

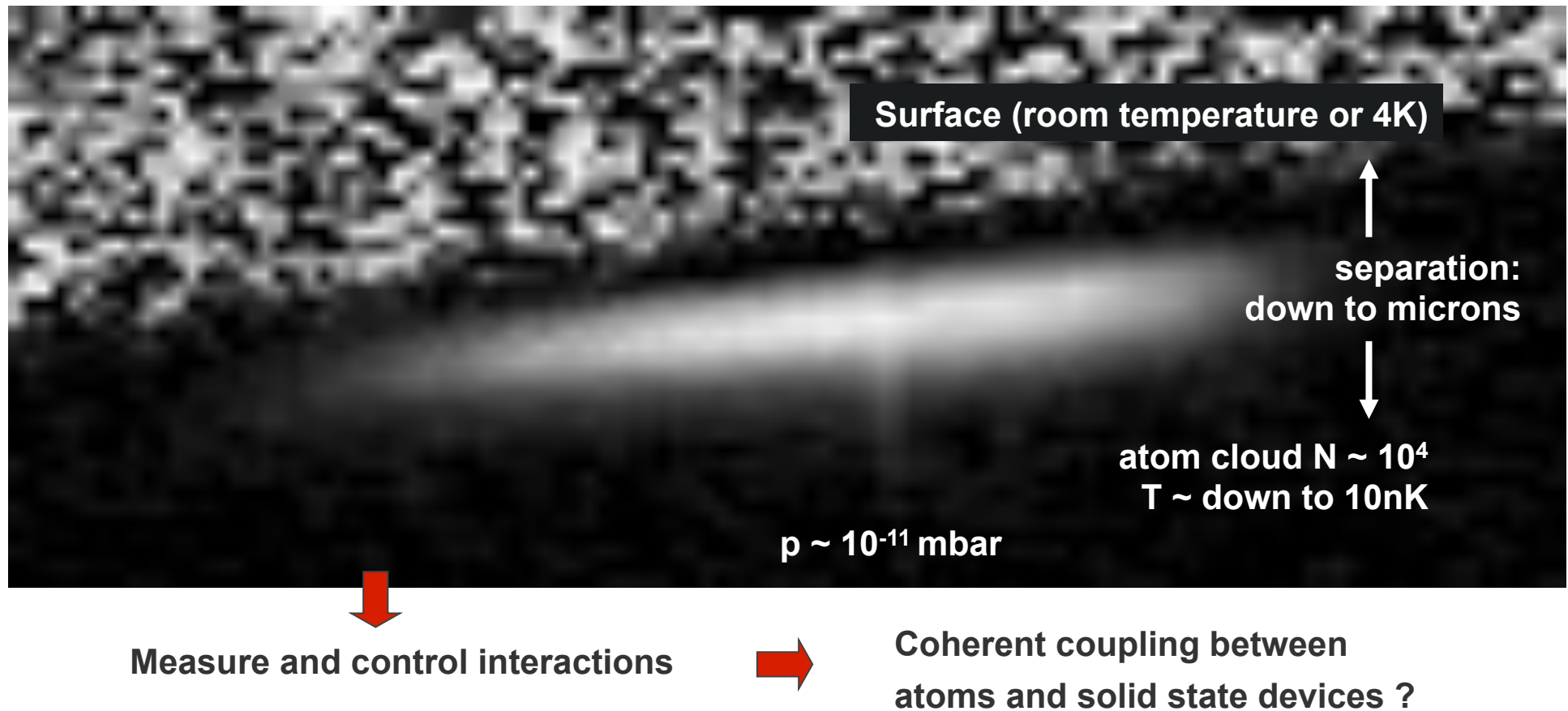


Interfacing cold atoms and superconductors

József Fortágh

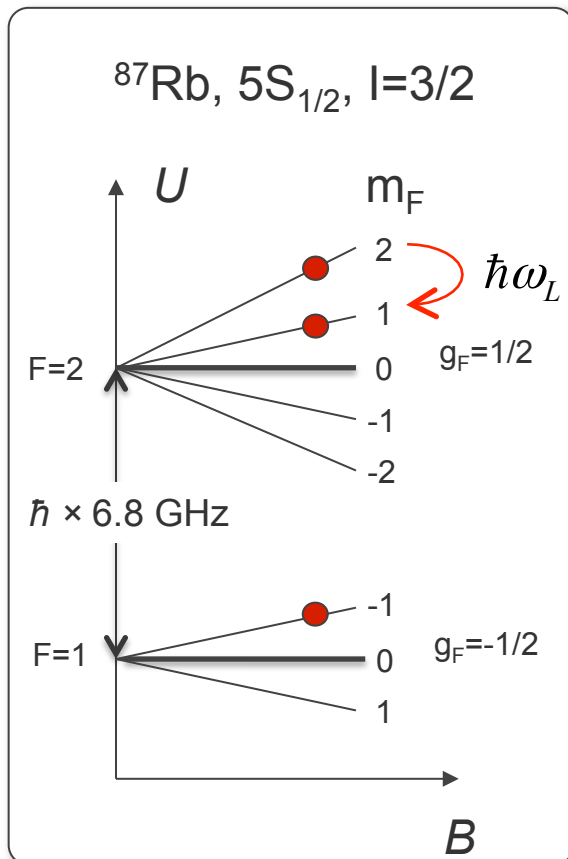


Cold atom – solid state interface





Rubidium ground state Zeeman splitting



$$H_Z = -\overline{\mu} \cdot \overline{B}$$

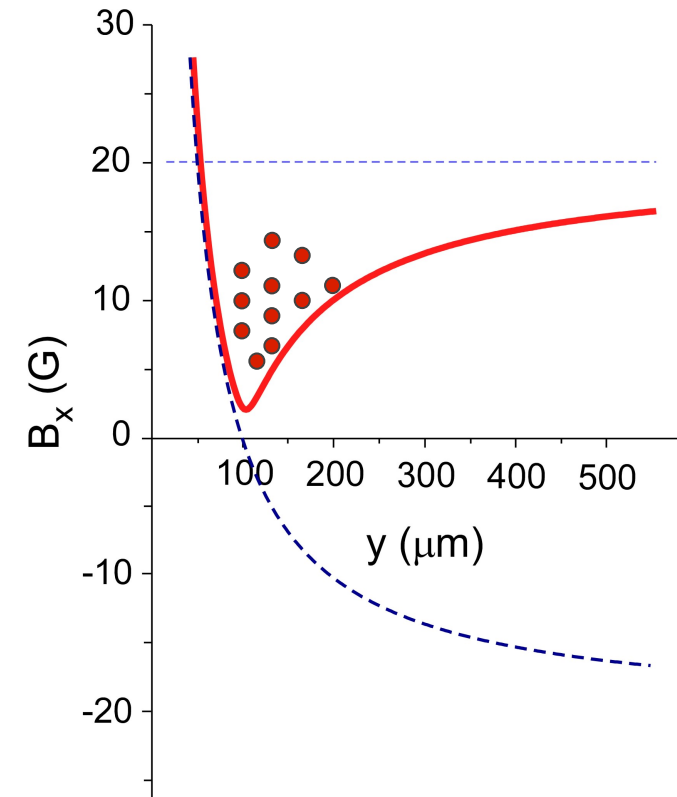
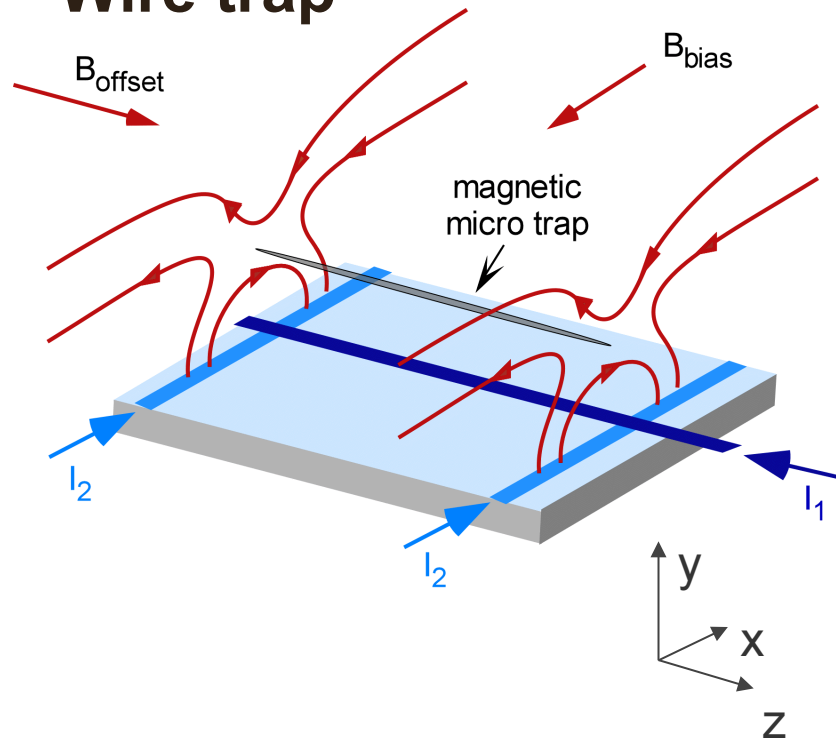
Magnetic moment: $\overline{\mu} = -g_F \mu_B \frac{\overline{F}}{\hbar} = -g_F \mu_B m_F$

