

# *Flavour physics 1*

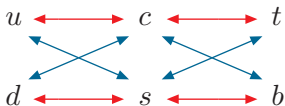
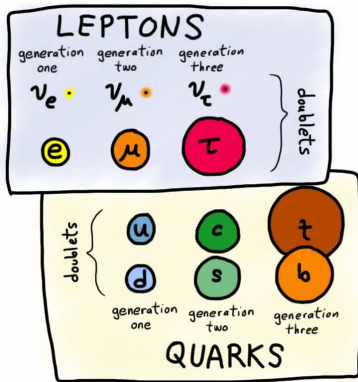
Lars Hofer

*IFAE Barcelona*

*Benasque, September 2015*

# What is flavour physics?

- ▶ Three generations of matter
- ▶ **flavour physics:** physics of transitions between fermions of different generations



flavour-changing  
charged/neutral currents

# Why is flavour physics interesting?

- ▶ **SM metrology:**

many of the free SM parameters related to flavour

- ▶ **SM flavour puzzle:**

hierarchy of fermion masses and mixing parameters not understood

- ▶ **CP violation:**

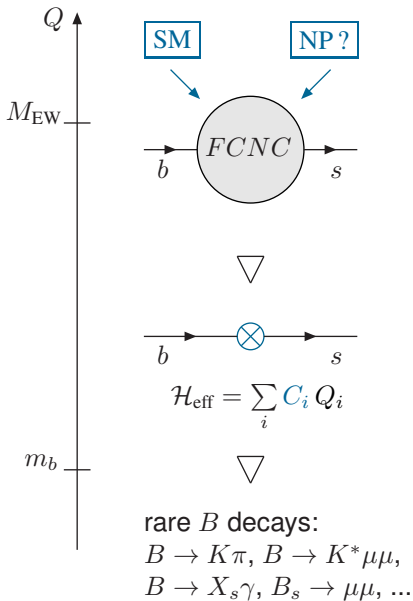
in the SM related to flavour violation  
needed to explain matter anti-matter asymmetry in the universe

- ▶ **indirect searches for new physics (NP):**

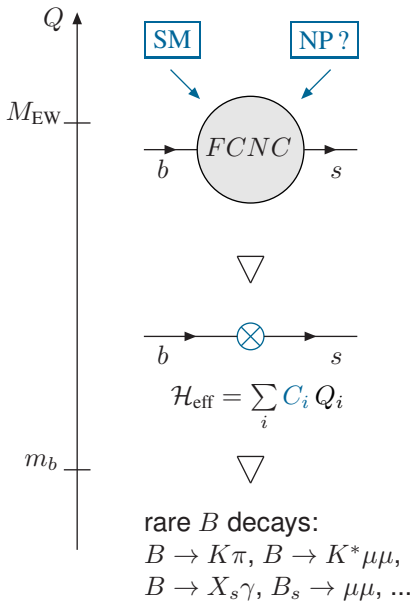
SM suppression renders flavour-changing neutral currents (FCNCs) sensitive to NP

	d	s	b
u	Large blue square	Small blue square	Very small red dot
c	Small blue square	Large blue square	Very small blue square
t	Very small red dot	Small blue square	Large blue square

# Exploring New Physics in FCNCs



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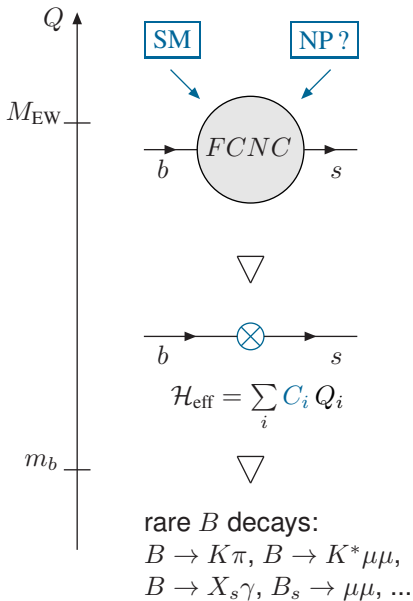


1  
Specific NP model  
e.g. MSSM,  $Z'$ , etc.

additional contributions to  
effective coefficients  $C_i$

predict impact on  
rare  $B$  decays

# Exploring New Physics in FCNCs



2

Which NP model  
can account for this pattern?



fit effective coefficients  
NP in certain  $C_i$



tensions in  
rare B decay data

# Outline

- 1 The spurion method in flavour physics
- 2 Effective theories in flavour physics
- 3 New physics in electroweak penguins?

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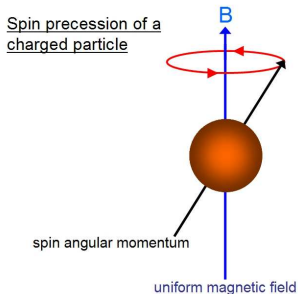


# $e^-$ in external $\vec{B}$ field

$$\mathcal{H} = \underbrace{\mathcal{H}_{\text{free } e^-}}_{SO(3)} + \underbrace{\mathcal{H}_{\vec{B}}}_{SO(2)}$$

external  $\vec{B}$  field induces **symmetry breaking**

$$SO(3) \rightarrow SO(2)$$



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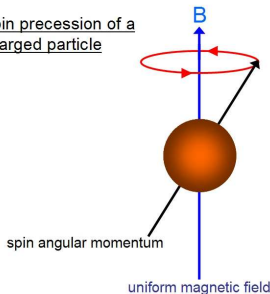
change point of view:

consider  $\vec{B}$  field as **internal part of system**

$\rightarrow \vec{B}$  transforms under  $SO(3)$

$\Rightarrow$  total system invariant under  $SO(3)$  symmetry

Spin precession of a charged particle



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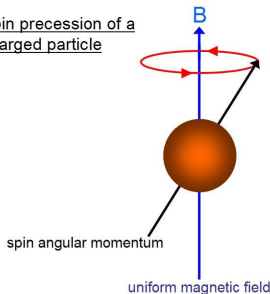
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$\vec{B}$  field  $\rightarrow$  **spurion:**

non-dynamical (=constant) field which has been promoted to an object transforming under a symmetry

