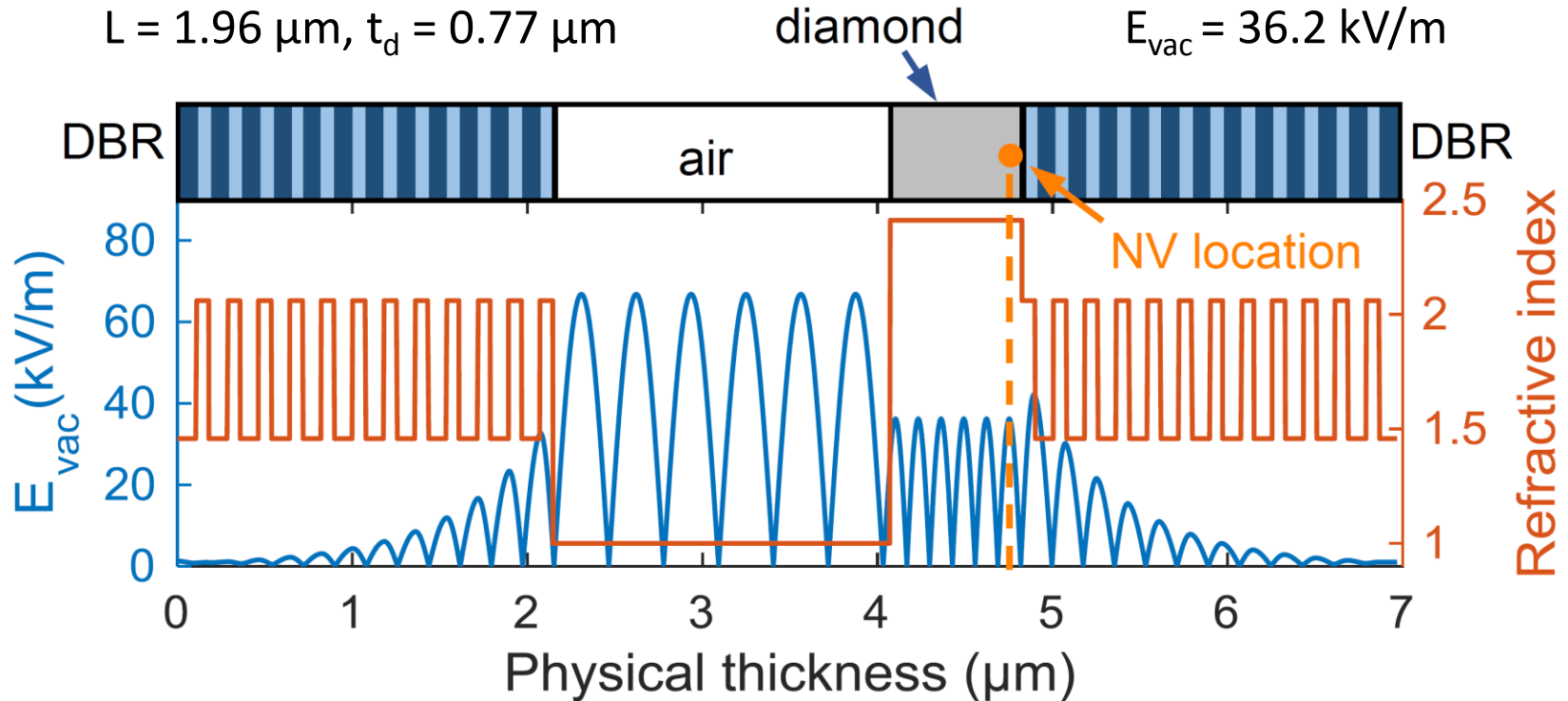


Calculation of expected Purcell enhancement



1D-transfer matrix calculation + Gaussian lateral confinement

Calculation of expected Purcell enhancement



1D-transfer matrix calculation + Gaussian lateral confinement

$$\gamma_{\text{NV}} = 79.4 \cdot 10^6 \text{ s}^{-1} \quad \kappa = 5.06 \cdot 10^{10} \text{ s}^{-1} \quad g = 5.97 \cdot 10^9 \text{ s}^{-1}$$

Theoretical Purcell enhancement:

$$F_p = 4 g^2 / (\kappa \gamma_{\text{NV}}) = 35.5$$

Current experiment:

$$\gamma_{NV} = 79.4 \cdot 10^6 \text{ s}^{-1}$$

$$\kappa = 5.06 \cdot 10^{10} \text{ s}^{-1}$$

$$g = 5.97 \cdot 10^9 \text{ s}^{-1}$$

Best air-confined cavity:

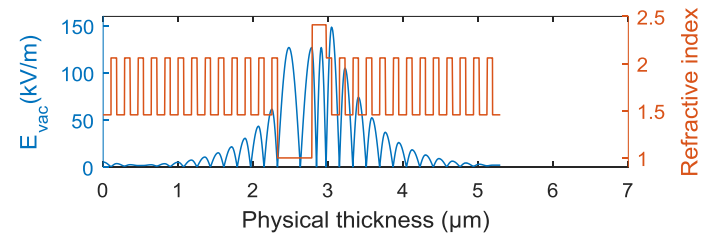
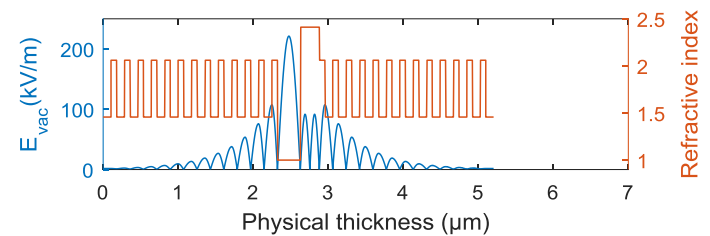
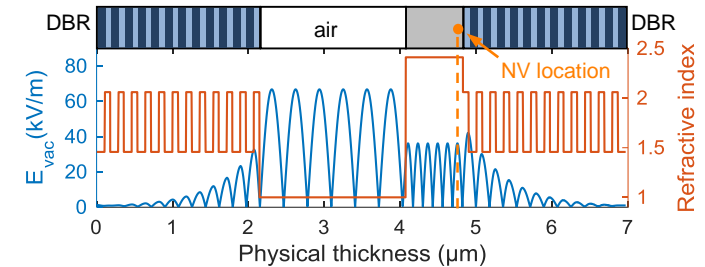
$$g = 1.41 \cdot 10^{10} \text{ s}^{-1}, \kappa = 2g$$

$$F_{P,air} = 356$$

Best diamond-confined cavity:

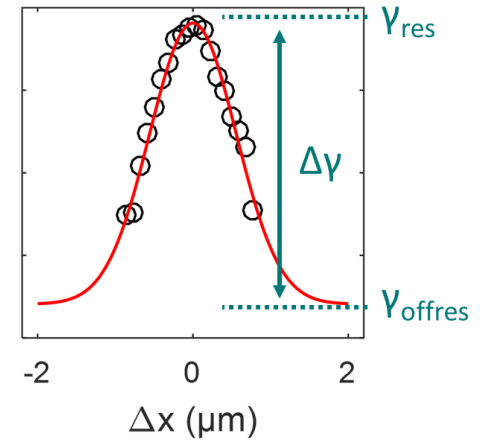
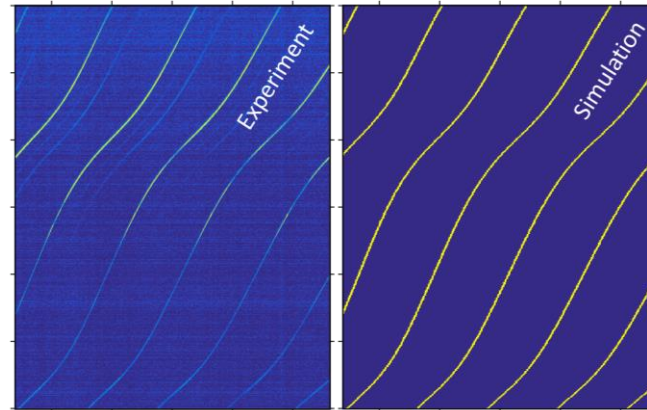
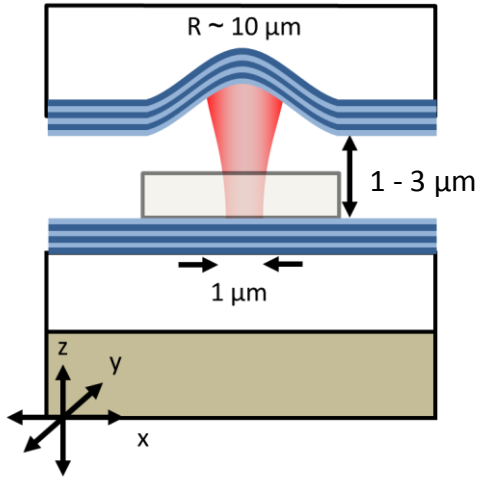
$$g = 2.09 \cdot 10^{10} \text{ s}^{-1}, \kappa = 2g$$

$$F_{P,dia} = 527$$



Potential enhancement of entanglement rate: 10^6

Conclusion and outlook



✓ Theoretical model

✓ Fully tunable microcavity

D. Riedel et al.,
submitted

✓ Purcell enhancement

Outlook:

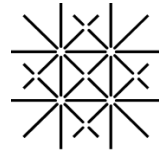
- integrate microwave for spin control of NV centers
- improve Q/V - enhancement > 500 feasible
- other colour centres in diamond (SiV, GeV), silicon carbide, ...



