

# Physics of ultrarelativistic heavy-ion collisions

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IPNO, Paris-Sud U.

**Taller de Altas Energías 2015, Benasque, Sep 20 - Oct 02, 2015**  
1st Lecture: September 28, 2015

## USEFUL REFERENCES:

- *Ultrarelativistic Heavy-Ion Collisions* by Ramona Vogt (Elsevier)
- *Introduction to Relativistic Heavy Ion Collisions* by Lazlo Csernai (pdf freely available online)  
[www.csernai.no/Csernai-textbook.pdf](http://www.csernai.no/Csernai-textbook.pdf)
- *Relativistic heavy-ion physics: three lectures* by L. McLerran  
[cds.cern.ch/record/1009274/files/p75.pdf](http://cds.cern.ch/record/1009274/files/p75.pdf)
- *Global Properties of Nucleus-Nucleus Collisions* by M. Kliemant *et al.*  
(Lect.Notes Phys. 785 (2010) 23-103) <http://arxiv.org/pdf/0809.2482.pdf>

## USEFUL SLIDES FROM TALKS/LECTURES:

(in particular for me to prepare these lectures)

- David d'Enterria (CERN): webpage [dde.web.cern.ch/dde](http://dde.web.cern.ch/dde)
- Anton Andronic (GSI):  
webpage <http://web-docs.gsi.de/~andronic/physics/act.html>
- K. Reygers / J. Stachel (Heidelberg) webpage:  
[http://www.physi.uni-heidelberg.de/~reygers/lectures/2011/qgp/qgp\\_lecture\\_ss2011.html](http://www.physi.uni-heidelberg.de/~reygers/lectures/2011/qgp/qgp_lecture_ss2011.html)
- Elena Ferreiro (USC)
- ...

# Part I

## (Ultra)(Relativistic)HIC:what for ?

## Preface: why study (ultra relativistic) heavy-ion collisions

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- **HEAVY-ION PHYSICS** addresses this question in the regime of the **highest temperature** and **densities** accessible in the laboratories
- **HOW ?** By colliding nucleus (or ions) and looking for specific signals

**Example**: looking for the quark-gluon plasma, *i.e.* a new state of matter, **using specific probes**

# Part II

## Confinement and Deconfinement in QCD



# Confinement

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- The **gauge bosons self interact**

(Yang-Mills theory)

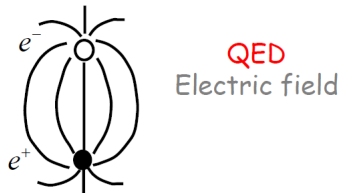
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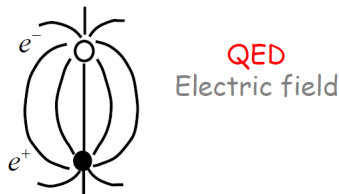
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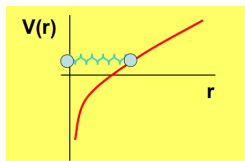
Energy stored per unit length in field  $\sim$  constant  $V(r) \propto r$

- If  $V(r) > 2m_\pi$ , 2  $\pi$ 's pop up from the vacuum and the  $q\bar{q}$

# Deconfining the quark and gluons

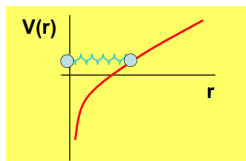
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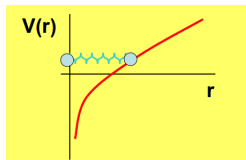


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- Is there a regime where the quarks and the gluons can be free ?

# The phase diagram of strongly interacting matter

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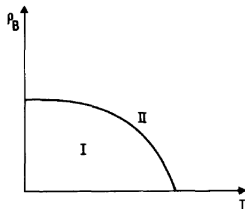
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*We suggest [...] the existence of a different phase of the vacuum in which quarks are not confined.”*



N. Cabibbo, G. Parisi, PLB 59 (1975) 67

Fig. 1. Schematic phase diagram of hadronic matter.  $\rho_B$  is the density of baryonic number. Quarks are confined in phase I and unconfined in phase II.