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# Applications

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- ▶  **$SO(3)$  invariance**  $\Rightarrow$   $\mathcal{H}_{\vec{B}}$  built from  $\vec{S} \cdot \vec{B}$   
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- ▶  $\mathcal{H}_{\vec{B}}$  **linear** in  $\vec{S} \cdot \vec{B}$  because  $(\vec{B} \cdot \vec{S})^2 = \vec{B}^2/4 = \text{const.}$

$$\Rightarrow \boxed{\mathcal{H}_{\vec{B}} = \mu \vec{S} \cdot \vec{B}}$$

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▶ naively:  $3 \rightarrow \vec{B} = (B_x, B_y, B_z)$

▶ but: broken symmetry reduces number of physical parameters:

$$\# \text{ generators} \quad \begin{pmatrix} SO(3) \\ 3 \end{pmatrix} \longrightarrow \begin{pmatrix} SO(2) \\ 1 \end{pmatrix}$$

**broken generators** (rotations about  $x$ - and  $y$ -axis) can be used to rotate  $z$ -axis such that  $\vec{B} \parallel \hat{z}$

$\Rightarrow$  only one physical parameter  $\rightarrow \boxed{\vec{B} = (0, 0, |\vec{B}|)}$

# Gauge interactions

$$\mathcal{L}_{\text{gauge}}^q = \bar{Q}_L i \not{D} Q_L + \bar{d}_R i \not{D} d_R + \bar{u}_R i \not{D} u_R$$

▶  $D^\mu$  contains photons, gluons and weak gauge bosons

▶  $Q_L : SU(2)_L$  doublet,  $d_R, u_R : SU(2)_L$  singlet

▶ **three generations** in

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$\mathcal{L}_{\text{gauge}}^q$  invariant under rotations

$$Q_L \rightarrow R^Q Q_L, \quad d_R \rightarrow R^d d_R, \quad u_R \rightarrow R^u u_R$$

⇒ gauge interactions cannot distinguish generations

**Global flavour symmetry:**

$$[U(3)]^3 = U(3)_Q \times U(3)_u \times U(3)_d$$

# Yukawa interactions

$$\mathcal{L}_y^q = -\bar{Q}_L \Phi y^d d_R - \bar{Q}_L \Phi^c y^u u_R + h.c.$$

$\Phi$  : Higgs field ( $SU(2)_L$  doublet),  $\Phi^c = \sigma_2 \Phi^\dagger$   
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$\mathcal{L}_y^q$  invariant under common phase transformation

$$Q_L \rightarrow e^{i\phi_B} Q_L, \quad d_R \rightarrow e^{i\phi_B} d_R, \quad u_R \rightarrow e^{i\phi_B} u_R$$

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spurion method:

promote  $y^d, y^u$  to spurions transforming as

$$y^d \rightarrow R^Q y^d R^{d\dagger}, \quad y^u \rightarrow R^Q y^u R^{u\dagger}$$

$\Rightarrow [U(3)]^3$  flavour symmetry **restored**

# Choice of basis

$y^d, y^u$  : generic complex  $3 \times 3$  matrices

$\Rightarrow$  can be diagonalized by biunitary transformations

$$\hat{y}^d = S_1^\dagger y^d S_2, \quad \hat{y}^u = S_3^\dagger y^u S_4$$

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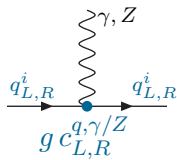
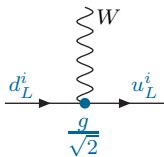
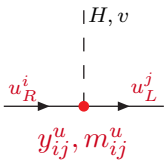
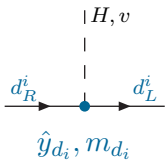
still: **weak eigenbasis** ( $\mathcal{L}_{\text{gauge}}^q$  unchanged)

$Q_L, d_R, u_R$  eigenstates of  $\mathcal{L}_{\text{gauge}}^q$

$y^u = V^\dagger \hat{y}_u \Rightarrow$  up-quark mass-terms non-diagonal

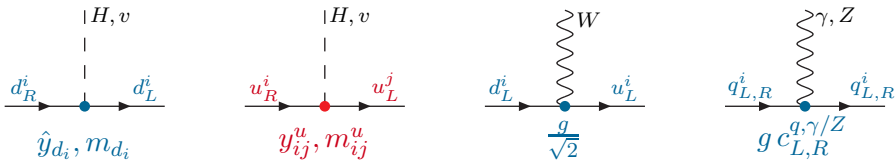
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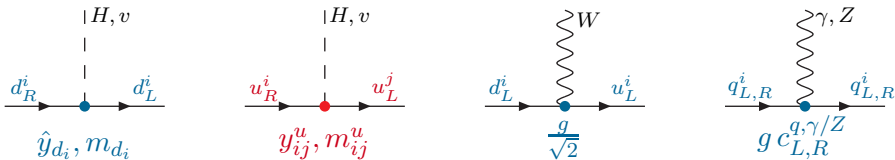
mass eigenbasis:

$$\bar{u}_L^i m_{ij}^u u_R^j = \bar{u}_L^i V_{ij}^\dagger m_{u_j} u_R^j = \bar{u}_L'^j m_{u_j} u_R^j \quad \text{with } m_{u_j} = y_{u_j} v$$

$$\text{perform rotation: } u_L^i \rightarrow u_L'^i = V_{ij} u_L^j$$

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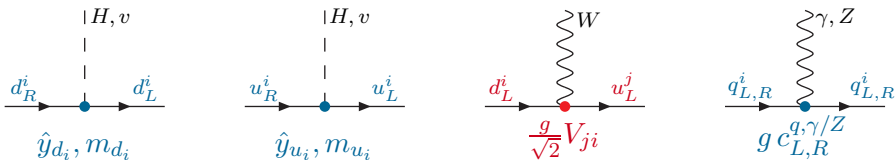
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# # physical parameters in $\mathcal{L}_y^q$ ?