Acknowledgements



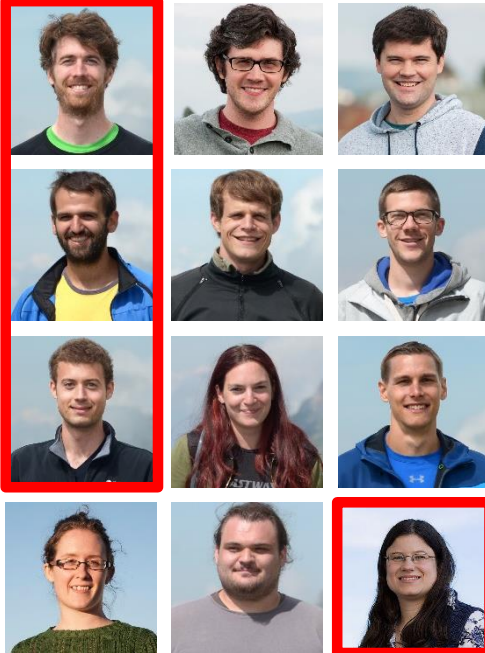
Patrick
Maletinsky



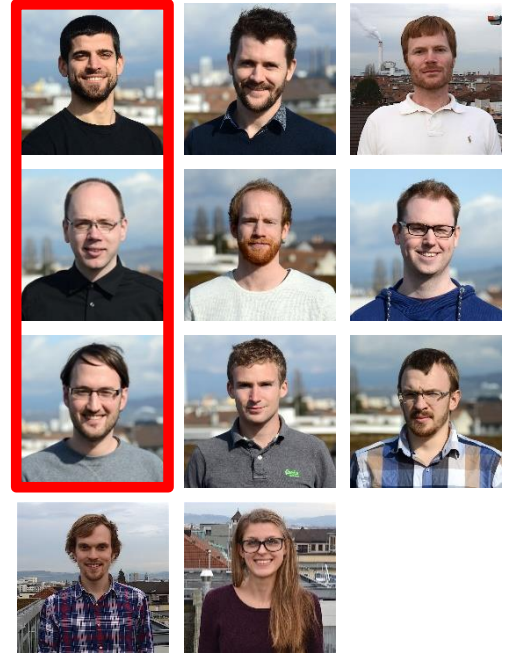
Universität
Basel



Richard J.
Warburton



Uni Saarbrücken



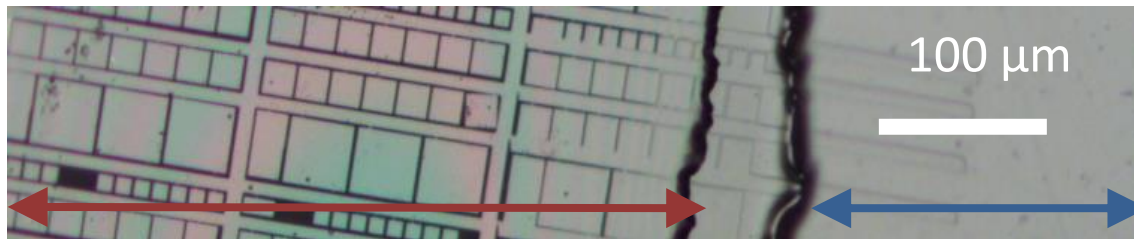
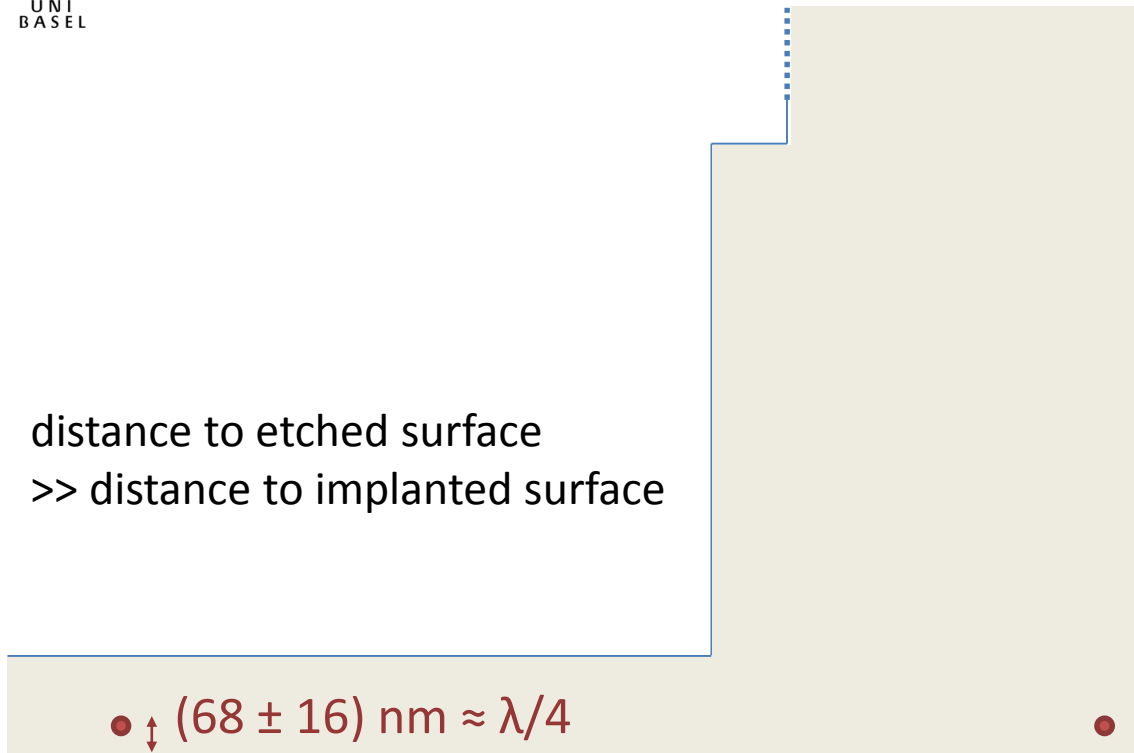
<https://quantum-sensing.ch/>