# When the asymptotic freedom leads to deconfinement

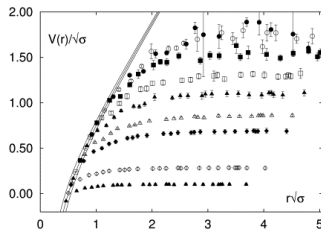
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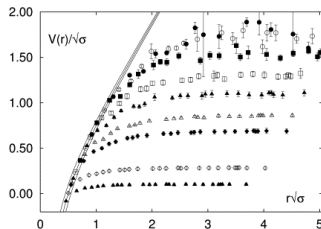
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F. Karsch *et al.*, PLB 605 (2001) 579

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- When  $T \nearrow$ , the long range potential decreases and becomes flat

$T/T_c = 0.58, 0.66, 0.74, 0.84, 0.9, 0.94, 0.97, 1.06$  et  $1.15$  (top to bottom)



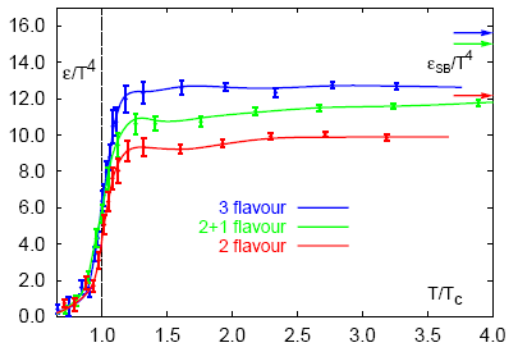
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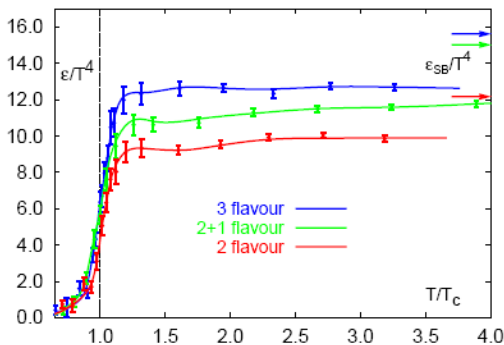
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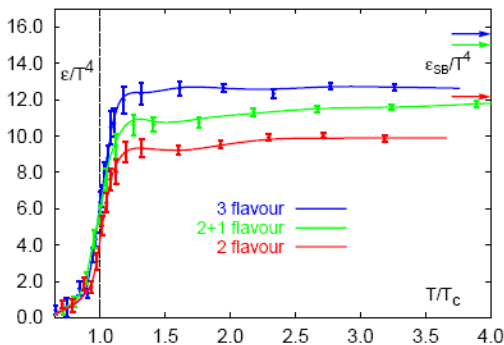
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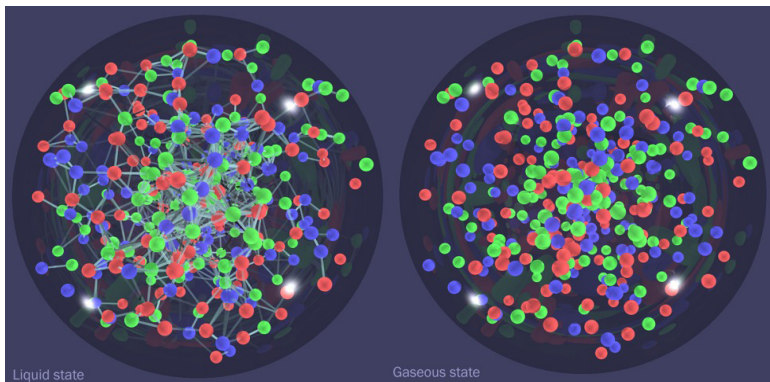
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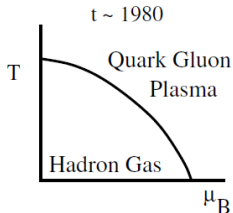
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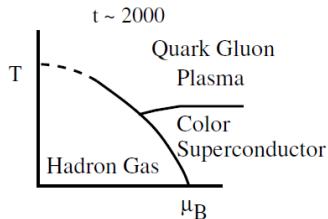
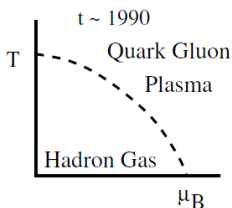
# Rapidly evolving field

Phase diagram as function of (scientific) time

## The Evolving QCD Phase Transition



Critical Temperature 150 - 200 MeV ( $\mu_B = 0$ )  
 Critical Density 1/2-2 Baryons/fm<sup>3</sup> ( $T = 0$ )



[Reminder: Quarks: 1964 ; Scaling: 1967 ; Asymptotic Freedom: 1973; Charm quark: 1974; ...]