Yukawa matrices

$$y^d, y^u$$

36 parameters

(18 real, 18 phases)

# # physical parameters in $\mathcal{L}_y^q$ ?

flavour symmetry

$$[U(3)]^3$$

27 generators

(9 real, 18 phases)

baryon symmetry

$$U(1)$$

1 generator

(1 phase)

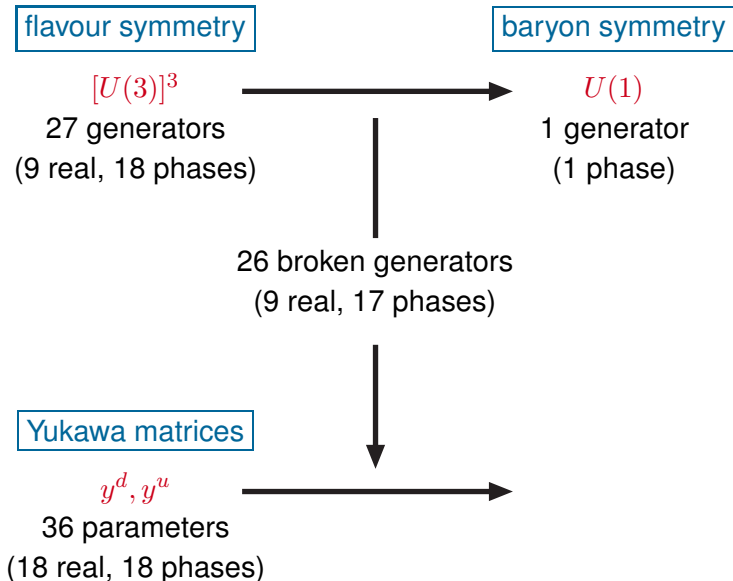
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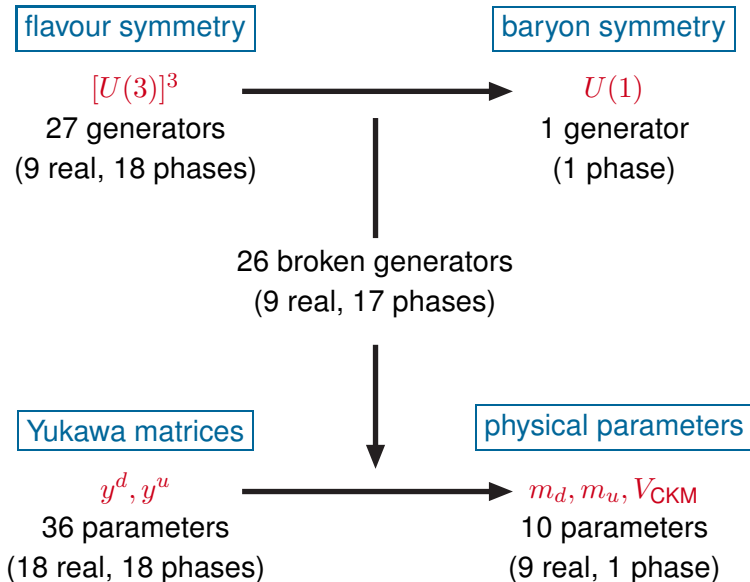
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# Yukawa-couplings and CKM matrix

## 9 real parameters

- ▶ 6 quark masses ( $\hat{=}$  diagonal Yukawa couplings  $\hat{y}_{d_i}, \hat{y}_{u_i}$ )
- ▶ 3 mixing angles in CKM matrix

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$$\hat{y}^d = \begin{pmatrix} y_d & 0 & 0 \\ 0 & y_s & 0 \\ 0 & 0 & y_b \end{pmatrix} \sim 0, \quad \hat{y}^u = \begin{pmatrix} y_u & 0 & 0 \\ 0 & y_c & 0 \\ 0 & 0 & y_t \end{pmatrix} \sim \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

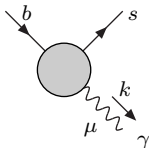
$$V = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \sim \mathcal{O}\left(\begin{pmatrix} 1 & \lambda & \lambda^3 \\ \lambda & 1 & \lambda^2 \\ \lambda^3 & \lambda^2 & 1 \end{pmatrix}\right), \quad \lambda \approx 0.22$$

$\rightarrow$  peculiar structure of measured quark masses and CKM matrix leads to **strong suppression of FCNCs** (flavour-changing neutral currents) in the SM

# FCNCs

example:

exclusive decay  $\bar{B} \rightarrow X_s \gamma$  (quark-level:  $b \rightarrow s \gamma$ )



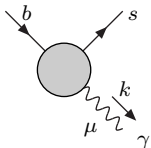
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$$\mathcal{M}_{b \rightarrow s \gamma}^\mu = \underbrace{A_L [\bar{s}_L \sigma^{\mu\nu} k_\nu b_R]}_{\mathcal{M}_L^\mu} + \underbrace{A_R [\bar{s}_R \sigma^{\mu\nu} k_\nu b_L]}_{\mathcal{M}_R^\mu}$$