<https://nano-photonics.unibas.ch/>



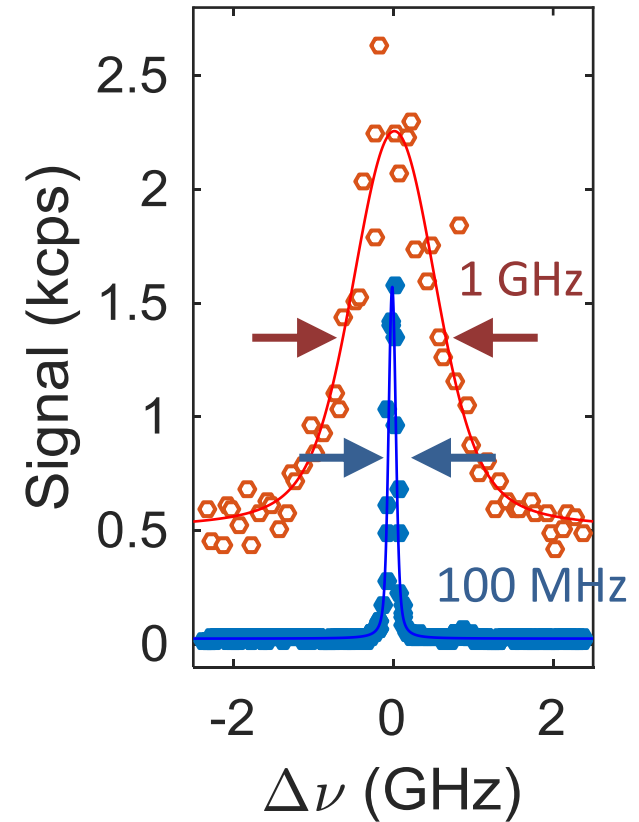
EINE INITIATIVE DER UNIVERSITÄT BASEL
UND DES KANTONS AARGAU

Linewidth measurements

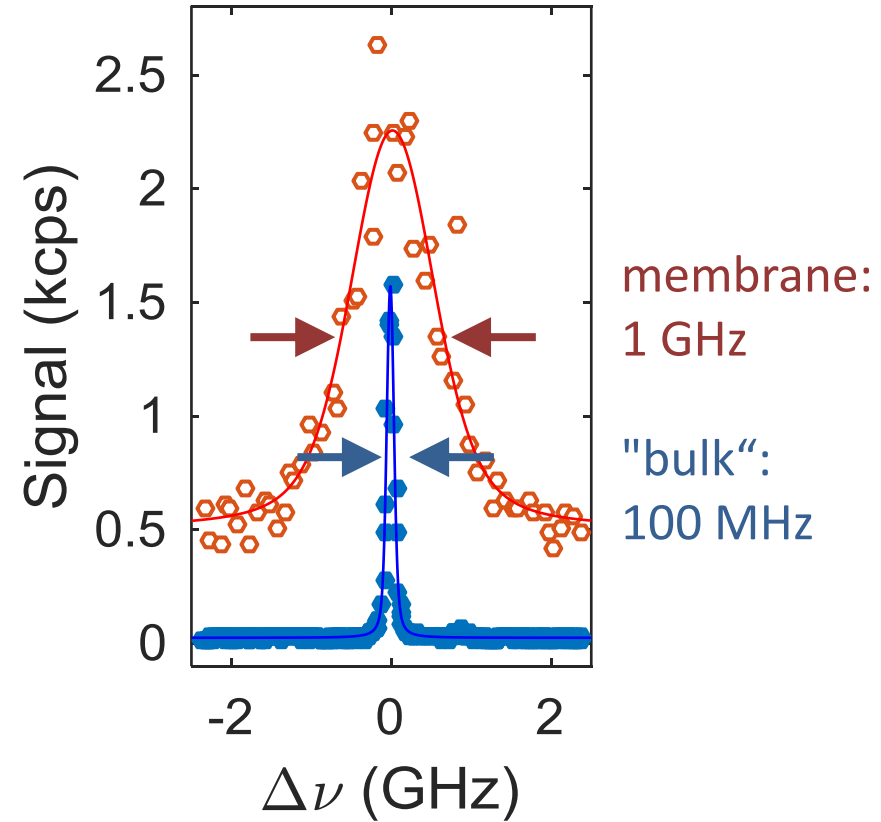
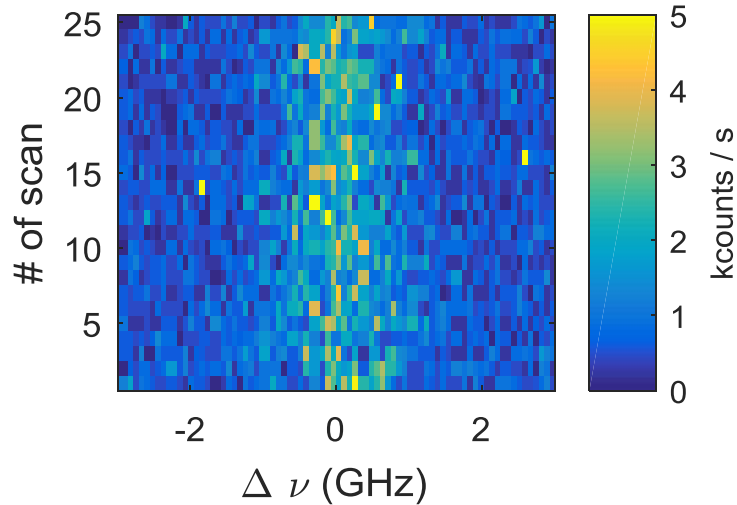
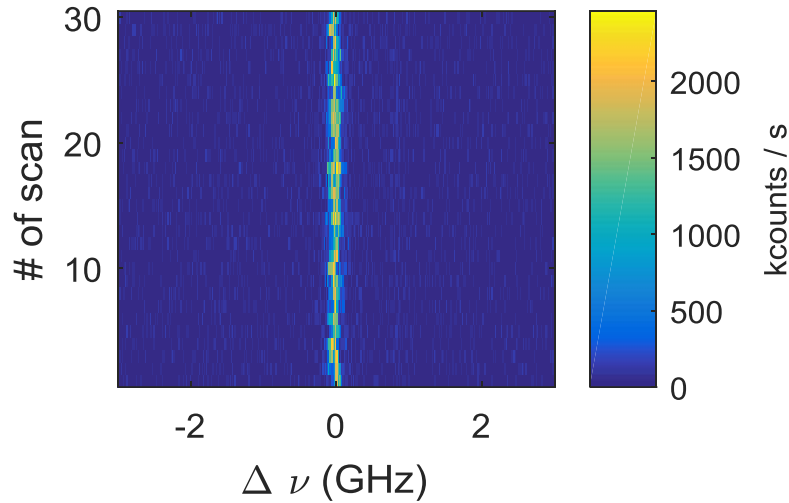


membrane
 $d \sim 1 \mu\text{m}$

"bulk"
 $d \sim 40 \mu\text{m}$

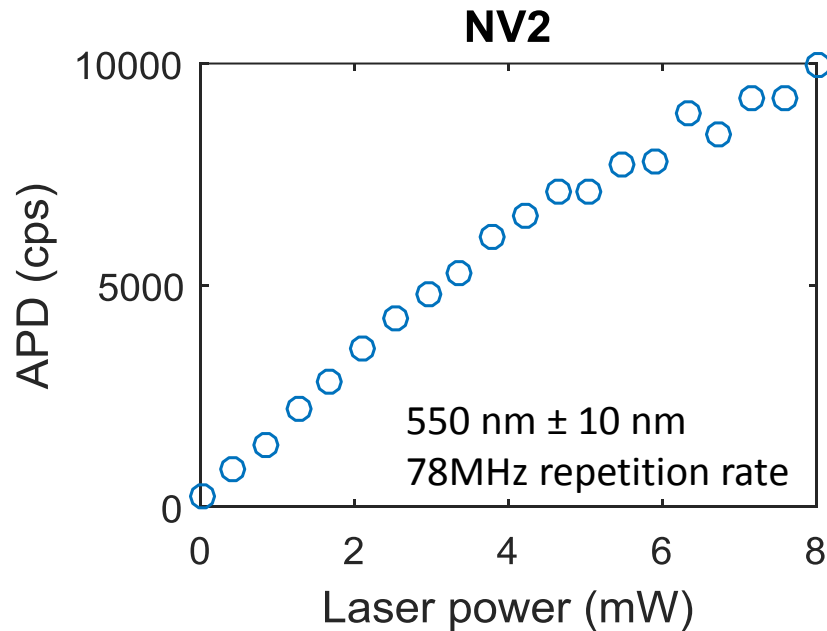


Linewidth measurements



membrane
 $d \sim 1 \mu\text{m}$

"bulk"
 $d \sim 40 \mu\text{m}$



Low count rate due to losses:

$$T = 1 - R - A$$

(T:= Transmissivity of mirror coating)