## Part III

# Heavy-Ion Collisions: the quest for a phase transition



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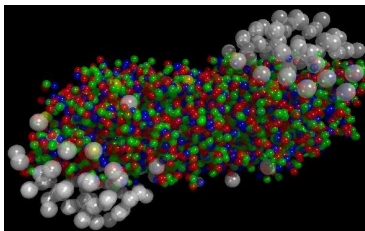
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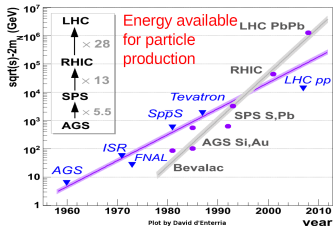
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- Duration: about  $10 \text{ fm/c}$  (*i.e.*  $3 \cdot 10^{-23}\text{s}$ )

# Energy density and center-of-mass energy



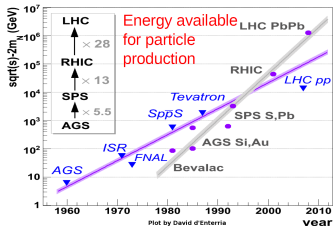
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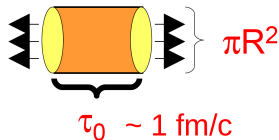


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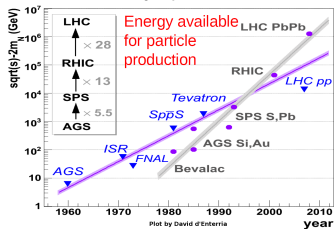


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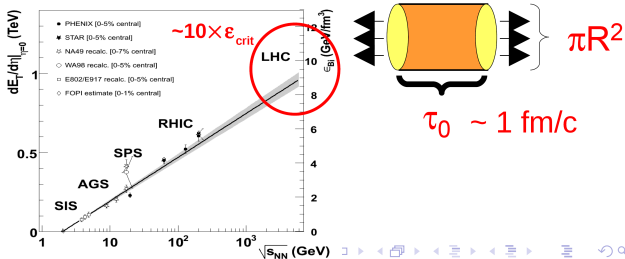


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## FIXED-TARGET EXPERIMENTS :

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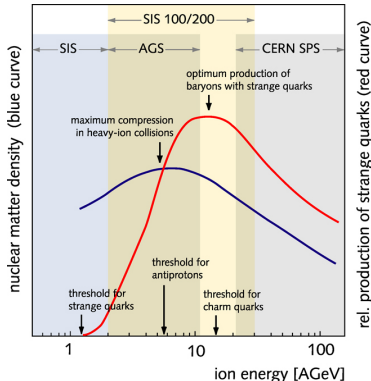
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<http://www.gsi.de>

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**REMARK:** The LHC in the fixed-target mode :  $\sqrt{s_{NN}} = 72 \text{ GeV}$   
 $\rightarrow$  energy comparable to RHIC, with extremely high rate



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[can't do anything against momentum conservation]
- Cons for colliders: collision rate ( 8000 per sec at the LHC vs.  $10^7$  per sec at FAIR)  
[ can't beat a target density with a (collimated) beam]

**REMARK:** The LHC in the fixed-target mode :  $\sqrt{s_{NN}} = 72 \text{ GeV}$   
 $\rightarrow$  energy comparable to RHIC, with extremely high rate