Larmor frequency: $\omega_L = \frac{g_F \mu_B |B|}{\hbar}$

Magnetic trap: $U_{trap} = \mu \cdot |B|$



Wire trap



Harmonic potential (*Ioffe-Pritchard trap*)

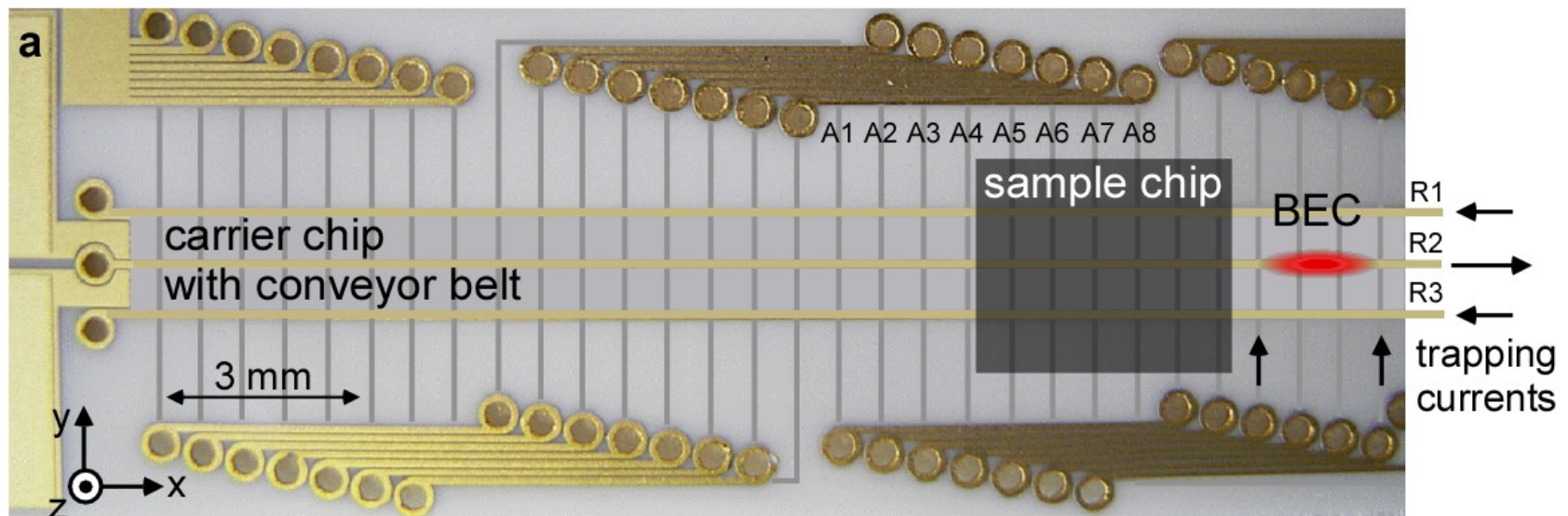
*Strong suppression of
Majorana spin-flip transitions:*

Sukumar and Brink, *PRA* 56, 2451 (1997)

Review: "Magnetic microtraps for ultracold atoms", Fortagh & Zimmermann, *Rev. Mod. Phys.* 79, 235 (2007)



Nanopositioning atomic clouds



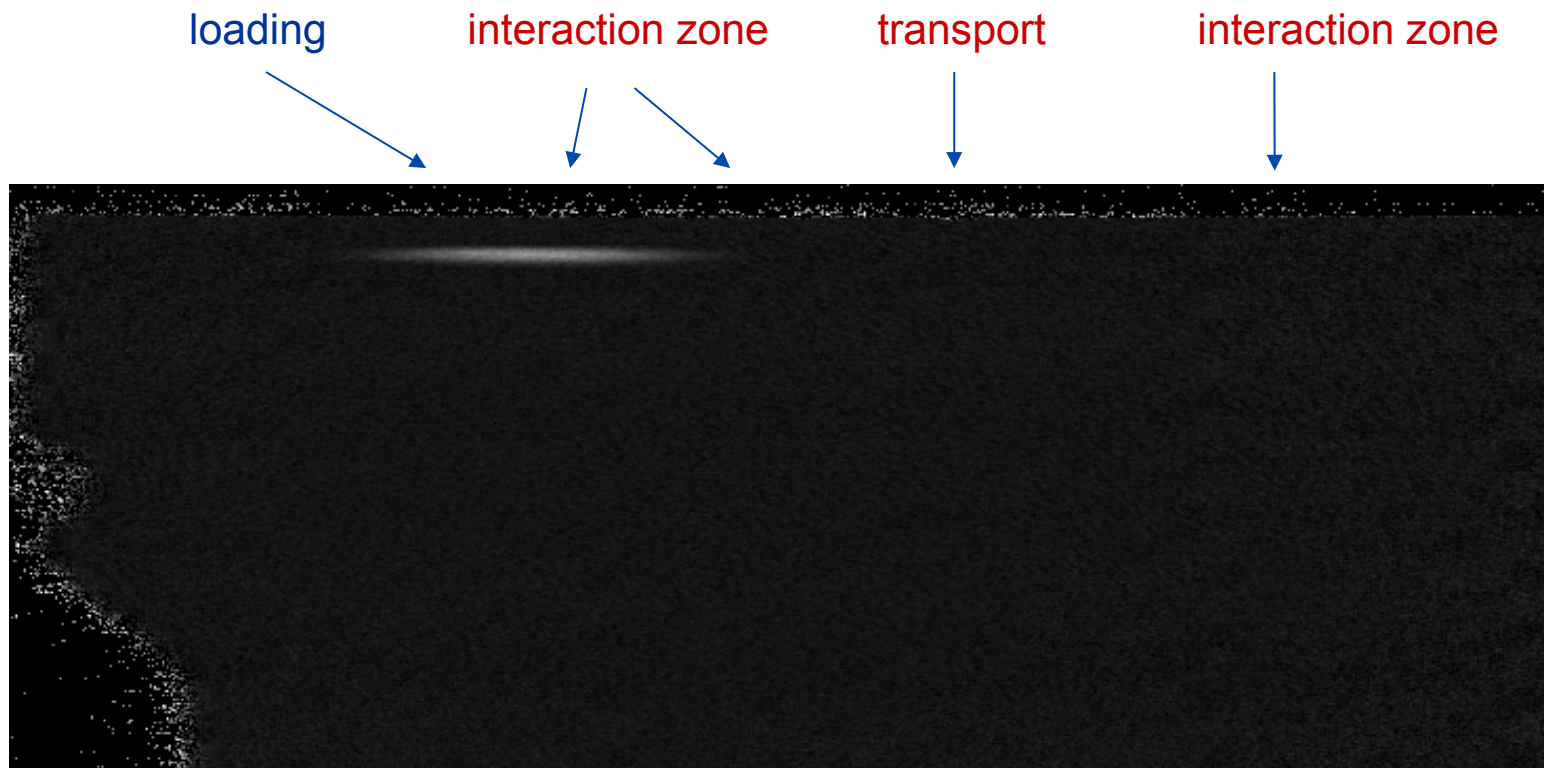
3D nanopositioning

positioning accuracy $< \pm 250$ nm velocity uncertainty $\Delta v < \pm 25$ $\mu\text{m/s}$