(R:= Reflectivity of mirror coating)

(A:= Absorption and scattering losses)

Transmission of tunable red diode laser:
~ 4%

Ideal transmission: 100%

→ Factor of 25 for lossless mirrors /
no scattering, no absorption

Optical cavity - Purcell enhancement

$$\frac{W_{\text{cav}}}{W_{\text{free}}} = F_{\text{P}} = \frac{3}{4\pi^2} \left(\frac{\lambda_{\text{cav}}}{n} \right)^3 \frac{Q}{V_{\text{cav}}}$$

Transition rate for spontaneous emission:

$$W_{12} = \frac{2\pi}{\hbar^2} |M_{12}|^2 g(\omega)$$

Increased DOS - High Q
Confined E_{vac} - Small V

Transition matrix element:

$$|M_{12}|^2 = \langle \vec{p} \cdot \vec{E}_{\text{vac}} \rangle^2$$

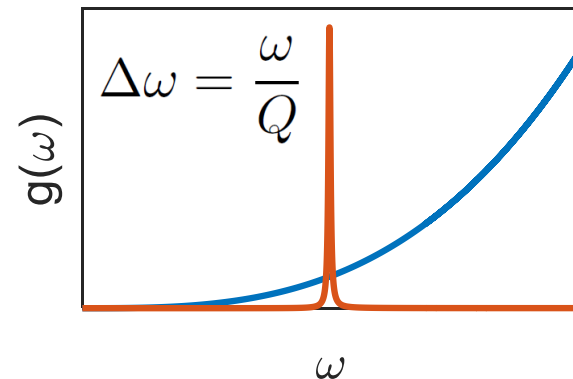
$$E_{\text{vac}} = \sqrt{\frac{\hbar\omega}{2\epsilon_0 V}}$$

single photon
mode volume

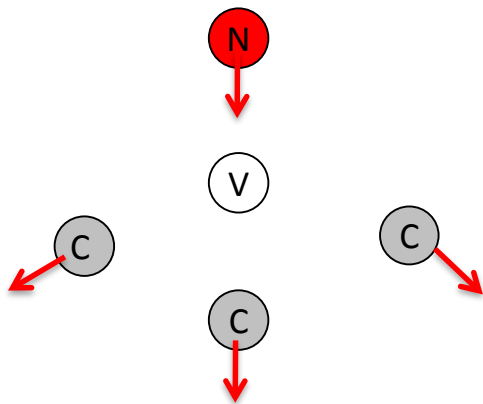
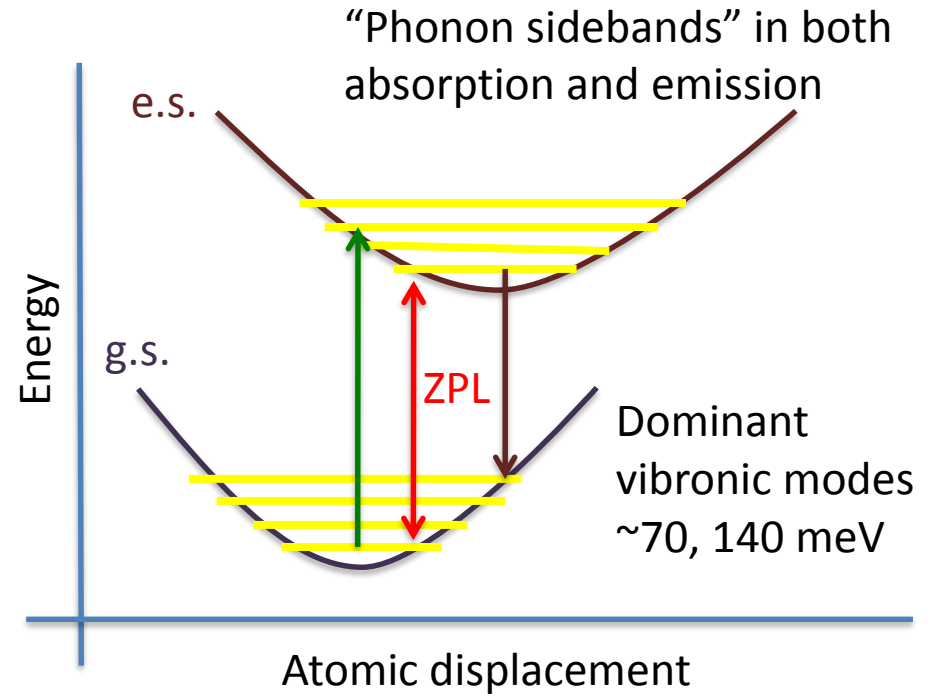
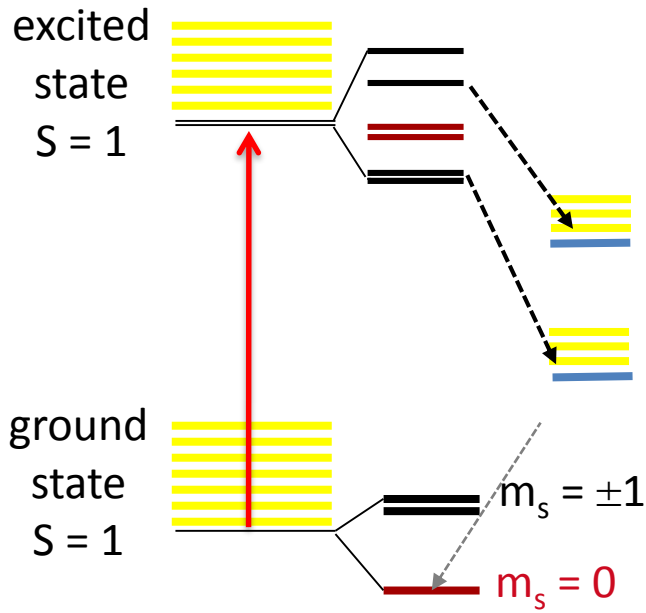
Photon density of states:

$$g_{\text{free}}(\omega) = \frac{\omega^2 V}{\pi^2 c^3}$$

$$g_{\text{cav}}(\omega) = \frac{2}{\pi \Delta\omega} \frac{\Delta\omega^2}{4(\omega - \omega_c)^2 + \Delta\omega^2}$$