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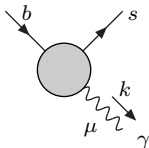
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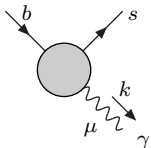
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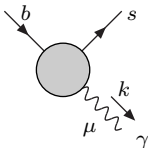
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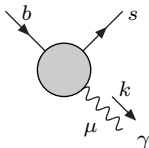
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$$\begin{aligned} \mathcal{M}_L^\mu &\propto \bar{Q}_L^2 \left( y^u y^{u\dagger} y^d \right)_{23} \sigma^{\mu\nu} k_\nu d_R^3 = \sum_i \bar{Q}_L^2 V_{i2}^* \hat{y}_i^u \hat{y}_i^u V_{i3} \hat{y}_3^d \sigma^{\mu\nu} k_\nu d_R^3 \\ &\approx y_b y_t^2 V_{ts}^* V_{tb} [\bar{s}_L \sigma^{\mu\nu} k_\nu b_R] \end{aligned}$$

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$[U(3)]^3$  transformations:

$$Q_L \rightarrow R^Q Q_L, \quad d_R \rightarrow R^d d_R, \quad u_R \rightarrow R^u u_R$$

$$y^d \rightarrow R^Q y^d R^{d\dagger}, \quad y^u \rightarrow R^Q y^u R^{u\dagger}$$

$[U(3)]^3$  invariance implies:  $(y_d = \hat{y}_d, y_u = V^\dagger \hat{y}^u)$

$$\mathcal{M}_L^\mu \propto \bar{Q}_L^2 \left( y^u y^{u\dagger} y^d \right)_{23} \sigma^{\mu\nu} k_\nu d_R^3 = \sum_i \bar{Q}_L^2 V_{i2}^* \hat{y}_i^u \hat{y}_i^u V_{i3} \hat{y}_3^d \sigma^{\mu\nu} k_\nu d_R^3$$

$$\approx y_b y_t^2 V_{ts}^* V_{tb} [\bar{s}_L \sigma^{\mu\nu} k_\nu b_R]$$

$$\mathcal{M}_R^\mu \propto \bar{d}_R^2 \left( y^{d\dagger} y^u y^{u\dagger} \right)_{23} \sigma^{\mu\nu} k_\nu Q_L^3 = \sum_i \bar{d}_R^2 \hat{y}_2^d V_{i2}^* \hat{y}_i^u \hat{y}_i^u V_{i3} \sigma^{\mu\nu} k_\nu d_R^3$$

$$\approx y_s y_t^2 V_{ts}^* V_{tb} [\bar{s}_R \sigma^{\mu\nu} k_\nu b_L]$$



# FCNCs

$$\mathcal{M}_{b \rightarrow s \gamma}^\mu = a_L (m_b m_t^2 V_{ts}^* V_{tb}) [\bar{s}_L \sigma^{\mu\nu} k_\nu b_R] + a_R (m_s m_t^2 V_{ts}^* V_{tb}) [\bar{s}_R \sigma^{\mu\nu} k_\nu b_L]$$

Suppression of FCNCs in SM:

- ▶ loop-induced
- ▶ small CKM elements:  $V_{ts}^* V_{tb} \sim \lambda^2$
- ▶ **GIM-suppression:**  
mass-independent terms cancel because of unitarity of CKM matrix
- ▶ here in addition: **helicity suppression**  $m_b/v$   
(suppression of right-handed current by  $m_s/m_b$ )

# Unitarity triangle

Unitarity of CKM matrix:

$$\sum_u V_{ud}V_{ud'}^* = 0 \quad \text{for } d \neq d', \quad \sum_d V_{ud}V_{u'd}^* = 0 \quad \text{for } u \neq u'$$

- ▶ 6 different relations: 3 for up-, 3 for down-quarks
- ▶ each relation defines **triangle in complex plane** (unitarity triangles)

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$$V_{ud}V_{us}^* + V_{cd}V_{cs}^* + V_{td}V_{ts}^* = 0$$

$\mathcal{O}(\lambda) \quad \mathcal{O}(\lambda) \quad \mathcal{O}(\lambda^5)$

→ distorted triangle!

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$$\begin{array}{ccc} V_{ud}V_{ub}^* & + & V_{cd}V_{cb}^* & + & V_{td}V_{tb}^* & = & 0 \\ \mathcal{O}(\lambda^3) & & \mathcal{O}(\lambda^3) & & \mathcal{O}(\lambda^3) & & \end{array}$$

→ **THE unitarity triangle!**

# Unitarity triangle

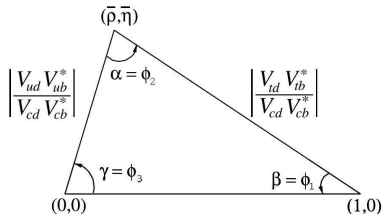
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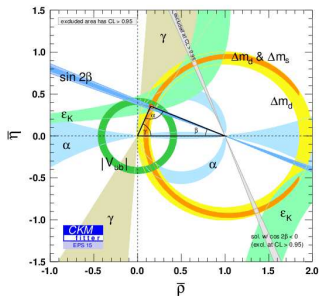
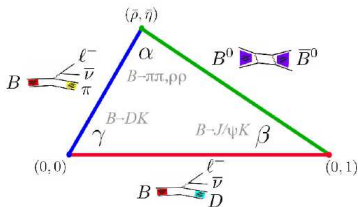
$$\frac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*} + 1 + \frac{V_{td}V_{tb}^*}{V_{cd}V_{cb}^*} = 0$$