Gierling et al., Nat. Nanotechnol. **6**, 445-451 (2011)



Nano-positioning of atomic clouds on a chip



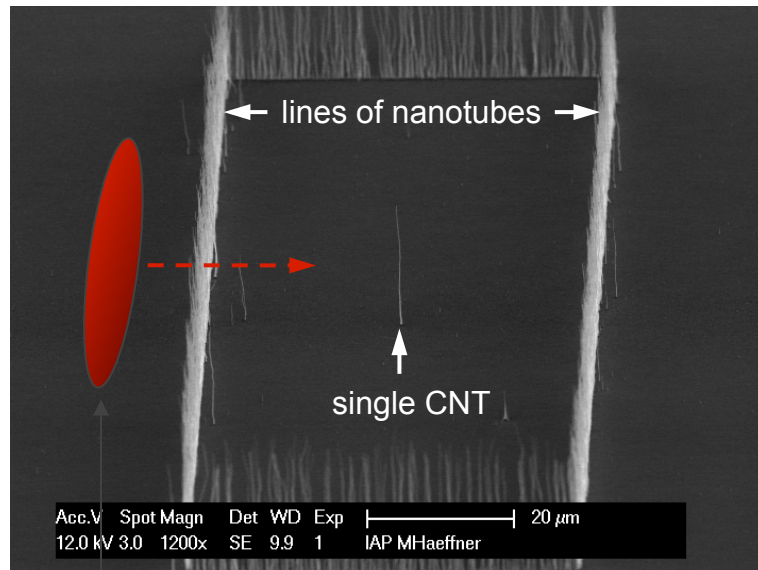
positioning accuracy $< \pm 250$ nm velocity uncertainty $\Delta v < \pm 25$ $\mu\text{m/s}$

Gierling et al., Nat. Nanotechnol. **6**, 445-451 (2011)



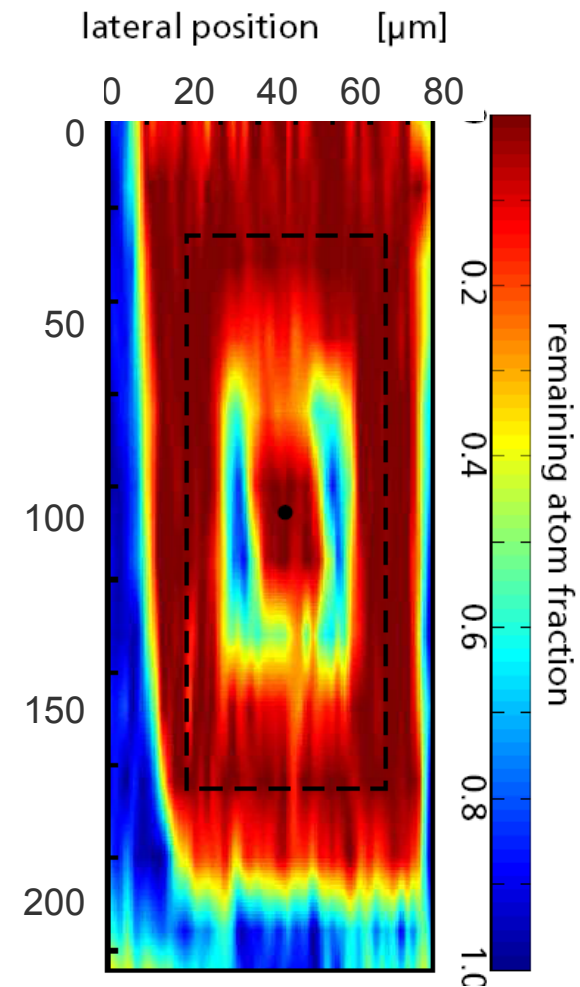
Scanning a BEC above the surface

Trap frequencies $(\omega_r, \omega_a) = 2 \pi \times (81, 17) \text{ 1/s}$



Atomic cloud & scan direction

SEM image

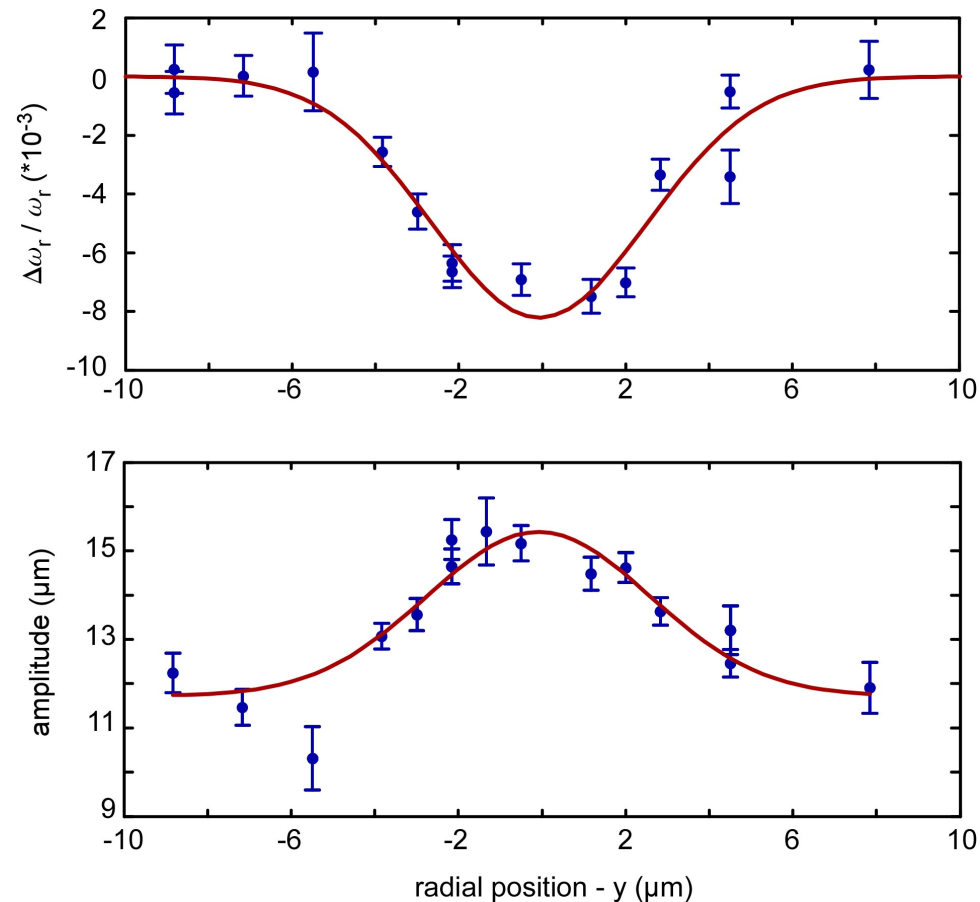
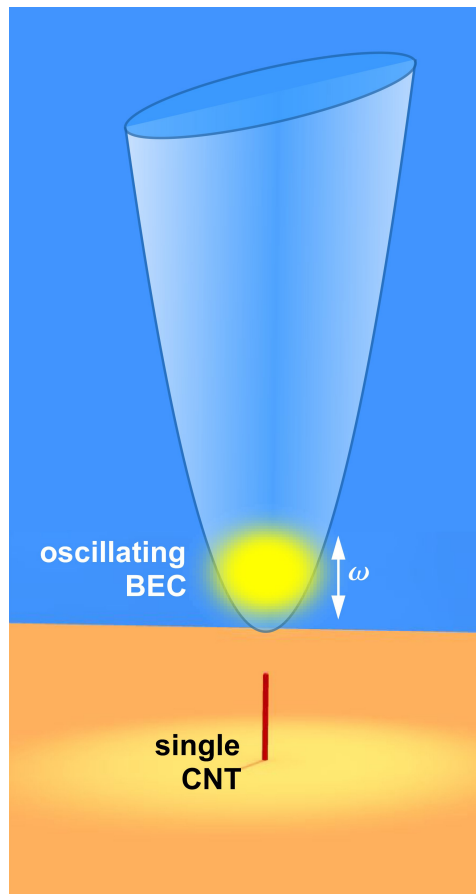