**Strong motivation for A Fixed Target Experiment @ LHC**  
**(AFTER@LHC)**

# Part IV

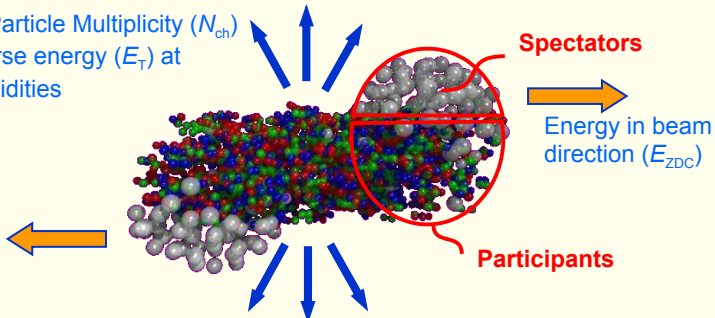
## Tuning an Heavy-Ion Collision: the centrality

# Smooth phase transition $\leftrightarrow$ complications

- We must study properties of the medium in **detail**  
without a smoking-gun phase-transition signature
- Most of observables will show  
**a smooth dependence on energy**
- Apart from changing the beam energy and colliding species,  
one can select (bias) the **geometry of the collisions**
- Preferred way of varying the energy density  
( $\leftrightarrow$  centrality, impact parameter  $b$ )

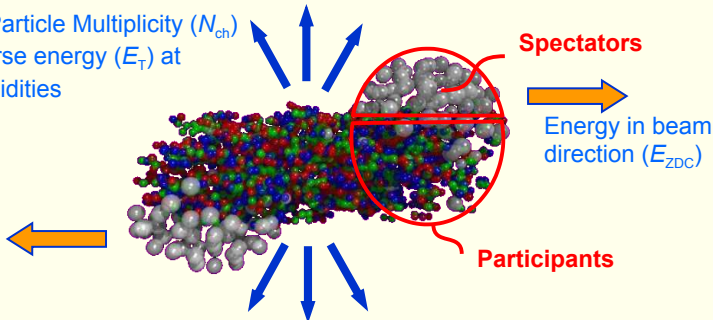
## Two important definitions: $N_{part}$ and $N_{coll}$

Charged Particle Multiplicity ( $N_{ch}$ )  
or transverse energy ( $E_T$ ) at  
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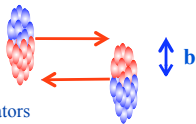


- Centrality can be described via
  - ◆  $N_{coll}$ : number of inelastic nucleon-nucleon collisions
  - ◆  $N_{part}$ : number of nucleons which underwent at least one inelastic nucleon-nucleon collisions
- This simplifies the comparison between theory and experiment and between different experiments
- Typically not directly measured but determined from Glauber calculations

Slide borrowed from K. Reygers

# Practical example with ALICE (2011 PbPb data)

semi-central collision

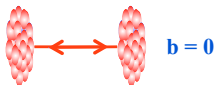


Spectators

Participants

$b$  impact parameter

central collision



$$N_{\text{part}} = 2 \quad N_{\text{coll}} = 1$$



$$N_{\text{part}} = 5 \quad N_{\text{coll}} = 6$$

$$\text{Pb-Pb cent.} \quad N_{\text{part}} = 360 \quad N_{\text{coll}} = 1500$$

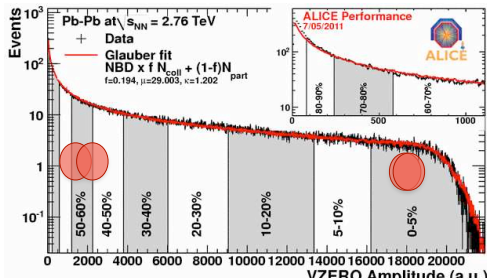
$$\text{p-Pb cent.} \quad N_{\text{part}} = 16 \quad N_{\text{coll}} = 15$$

→ Glauber model used to determine the geometry of the collision

## Centrality determination

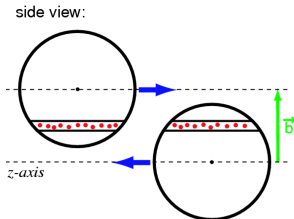
Multiplicity measurements with forward or central detectors

Relate the measured multiplicity in A-A collisions to  $N_{\text{part}}$  and  $N_{\text{coll}}$