→ **THE unitarity triangle!**

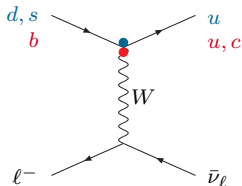


# CKM metrology

Overconstraining measurements:



- ▶  $|V_{ud}|, |V_{us}|, |V_{ub}|, |V_{cb}|$  at tree-level from semi-leptonic decays
- ▶  $|V_{td}|, |V_{ts}|$  only at loop-level via FCNCs  
 $\Delta m_d$  from  $B - \bar{B}$  mixing  $\rightarrow |V_{td}|$



# $B^0 - \bar{B}^0$ mixing

box diagrams mediate  $B^0 - \bar{B}^0$  transitions:

$$i\mathcal{M}_{12} = \text{[Box Diagram 1]} + \text{[Box Diagram 2]}$$

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time evolution:

$$i\frac{d}{dt} \begin{pmatrix} B^0(t) \\ \bar{B}^0(t) \end{pmatrix} = \mathcal{H} \begin{pmatrix} B^0(t) \\ \bar{B}^0(t) \end{pmatrix}, \quad \mathcal{H} = \mathcal{M} + i\Gamma$$

- $\mathcal{M}, \Gamma$  hermitian  $2 \times 2$  matrices:  
 $\mathcal{M}$  : transition within  $B^0 - \bar{B}^0$  system,

$\Gamma$  : decay of  $B^0, \bar{B}^0$



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$\mathcal{M}$ : transition within  $B^0 - \bar{B}^0$  system,  $\Gamma$ : decay of  $B^0, \bar{B}^0$

► empirically:  $\Gamma_{ij} \ll \mathcal{M}_{ij}$ ,

CPT-invariance:  $\mathcal{M}_{11} = \mathcal{M}_{22}$

$$\Rightarrow \mathcal{H} \approx \begin{pmatrix} \mathcal{M}_{11} & \mathcal{M}_{12} \\ \mathcal{M}_{12}^* & \mathcal{M}_{11} \end{pmatrix} \rightarrow \text{eigenvalues: } \mathcal{M}_{11} \pm |\mathcal{M}_{12}|$$

$\Rightarrow$  mass difference  $\Delta m_d = 2|\mathcal{M}_{12}|$

# $B^0 - \bar{B}^0$ mixing

$$i\mathcal{M}_{12} = \text{Diagram 1} + \text{Diagram 2}$$

$$\mathcal{M}_{12} = \sum_{ij} (V_{id}V_{ib}^*)(V_{jd}V_{jb}^*) f(x_i, x_j), \quad x_i = m_{u_i}^2/M_W^2$$

# $B^0 - \bar{B}^0$ mixing

$$i\mathcal{M}_{12} = \text{[Diagram 1]} + \text{[Diagram 2]}$$

Diagram 1: A box diagram with two external quark lines. The top line has an incoming  $d$  quark from the left and an outgoing  $b$  quark to the right. The bottom line has an incoming  $b$  quark from the left and an outgoing  $d$  quark to the right. Two vertical lines represent quark propagators, both labeled  $u, c, t$ . The left vertical line has an upward arrow, and the right vertical line has a downward arrow. Two horizontal wavy lines represent  $W$  boson exchanges. The top  $W$  boson connects the top vertex to the right vertex, and the bottom  $W$  boson connects the bottom vertex to the left vertex.

Diagram 2: A box diagram with two external quark lines. The top line has an incoming  $b$  quark from the left and an outgoing  $d$  quark to the right. The bottom line has an incoming  $d$  quark from the left and an outgoing  $b$  quark to the right. Two vertical wavy lines represent  $W$  boson exchanges. The left  $W$  boson connects the top vertex to the bottom vertex, and the right  $W$  boson connects the top vertex to the bottom vertex. Two horizontal lines represent quark propagators, both labeled  $u, c, t$ . The top horizontal line has a leftward arrow, and the bottom horizontal line has a rightward arrow.

$$\mathcal{M}_{12} = \sum_{ij} (V_{id}V_{ib}^*)(V_{jd}V_{jb}^*) f(x_i, x_j), \quad x_i = m_{u_i}^2/M_W^2$$

**GIM mechanism** ( $x_u \approx x_c \approx 0$ ):

$$\underbrace{V_{ud}V_{ub}^* g(x_u) + V_{cd}V_{cb}^* g(x_c) + V_{td}V_{tb}^* g(x_t)}_{\approx \underbrace{(V_{ud}V_{ub}^* + V_{cd}V_{cb}^*)}_{-V_{td}V_{tb}^*} g(0)}$$

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$$i\mathcal{M}_{12} = \text{[Diagram 1]} + \text{[Diagram 2]}$$

The first diagram shows a box with two horizontal lines. The top line has an arrow pointing left labeled  $b$  at the left end and an arrow pointing left labeled  $d$  at the right end. The bottom line has an arrow pointing right labeled  $d$  at the left end and an arrow pointing right labeled  $b$  at the right end. A wavy line labeled  $W$  connects the top and bottom lines in the middle. On the left side, a vertical arrow points up labeled  $u, c, t$ . On the right side, a vertical arrow points down labeled  $u, c, t$ .

The second diagram shows a box with two horizontal lines. The top line has an arrow pointing left labeled  $b$  at the left end and an arrow pointing left labeled  $d$  at the right end. The bottom line has an arrow pointing right labeled  $d$  at the left end and an arrow pointing right labeled  $b$  at the right end. Two wavy lines labeled  $W$  connect the top and bottom lines. The left wavy line is on the left side, and the right wavy line is on the right side. Between the two wavy lines, there are two horizontal arrows pointing towards each other, both labeled  $u, c, t$ .