Gierling et al., *Nat. Nano.* 6, 445-451 (2011)

Schneeweiss et al., *Nat. Nano* 7, 515-519 (2012)



BEC oscillating above the surface



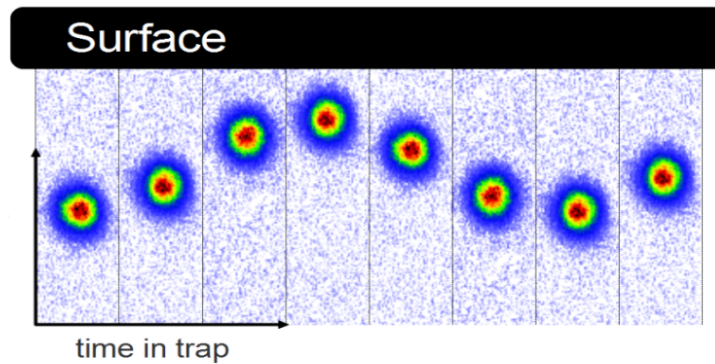
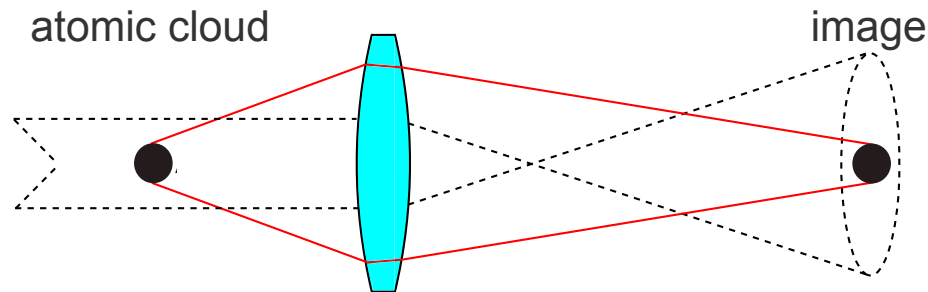
Measured force between nanotube tip and an atom in the trap: $2 \times 10^{-25} \text{ N} \cong 0.2 \text{ yN}$

Harber et al., PRA 72, 033610 (2005)
Obrecht et al., PRL 98, 063201 (2007)

Gierling et al., Nat. Nano. 6, 445-451 (2011)
Schneeweiss et al., Nat. Nano 7, 515-519 (2012)

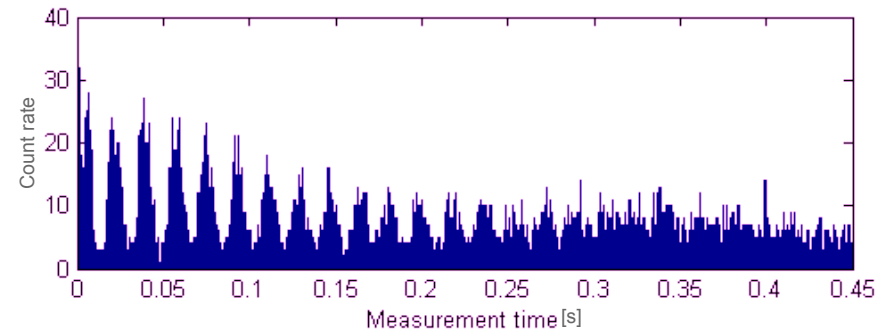
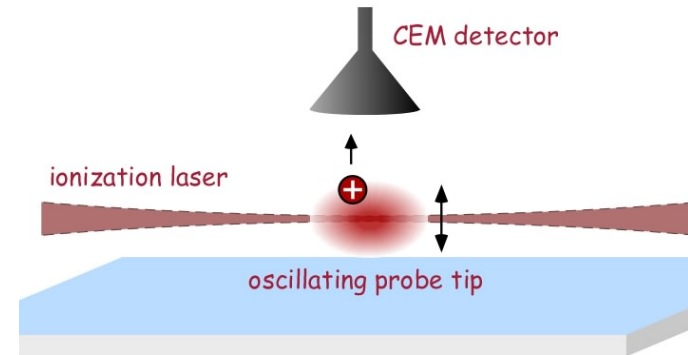


Absorption imaging



One measurement point: few seconds

Single atom detection



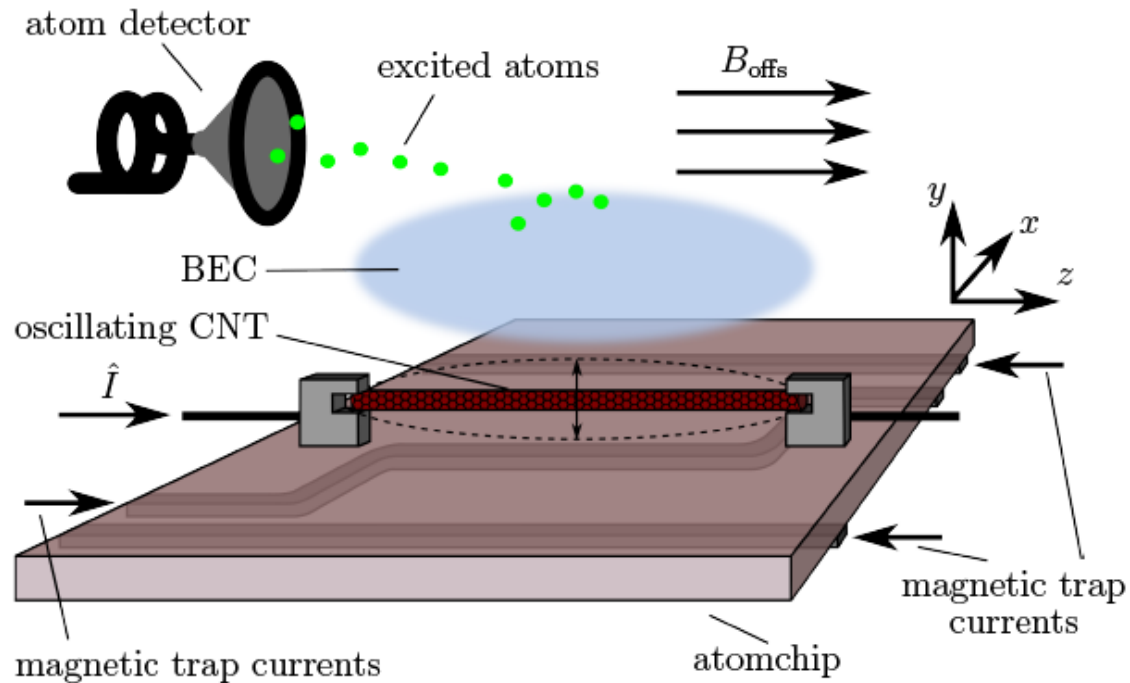
One point in <1 ms, full curve: few seconds

Stibor et al., New J. Phys. 12, 065034 (2010)



Quantum galvanometer / spectrum analyzer

Magneto-mechanical interface between atoms and a vibrating nanowire.



Quantum noise of
electric currents?

Quantum drive of
mechanical vibrations?