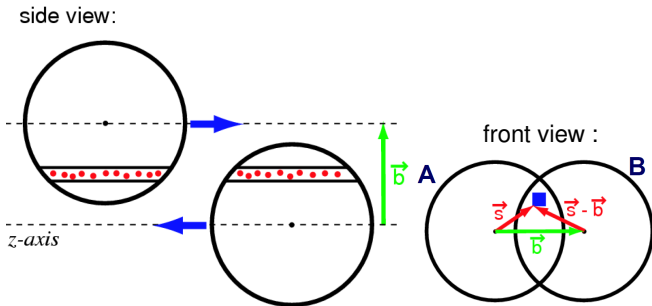


# Glauber model for $pA$ and $AA$ collisions

- Input:
  - **density profile** of the nucleus: Woods-Saxon
  - **inelastic nucleon-nucleon cross section** (which is a function of the collisions energy:  $\sigma_{NN}^{inel.}(\sqrt{s})$ )
- Nucleons travel on **straight trajectories** along the beam axis (after a nucleon-nucleon collisions)
- Nucleon-nucleon cross section is **independent of the number of collisions** a nucleon underwent before [neglect the possible decrease of the inelastic nucleon-nucleon cross section for the consecutive scattering]



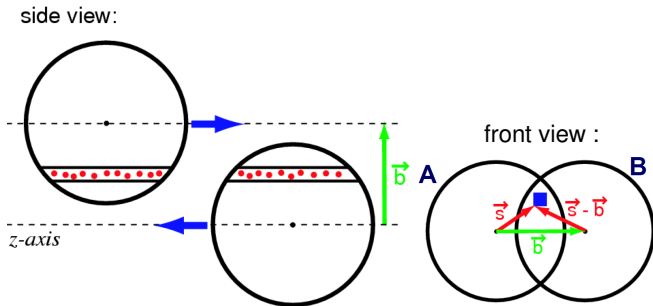
# Number of Nucleon-Nucleon Collisions $N_{coll}$



- Nuclear thickness : integral of the density on  $z$  as function of the distance  $\vec{s}$  from the nucleus center:  $\int \rho(\vec{s}, z) dz = T_A(\vec{s})$

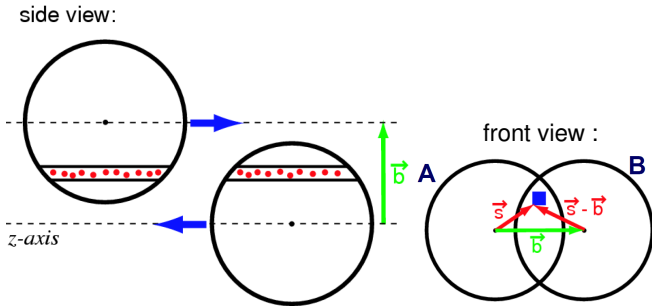


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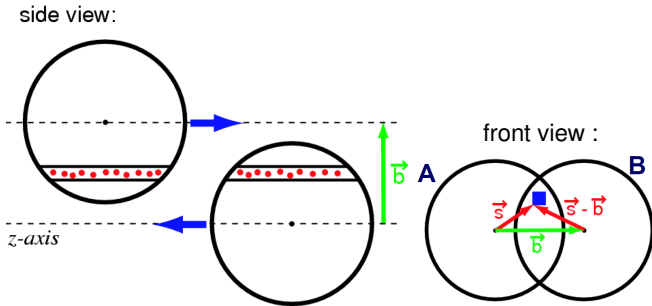
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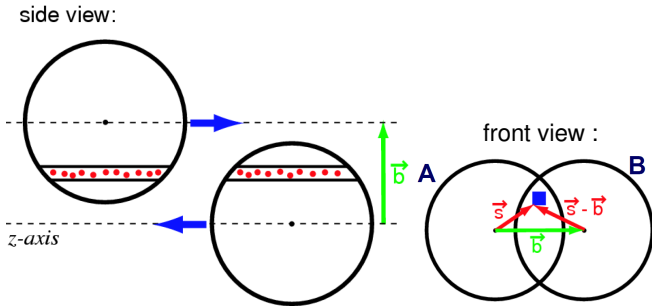
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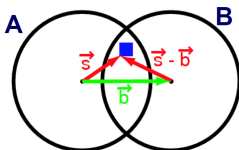
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- Average number of collisions: overlap times the cross section