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Diagram 1: A box diagram with two vertices. The top vertex has incoming lines  $b$  and  $d$  and outgoing lines  $u, c, t$  and  $u, c, t$ . The bottom vertex has incoming lines  $d$  and  $b$  and outgoing lines  $u, c, t$  and  $u, c, t$ . Two  $W$  bosons are exchanged between the vertices.

Diagram 2: A box diagram with two vertices. The top vertex has incoming lines  $b$  and  $d$  and outgoing lines  $u, c, t$  and  $u, c, t$ . The bottom vertex has incoming lines  $d$  and  $b$  and outgoing lines  $u, c, t$  and  $u, c, t$ . Two  $W$  bosons are exchanged between the vertices.

$$\mathcal{M}_{12} = \sum_{ij} (V_{id}V_{ib}^*)(V_{jd}V_{jb}^*) f(x_i, x_j), \quad x_i = m_{u_i}^2/M_W^2$$

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$$\underbrace{V_{ud}V_{ub}^* g(x_u) + V_{cd}V_{cb}^* g(x_c)}_{\approx (V_{ud}V_{ub}^* + V_{cd}V_{cb}^*)g(0)} + V_{td}V_{tb}^* g(x_t) \approx V_{td}V_{tb}^* [g(x_t) - g(0)]$$

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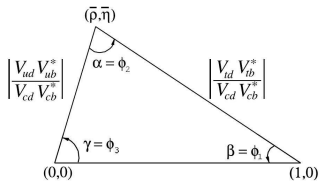
$$\Rightarrow \mathcal{M}_{12} \approx (V_{td}V_{tb}^*)^2 [f(x_t, x_t) - 2f(x_t, 0) + f(0, 0)]$$

$$V_{td}V_{tb}^* = V_{td} + \mathcal{O}(\lambda^4) \quad \Rightarrow \quad \Delta m_d = 2|\mathcal{M}_{12}| \text{ measures } |V_{td}|$$

# $\Delta m_d$ and $\Delta m_s$

with  $|V_{cd}|$  and  $|V_{cb}|$  from semi-leptonic decays:

$\Delta m_d$  measures side  $\left| \frac{V_{td}V_{tb}^*}{V_{cd}V_{cb}^*} \right| \propto \frac{\Delta m_d}{|V_{cd}||V_{cb}|}$  of unitarity triangle

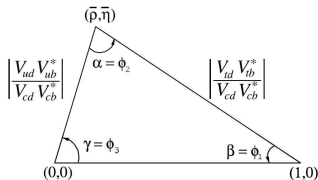


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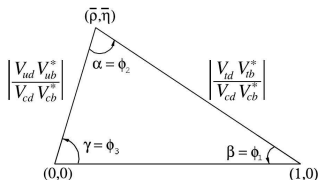
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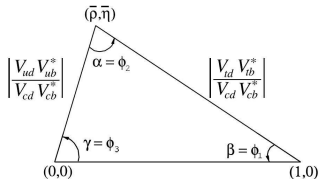
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- ▶ ratio of hadronic matrix elements can be calculated to higher precision than individual hadronic matrix elements



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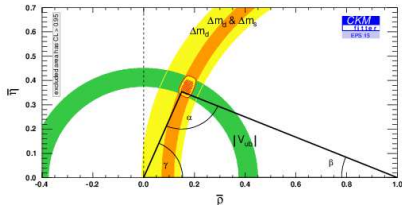
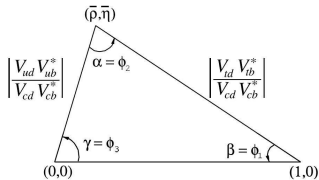
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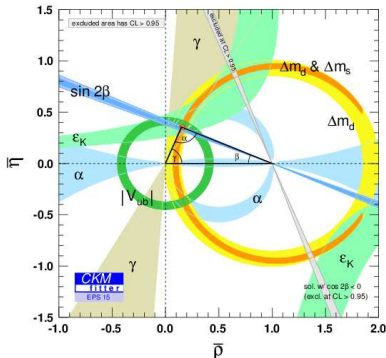
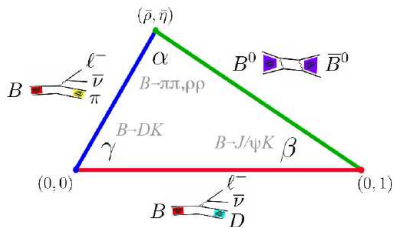
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# CKM metrology

Overconstraining measurements:



angles of unitarity triangle related to CP violation, e.g.

- ▶ mixing-induced CP asymmetry in  $B \rightarrow J/\psi K_s \rightarrow \beta$
- ▶ direct CP asymmetry in  $B \rightarrow DK \rightarrow \gamma$

# Flavour beyond the SM

generic extension of SM

→ new sources of flavour (=  $[U(3)]^3$ ) violation

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example: **MSSM** → soft SUSY-breaking terms

$$-\mathcal{L}_{\text{soft}}^{\text{SUSY}} \supset \tilde{Q}_L^* \tilde{m}_Q^2 \tilde{Q}_L + \tilde{u}_R^* \tilde{m}_u^2 \tilde{u}_R + \tilde{d}_R^* \tilde{m}_d^2 \tilde{d}_R + \\ \tilde{u}_R^* H_u a^u \tilde{Q}_L + \tilde{d}_R^* H_d a^d \tilde{Q}_L + h.c.$$

$\tilde{m}_Q^2, \tilde{m}_u^2, \tilde{m}_d^2$  :  $3 \times 3$  hermitian mass matrices