Quantum galvanometer:
Kálmán et al., Nano Letters 12, 435-439 (2013)

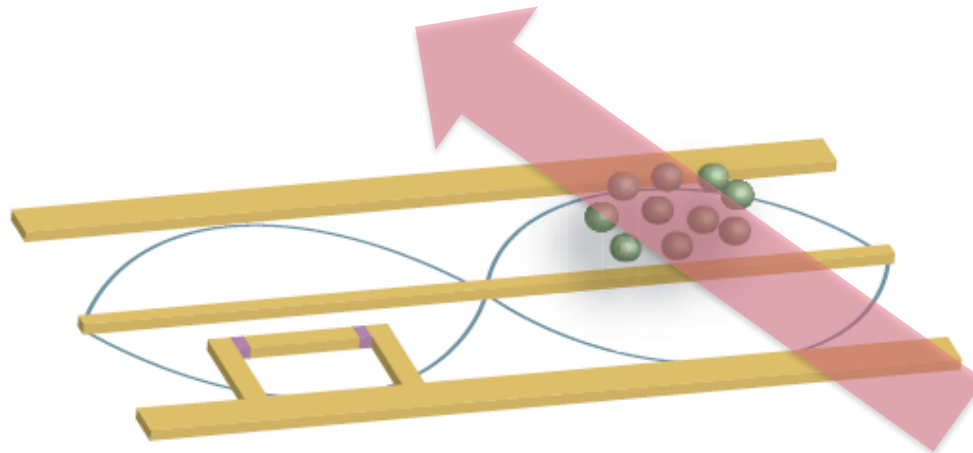
Single atom detector:
Stibor et al., New J. Phys. 12, 065034 (2010)

Parametric drive of mechanic oscillations by the BEC:
Darázs et al., Phys. Rev. Lett. 112, 133603 (2014)



Coupling superconducting devices and atomic gases

via superconducting-coplanar-waveguide resonators operating in the microwave regime



Proposals for quantum information processing

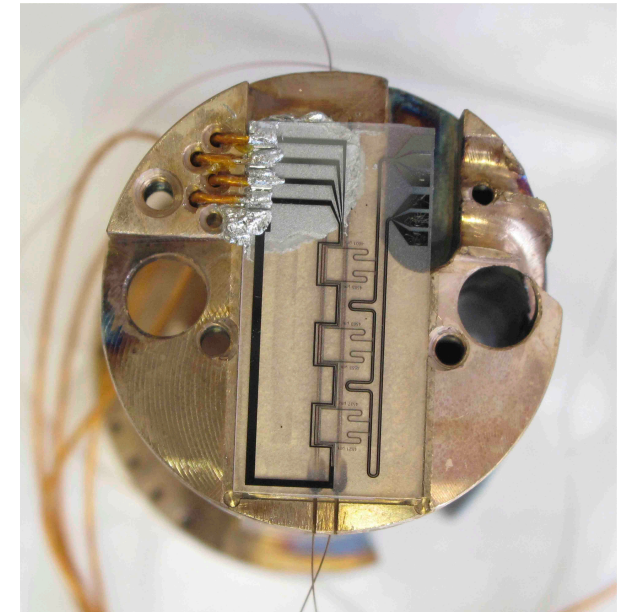
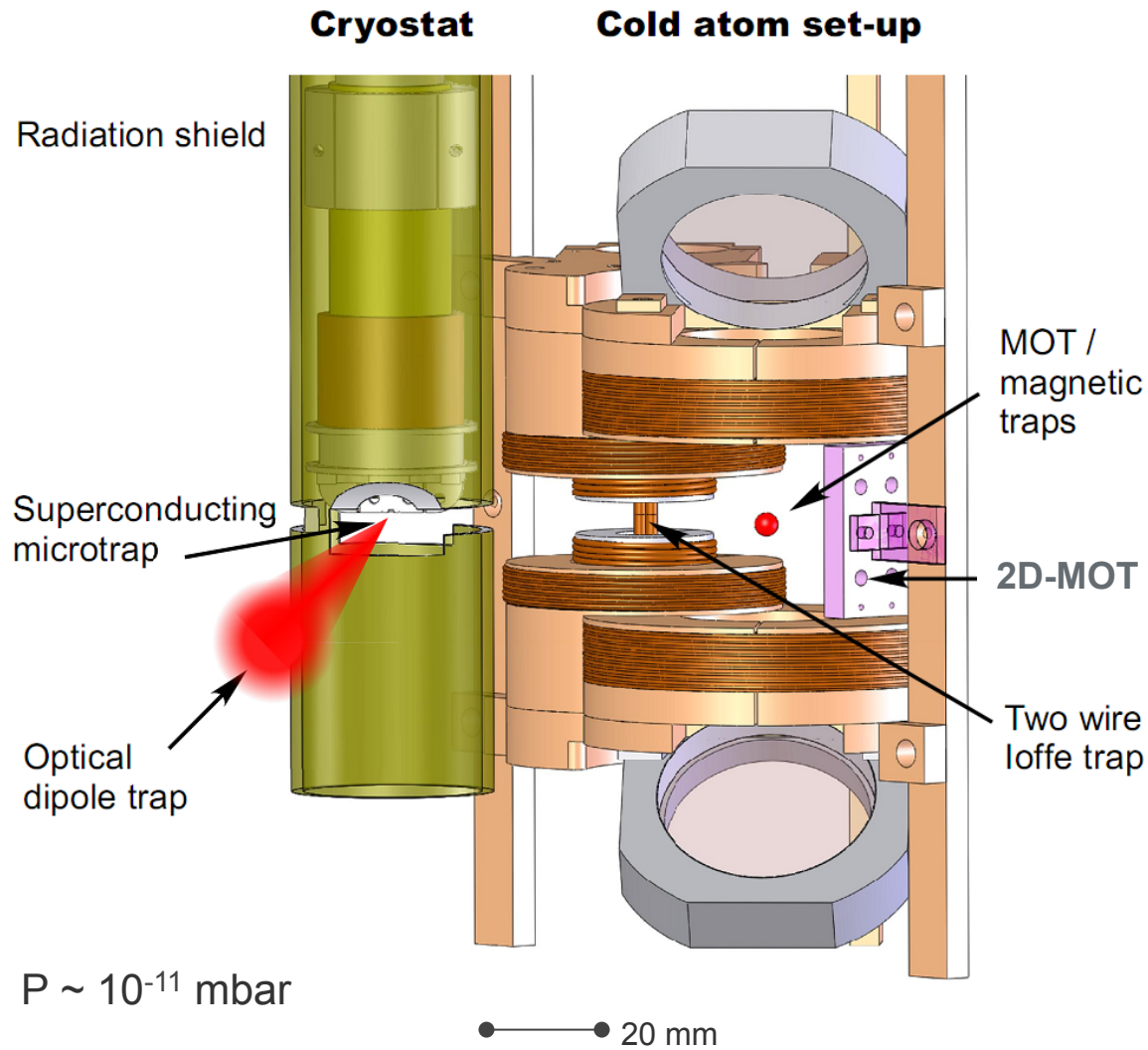
- K. Tordrup and K. Molmer, PRA 77 020301(R) (2008)

- Henschel et al., PRA **82**, 033810 (2010)
- Verdú et al., PRL 103, 043603 (2009)
- Petrosyan and Fleischhauer, PRL 100, 170501 (2008)
- Petrosyan et al., Phys. Rev. A 79, 040304 (2009)
- Rabl et al., PRL 97, 033003 (2006)
- Sorensen et al., PRL 92, 063601 (2004)

The list is growing...



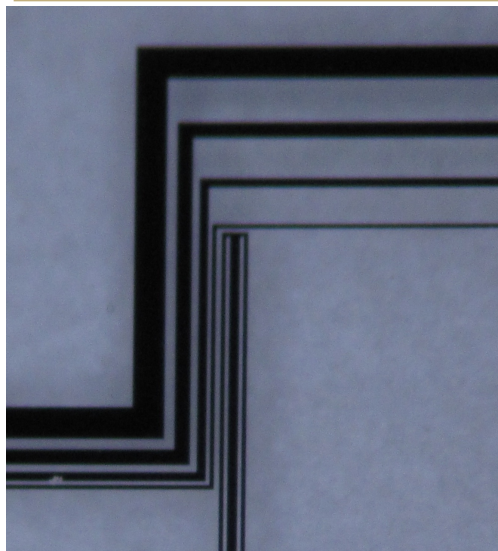
Cold atoms & superconductors



Cano et al., Eur. Phys. J. D **63**, 17-23 (2011)