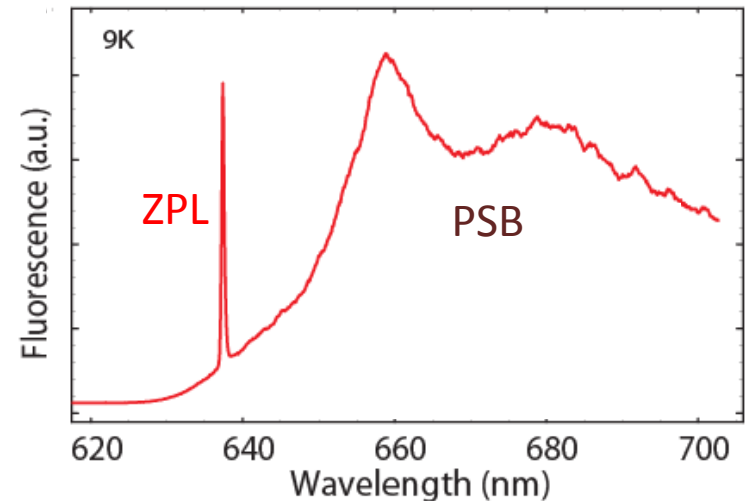


Vibronic structure of the NV center

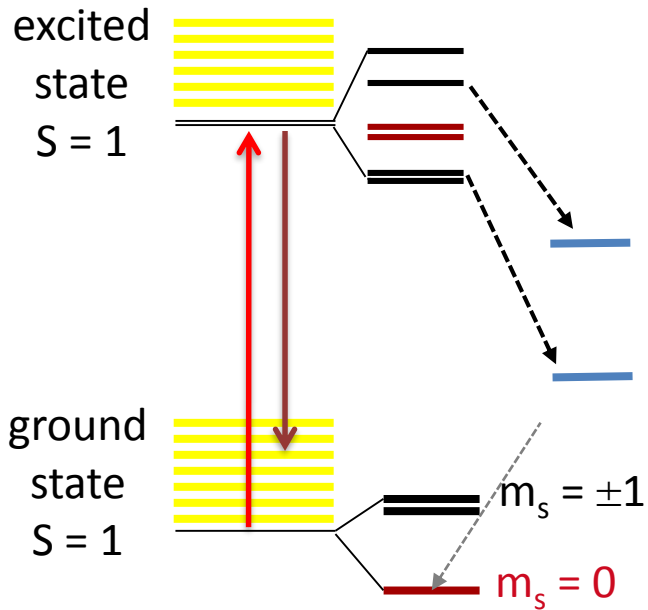


Different equilibrium positions in the ground and excited states (*ab initio* calculations)

Ma et al. 2010 PRB
 Gali et al. 2011 NJP
 Zhang et al. 2011 PRB
 Abtew et al. 2011 PRL
 Toyli et al. 2012 PRX



Strain effects at low temperatures

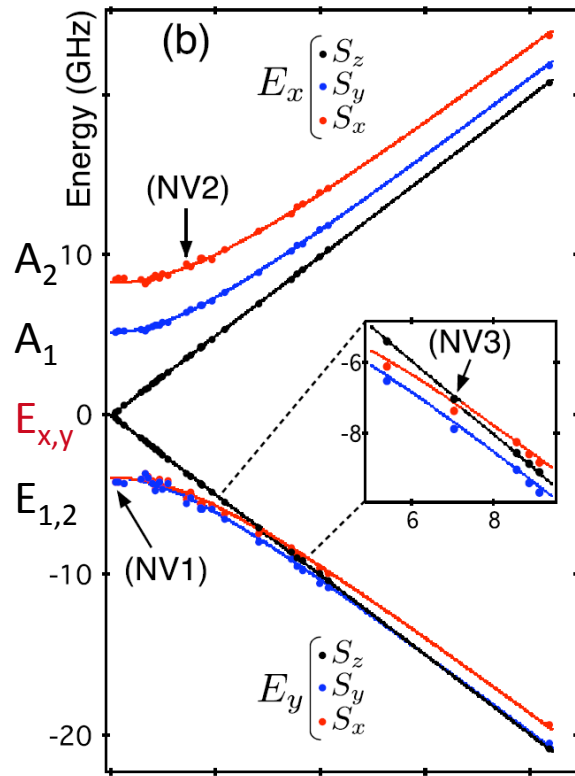


Zero strain:
 C_{3v} symmetry

Axial strain shifts all the energy levels together

Electric fields have the same effect as strain

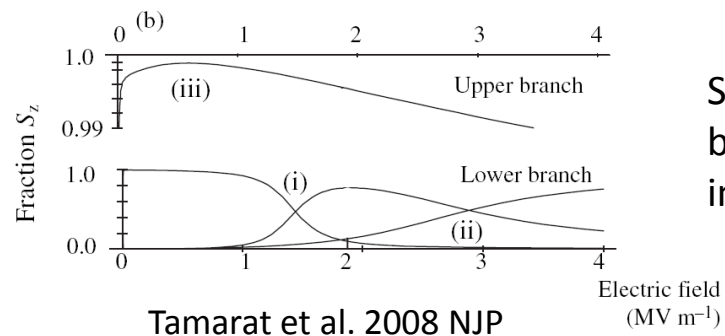
Batalov et al. 2009 PRL



High transverse strain:

Two $S=1$ orbital branches

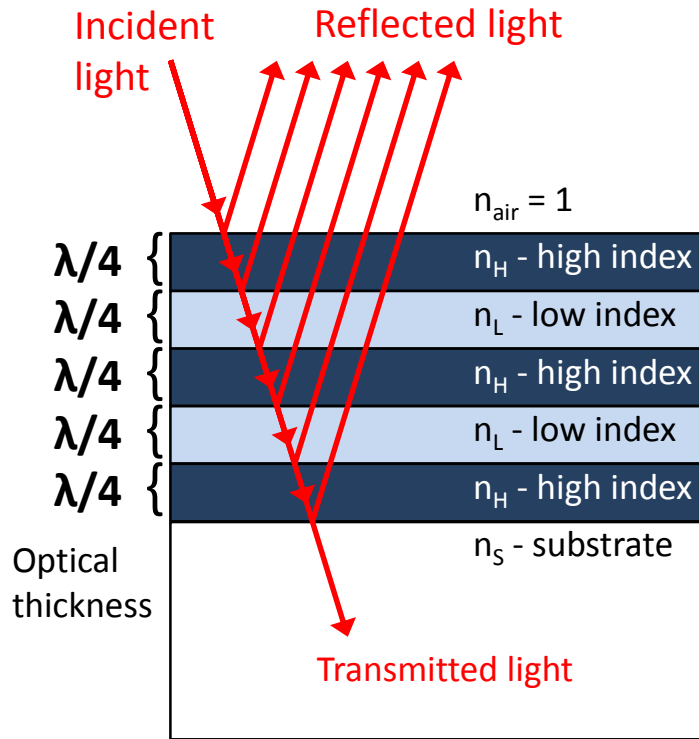
Linearly polarized emission, spin conserving in the limit of high strain