$a^u, a^d$  :  $3 \times 3$  trilinear coupling matrices

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need **further spurions** to restore flavour symmetry:

$$\tilde{m}_Q^2 \rightarrow R^Q \tilde{m}_Q^2 R^{Q\dagger}, \quad \tilde{m}_u^2 \rightarrow R^u \tilde{m}_u^2 R^{u\dagger}, \quad \tilde{m}_d^2 \rightarrow R^d \tilde{m}_d^2 R^{d\dagger}$$

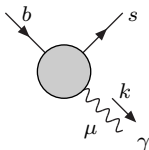
$$a^u \rightarrow R^u a^u R^{Q\dagger}, \quad a^d \rightarrow R^d a^d R^{Q\dagger}$$

⇒ new contributions to FCNCs

# FCNCs beyond the SM

example:

exclusive decay  $\bar{B} \rightarrow X_s \gamma$  (quark-level:  $b \rightarrow s \gamma$ )



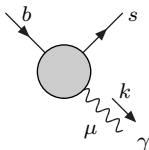
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$$\mathcal{M}_R^\mu \propto \bar{d}_R^2 a_{23}^d \sigma^{\mu\nu} k_\nu Q_L^3 = a_{23}^d \bar{s}_R \sigma^{\mu\nu} k_\nu b_L$$

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most suppression effects of FCNCs absent!

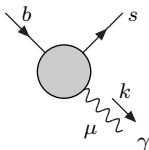
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- ⇒ **flavour problem** of new physics



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MFV hypothesis: (Minimal Flavour Violation)

$y^u, y^d$  are the **only spurions** of the  $[U(3)]^3$  flavour symmetry

flavour problem of new physics reduces to SM flavour problem

# Minimal Flavour Violation

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parametrisation of flavoured NP parameters in terms of  $y^d, y^u$

e.g. SUSY-breaking terms:

$$\tilde{m}_Q^2 = m_0^2 [a_1 + b_1 y^u y^{u\dagger} + b_2 y^d y^{d\dagger} + (b_3 y^d y^{d\dagger} y^u y^{u\dagger} + h.c.) + \dots]$$

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All possible Yukawa structures form **basis of  $3 \times 3$  matrices**

but: **nearly aligned**  $\Rightarrow$  generic flavour structure needs large  $a_i, b_i$

$\Rightarrow$  require **naturality** for  $a_i, b_i$

# Minimal Flavour Violation

MFV hypothesis: (Minimal Flavour Violation)

$y^u, y^d$  are the **only spurions** of the  $[U(3)]^3$  flavour symmetry

parametrisation of flavoured NP parameters in terms of  $y^d, y^u$

e.g. SUSY-breaking terms:

$$\begin{aligned}\tilde{m}_Q^2 &= m_0^2 [a_1 + b_1 y^u y^{u\dagger} + b_2 y^d y^{d\dagger} + (b_3 y^d y^{d\dagger} y^u y^{u\dagger} + h.c.) + \dots] \\ a^d &= A_0 y^d [a_2 + b_4 y^u y^{u\dagger} + \dots]\end{aligned}$$

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but: **nearly aligned**  $\Rightarrow$  generic flavour structure needs large  $a_i, b_i$   
 $\Rightarrow$  require **naturality** for  $a_i, b_i$

“more minimal” definition  $b_i \equiv 0$ ?

**not RGE invariant:** if imposed at one scale,  $b_i \neq 0$  induced at others

**CMSSM** (constrained MSSM):  $b_i \equiv 0$  at Planck scale

# Radiative flavour violation

- ▶ origin of NP flavour problem:
  - approximate flavour symmetry of Yukawa sector
  - exact symmetry limit: only top quark massive and  $V = 1$

# Radiative flavour violation

- ▶ origin of NP flavour problem:
  - approximate flavour symmetry of Yukawa sector
  - exact symmetry limit: only top quark massive and  $V = 1$
- ▶ assume exact flavour symmetry in Yukawa sector  
use flavour structure of NP model to generate small quark masses and  $V \neq 1$  radiatively

Radiative Flavour Violation (RFV) [Weinberg'72]

from soft-susy breaking terms

[Buchmüller,Wyler'83, Banks'88, Borzumati,Farrar,Polonsky'98'99,

Ferrandis,Haba'04]

today: strong constraints from FCNCs

but: RFV from trilinear  $A$ -terms still viable

[Crivellin,LH,Nierste,Scherer'11]

# MFV vs. RFV

gauge sector

Yukawa sector

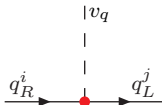
SUSY breaking

MFV

$$U(3)^3 \longrightarrow U(1)_B$$

$$Y^{q(0)} = \begin{pmatrix} y_{11}^q & y_{12}^q & y_{13}^q \\ y_{21}^q & y_{22}^q & y_{23}^q \\ y_{31}^q & y_{32}^q & y_{33}^q \end{pmatrix}$$

$$m_{u_i}, m_{d_i}, V_{ij}$$



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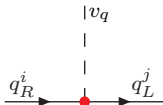
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$$\tilde{m}_q^2 \propto 1, Y^{q(0)\dagger} Y^{q(0)}, \dots$$

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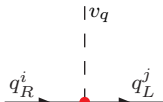
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RFV

$$U(3)^3 \longrightarrow U(2)^3$$

$$Y^{q(0)} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & y^q \end{pmatrix}$$

$$m_t, m_b, V = 1$$



# MFV vs. RFV

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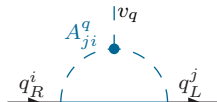
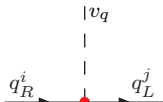
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$m_t, m_b, V = 1$        $m_u, m_d, m_s, m_c, V_{ij} (i \neq j)$