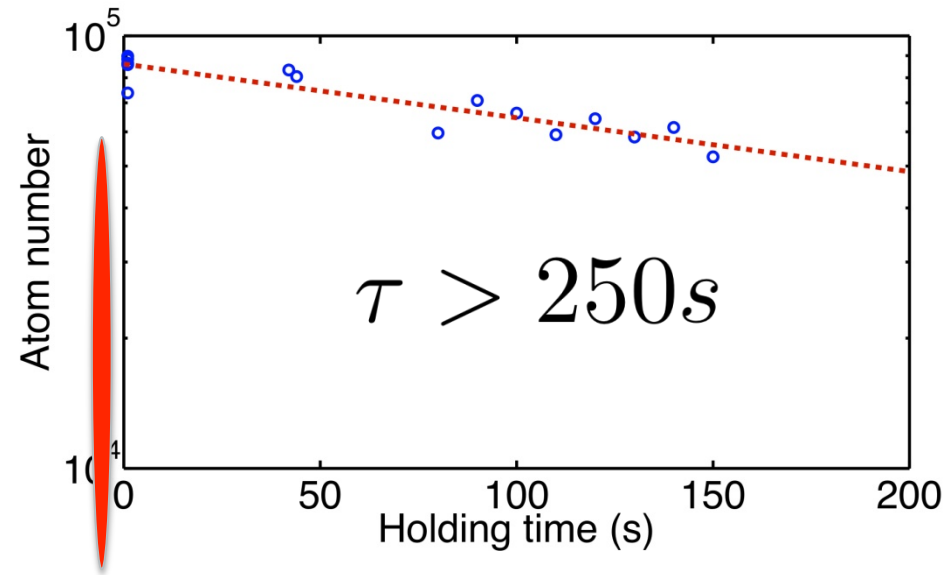
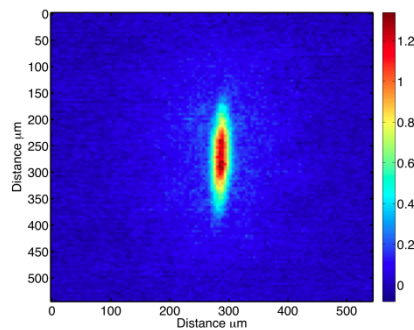
Cold atoms on the SC chip



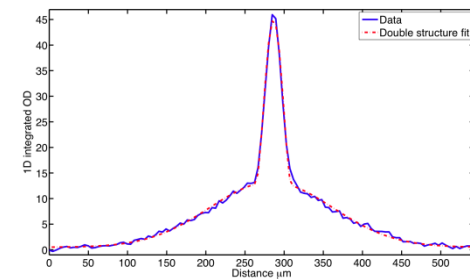
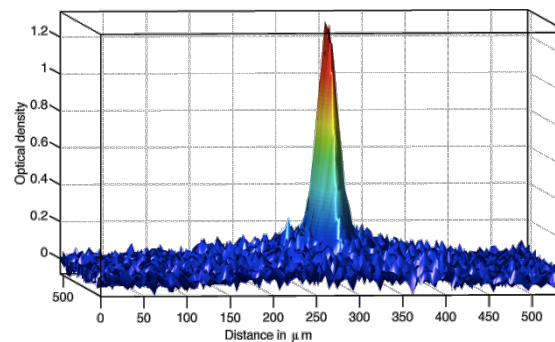
Chip surface