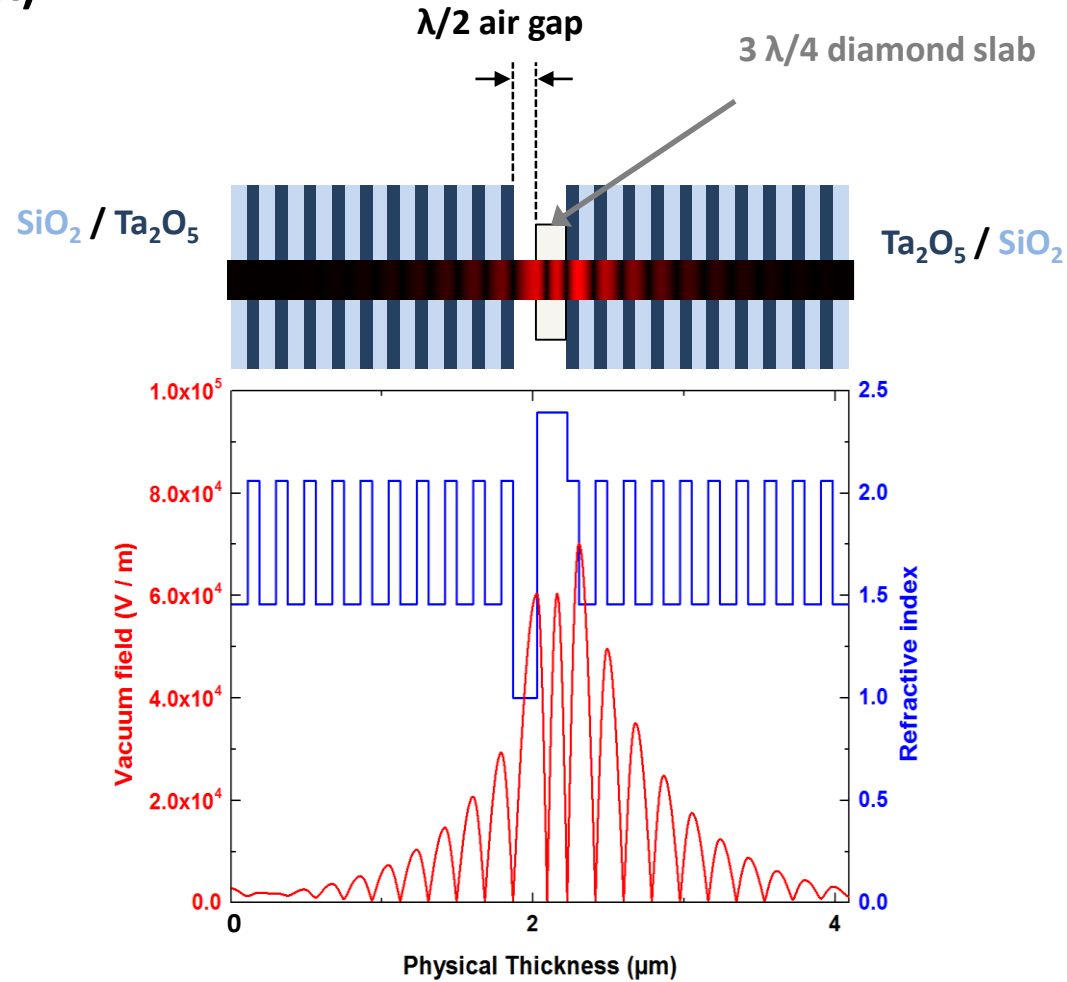
Tamarat et al. 2008 NJP

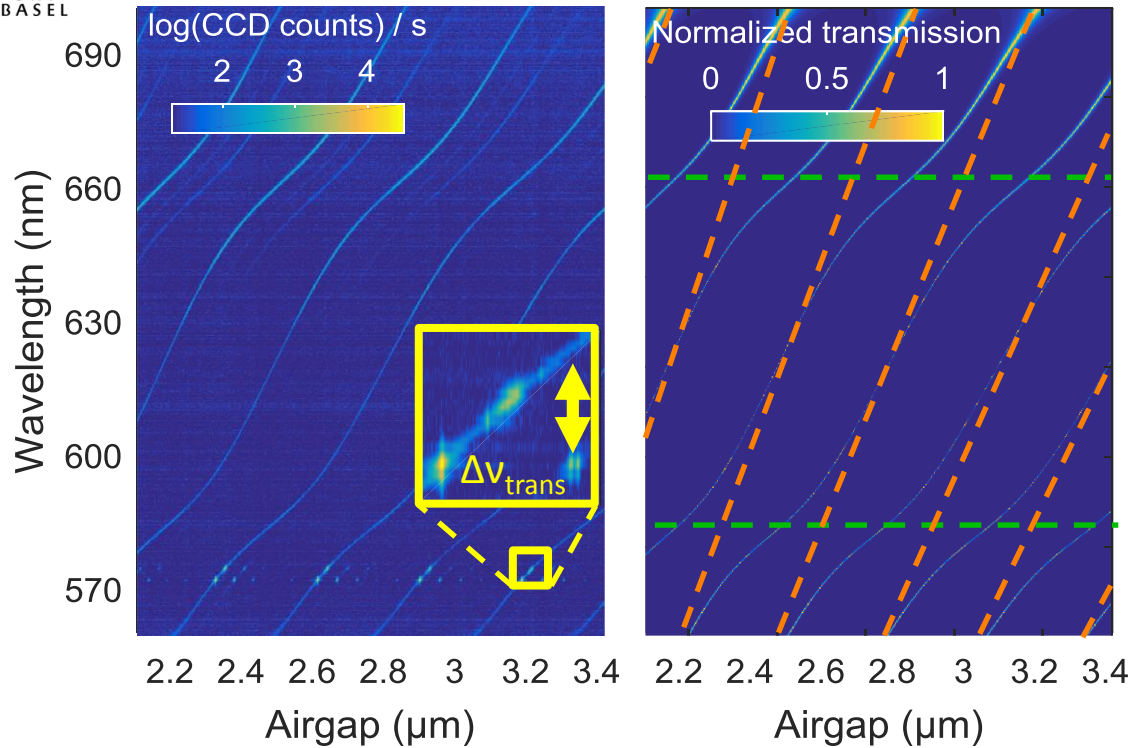
Significant mixing between spin states in lower branch

Distributed Bragg Reflector (DBR) R > 99.99% @ 637nm



SiO₂: n = 1.457
 Ta₂O₅: n = 2.060
 Diamond: n = 2.393





Mode structure:

- Two hybridized cavities:

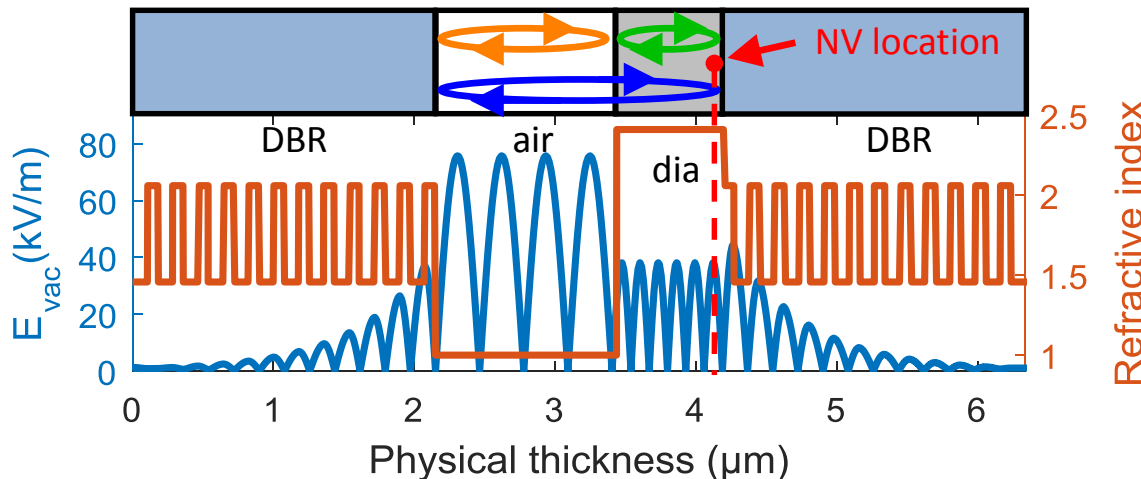
- air modes
- diamond modes

- From simulation:

- Diamond thickness
- Width airgap
- Vacuum field at NV

- Higher order mode spacing

- Radius of curved mirror



Experimental results:

$$\gamma_{\text{res}} = 158 \text{ MHz}, \gamma_{\text{offres}} = 88 \text{ MHz}, \Delta\gamma = 70 \text{ MHz}$$

Transition rate without top mirror:

$$\gamma_0 = 78.4 \text{ MHz}$$

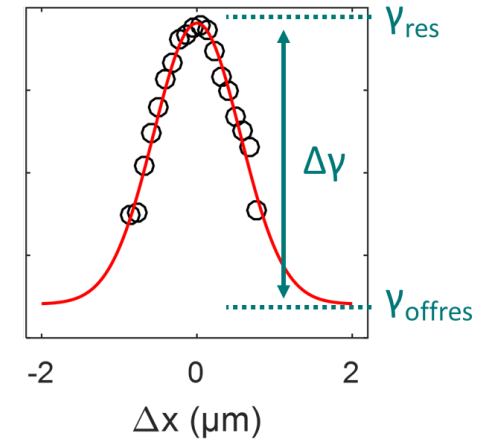
Fraction of ZPL emission:

$$\gamma_{\text{ZPL}} = \zeta \cdot \gamma_0, \text{ with } \zeta = 2\% \dots 5\%$$

$$\Delta\gamma = F_p \cdot \gamma_{\text{ZPL}} = F_p \cdot \zeta \cdot \gamma_0$$

$$\zeta = \Delta\gamma / (F_p \cdot \gamma_0) = 2.2\%$$

ZPL enhancement: ~ 40



waveguide effect