# Radiative Flavour Violation

$U(2)^3$  symmetry of Yukawa sector

- ▶ **obeyed** by bilinear squark mass terms  $\widetilde{M}_{Q_L, u_R, d_R}^2$
- ▶ **broken** by trilinear  $A^{u,d}$ -terms

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This scenario of RFV

- ▶ links the **breaking of flavour-symmetries** to SUSY-breaking
- ▶ explains overall smallness of quark-masses  $m_u, m_d, m_s, m_c$  and CKM-elements  $V_{ti}, V_{ib}$  ( $i = 1, 2$ ) by **loop suppression**
- ▶ **softens the SUSY flavour problem** by linking most of the flavour off-diagonal SUSY-breaking terms to measured CKM elements
- ▶ allows to split the third squark generation from the first two in order have
  - ▶ **light stops** as favoured by the hierarchy problem
  - ▶ **heavy squarks of first two generations** avoiding bounds from direct searches

# A-terms

perform  $U(2)$ -rotations on left- and righthanded superfields such that

$$A^{q=u,d} = \begin{pmatrix} A_{11}^q & 0 & A_{13}^q \\ 0 & A_{22}^q & A_{23}^q \\ A_{31}^q & A_{32}^q & A_{33}^q \end{pmatrix}, \quad V^{(0)} = \begin{pmatrix} \cos \theta_C & \sin \theta_C & 0 \\ -\sin \theta_C & \cos \theta_C & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

$\theta_C$  = exp. measured Cabbibo-angle

- ▶ minimal flavour violation with respect to the first two generations
- ▶ avoid tight constraints from Kaon physics

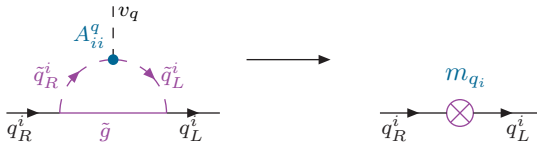
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radiative mass generation ( $q = u, d, i = 1, 2$ ):



$$m_{q_i} = a_q A_{ii}^q v_q$$

smallness of light quark masses  $\longleftrightarrow a_q \sim \frac{\alpha_s}{4\pi}$

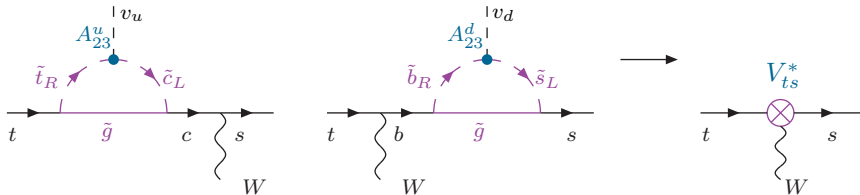
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radiative CKM generation (example:  $V_{ts}$ ):



$$V_{ts}^* = b_u A_{23}^u \frac{v_u}{m_t} - b_d A_{23}^d \frac{v_d}{m_b}$$

smallness of CKM elements  $V_{ti}, V_{ib}$  ( $i = 1, 2$ )  $\longleftrightarrow$   $b_q \sim \frac{\alpha_s}{4\pi}$

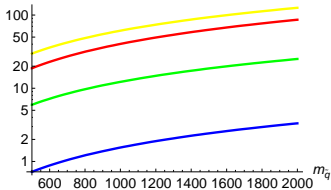
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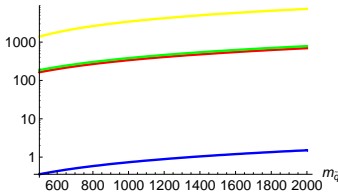
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$\cos(\beta)|A^q|$  in GeV



$\sin(\beta)|A^q|$  in GeV



loop-functions in radiative mass and CKM generation **do not decouple**  
for  $M_{\text{SUSY}} \rightarrow \infty$

$\Rightarrow$  RFV works also for **high SUSY mass scale**



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perform  $U(2)$ -rotations on left- and righthanded superfields such that

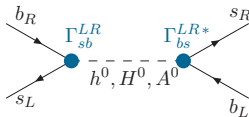
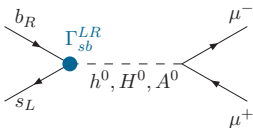
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contribution of  $A_{31}^q, A_{32}^q$  to CKM elements **helicity-suppressed**  
(small quark mass ratios  $m_s/m_b, m_c/m_t, \dots$ )

- ▶  $A_{31}^q, A_{32}^q$  **not constrained** from measured CKM elements
- ▶  $A_{31}^q, A_{32}^q$  act as sources of **non-minimal flavour violation**  
⇒ different phenomenology than MFV scenarios

# Higgs (double) penguins



## ► MFV:

$$\Gamma_{sb}^{LR} \propto y_b y_t^2 V_{ts}^* V_{tb}, \quad \Gamma_{bs}^{LR*} \propto y_s y_t^2 V_{ts}^* V_{tb}$$

⇒ Experimental bounds on  $B_s \rightarrow \mu^+ \mu^-$  render Higgs double penguin effects in  $B_s - \bar{B}_s$  mixing negligible because of

$$\Gamma_{bs}^{LR*} / \Gamma_{sb}^{LR} \propto m_s / m_b$$

## ► RFV:

$$\Gamma_{sb}^{LR} \propto A_{23}^d \propto V_{ts}^*, \quad \Gamma_{bs}^{LR*} \propto A_{32}^{d*}$$

⇒  $\Gamma_{bs}^{LR*}$  not suppressed with respect to  $\Gamma_{sb}^{LR}$