TOF

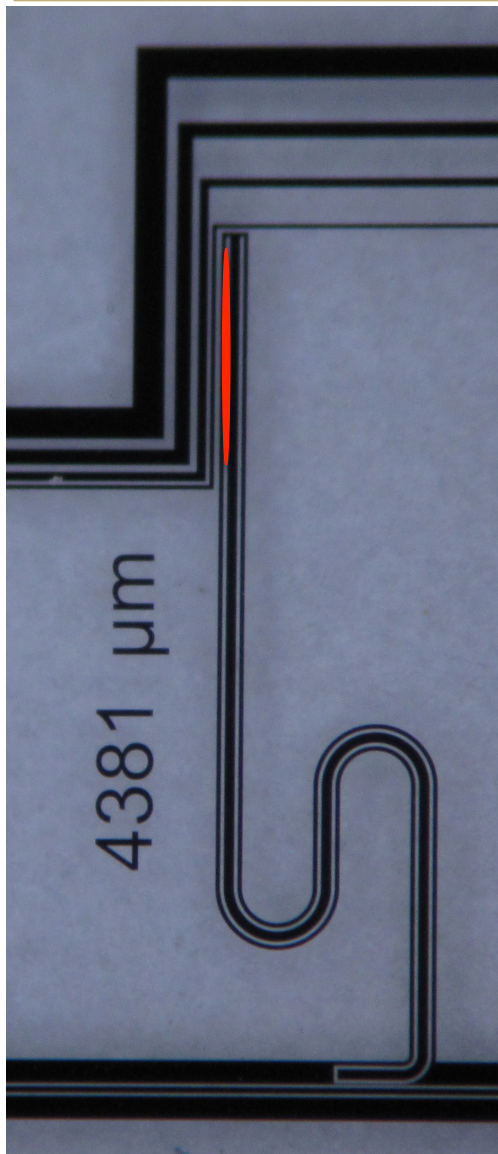


$N_C \approx 10^6$ in the F=1 or F=2 hyperfine state

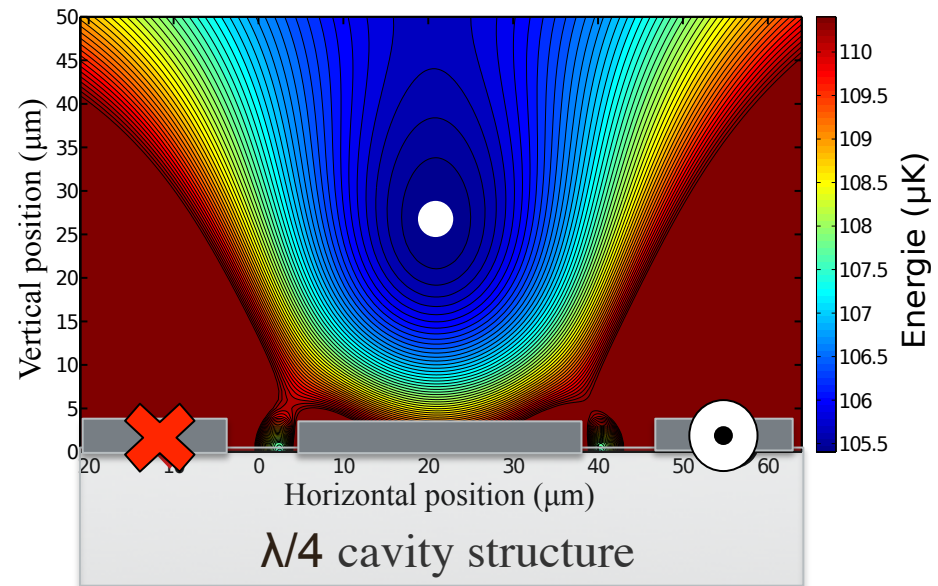




Trapping atoms at the superconducting microwave cavity

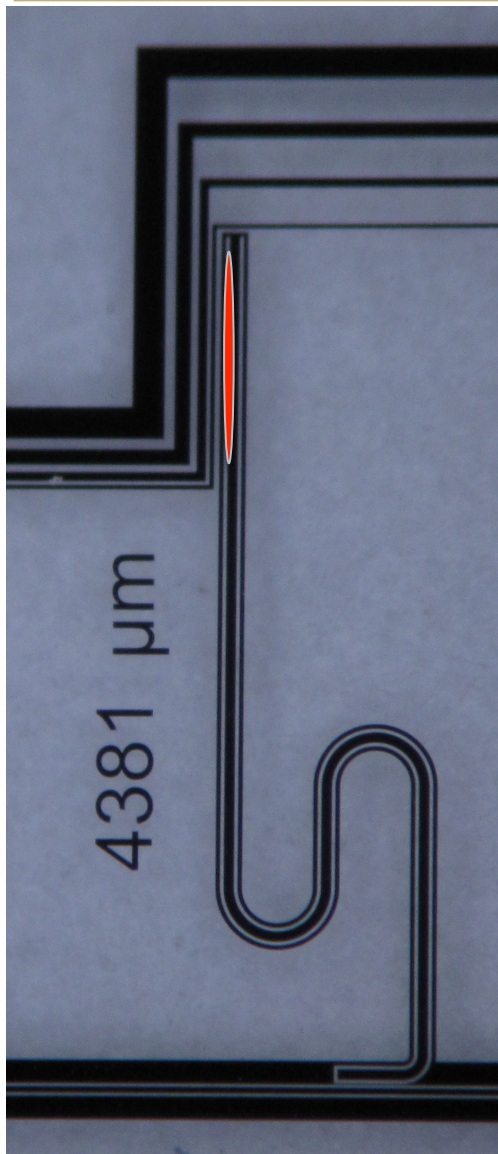


Persistent current trap





Atomic coherence at the superconducting coplanar cavity structure



$$|0\rangle \rightarrow \frac{1}{\sqrt{2}} (|0\rangle + |1\rangle)$$

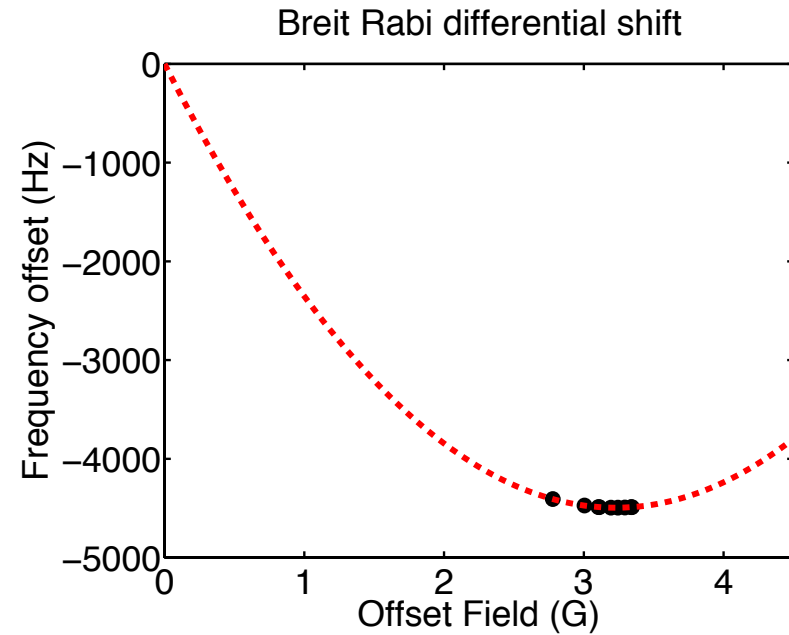
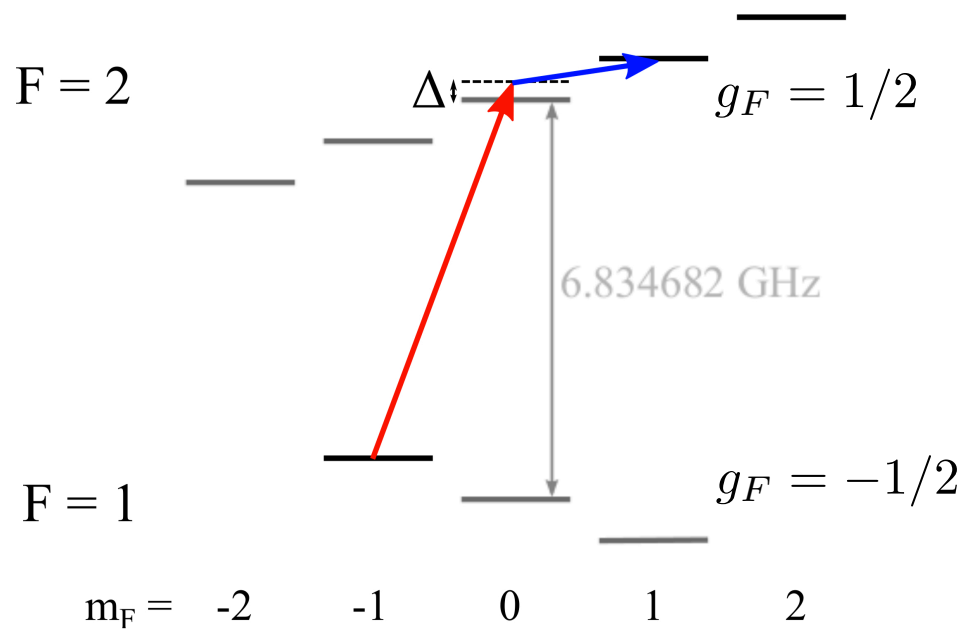
Time evolution



Coherence ?



Atomic coherence on a SC chip



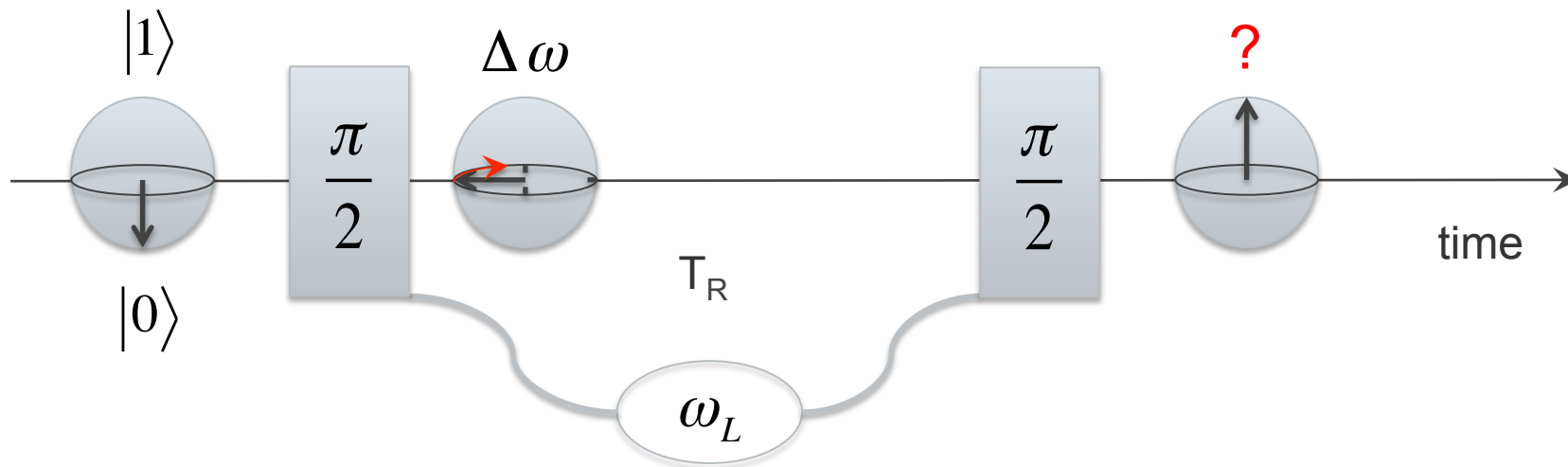
At 500 nK: differential shift $< 1 \text{ Hz}$

D.M. Harber *et al* Phys. Rev. A **66**, 053616 (2002)

P. Treutlein *et al* Phys. Rev. Lett. **92**, 203005 (2004)



Ramsey interferometry

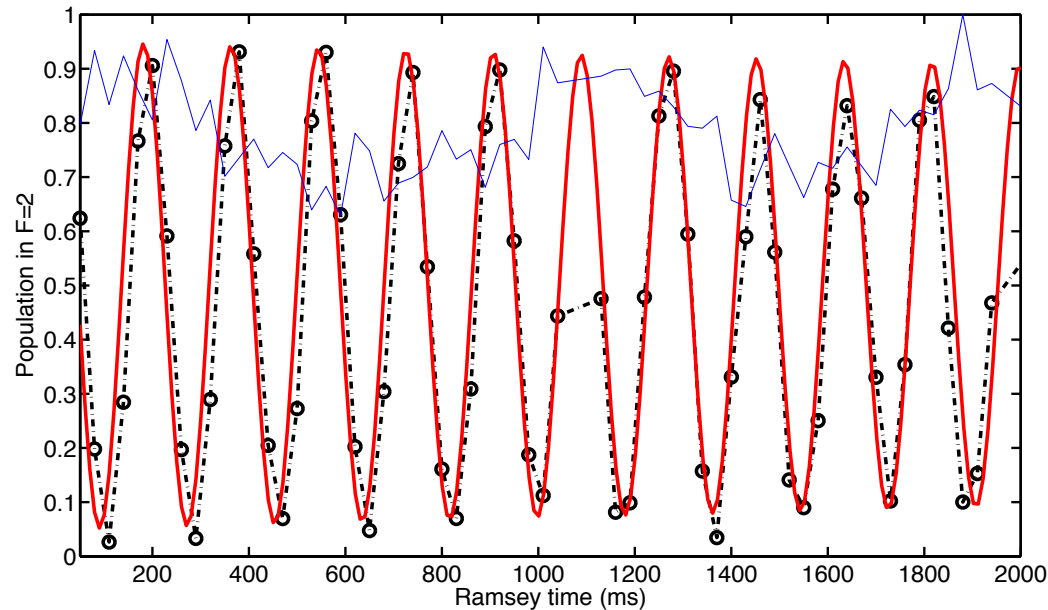


$$|0\rangle \rightarrow \frac{1}{\sqrt{2}} (|0\rangle + |1\rangle) \rightarrow \text{Coherence ?}$$



Atomic coherence on a SC chip

Ramsey interferometer $\frac{\pi}{2} T_R \frac{\pi}{2}$



Long coherence time > 2 s !!