$$\langle N_{coll}(b) \rangle = T_{AB}(b) \times \sigma_{NN}^{inel.}$$

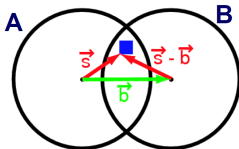
# Number of participants $N_{part}$



- Proba that a given nucleon from A scatters with another from B:

$$\mathcal{P} = \frac{T_B(\vec{s})}{B} \times \sigma_{NN}^{inel.}$$

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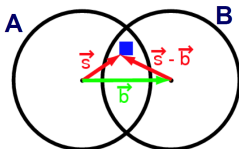


- Proba that a given nucleon from  $A$  scatters with another from  $B$ :

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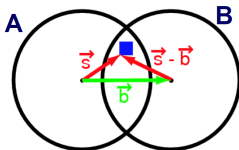


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- Number of participant in  $A$ :

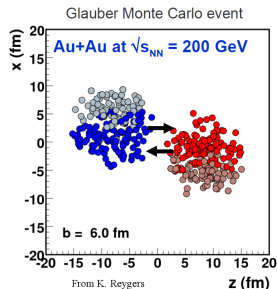
$$\langle N_{part}^A(b) \rangle = A \int \frac{T_A(\vec{s})}{A} (1 - (1 - \frac{T_B(\vec{s})}{B} \times \sigma_{NN}^{inel.})^B) d^2s$$

- Total mean number of participant:  $\langle N_{part}^A(b) \rangle + \langle N_{part}^B(b) \rangle$



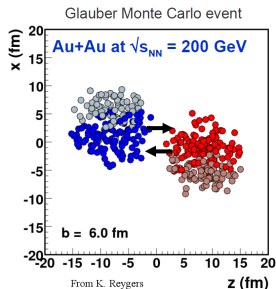
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- As illustrated by the ALICE example, the **experiments** use Glauber MC to determine  $N_{part}$  vs  $N_{coll}$



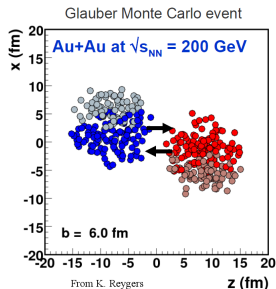
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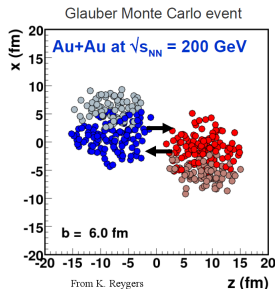
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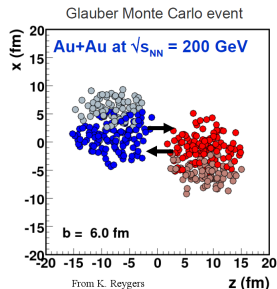
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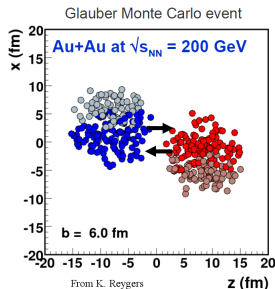


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The larger the number of collisions is,

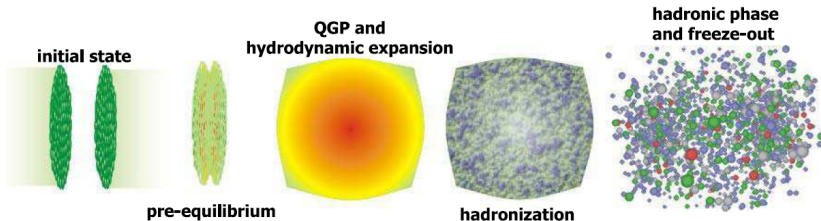
- the larger the energy released is,  
the larger the energy density is



# Part V

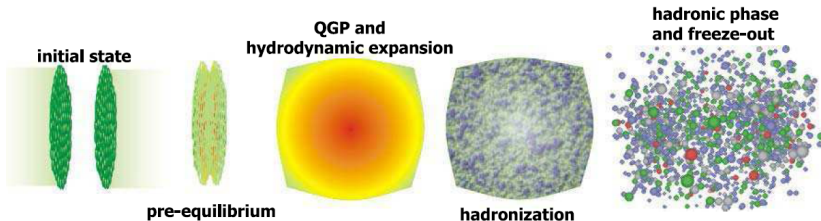
## Snapshots of a nucleus-nucleus collision

# Evolution stages of a nucleus-nucleus collision



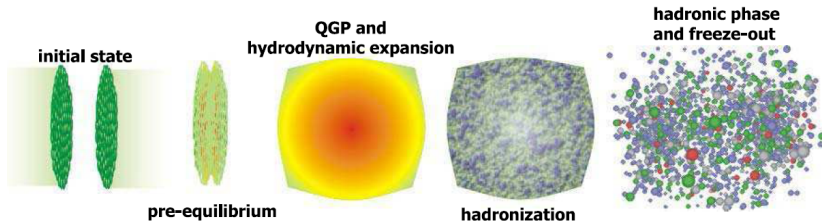


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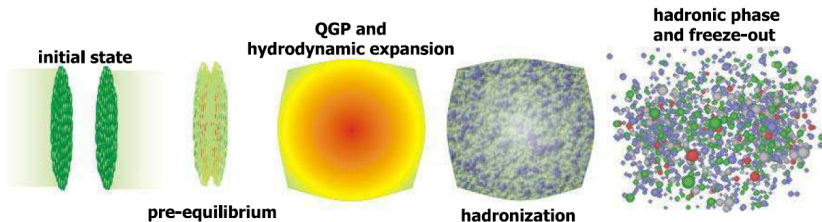
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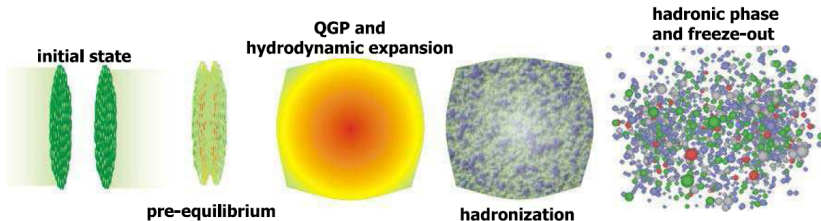
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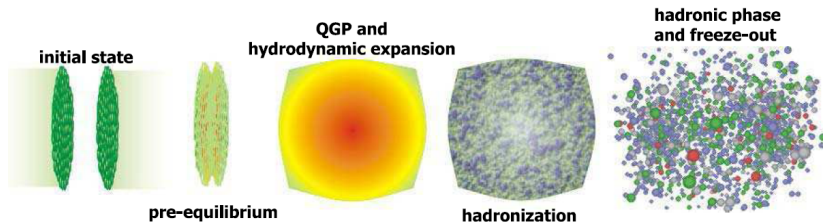
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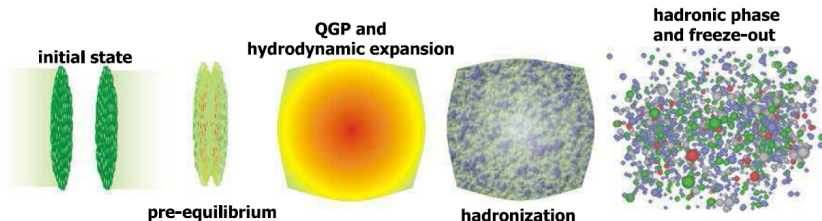
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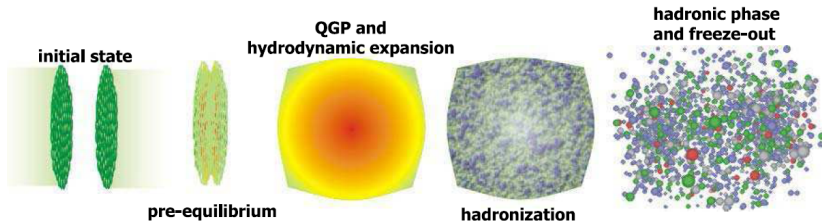
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Measurement at stage 5 & 6 to learn about stage 3