Parameters:

Atomic cloud

$$\omega_l/2\pi \approx 20 \text{ Hz}$$

$$\omega_r/2\pi \approx 180 \text{ Hz}$$

$$z_0 \approx 60 \mu\text{m}$$

$$N_{\text{at}} \approx 3 \times 10^4$$

$$\bar{n} \approx 10^{13} \text{ at.cm}^{-3}$$

Interferometer

Rabi frequency

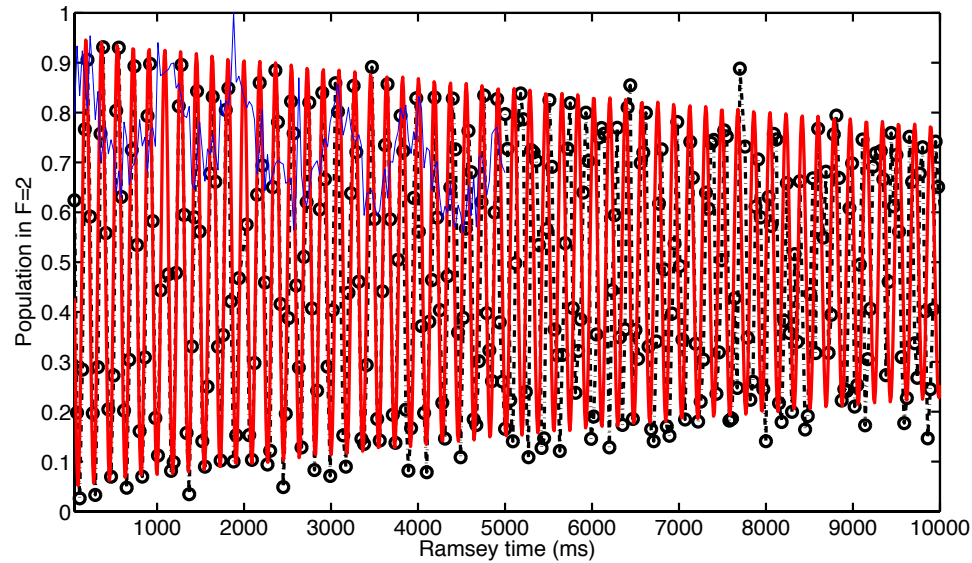
$$\Omega_R/2\pi = 400 \text{ Hz}$$

Single photon detuning

$$\Delta/2\pi = 900 \text{ kHz}$$

Two photons detuning

$$\delta/2\pi = 5.5 \text{ Hz}$$



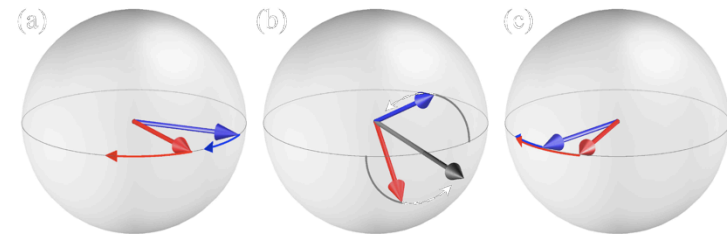
Coherence time $T_2 \approx 20 \text{ s}$

Expected due to residual frequency inhomogeneity in the trap $T_2 \approx 6.5 \text{ s}$

Identical spin rotation effect synchronizes the clock

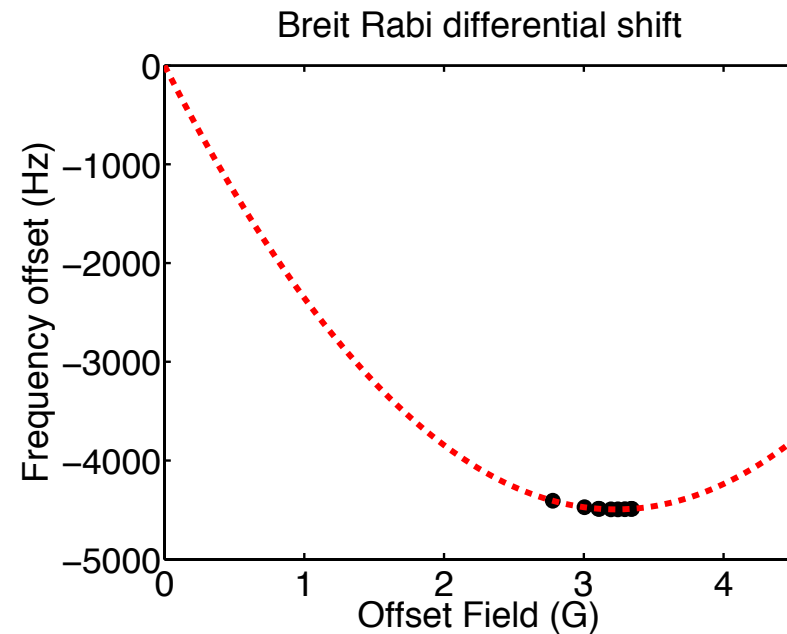
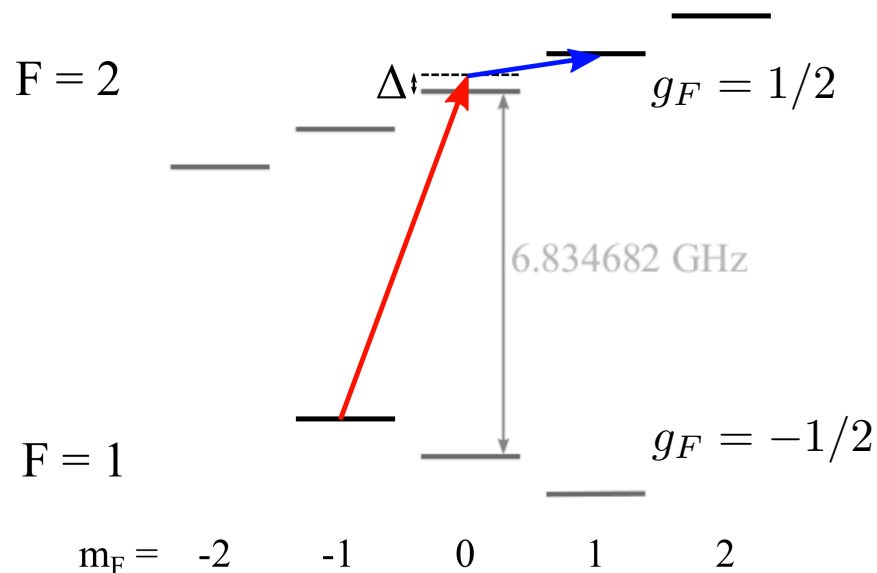
C. Deutsch *et al* Phys. Rev. Lett. **105**, 020401 (2010)

Bernon *et al.*, Nat. Commun. **4**, 2380 (2013)





The differential Zeeman shift and magnetic field fluctuations limit the clock coherence



$$\Delta\omega(B) \cong \omega_f + \beta \cdot (B - B_0)^2$$

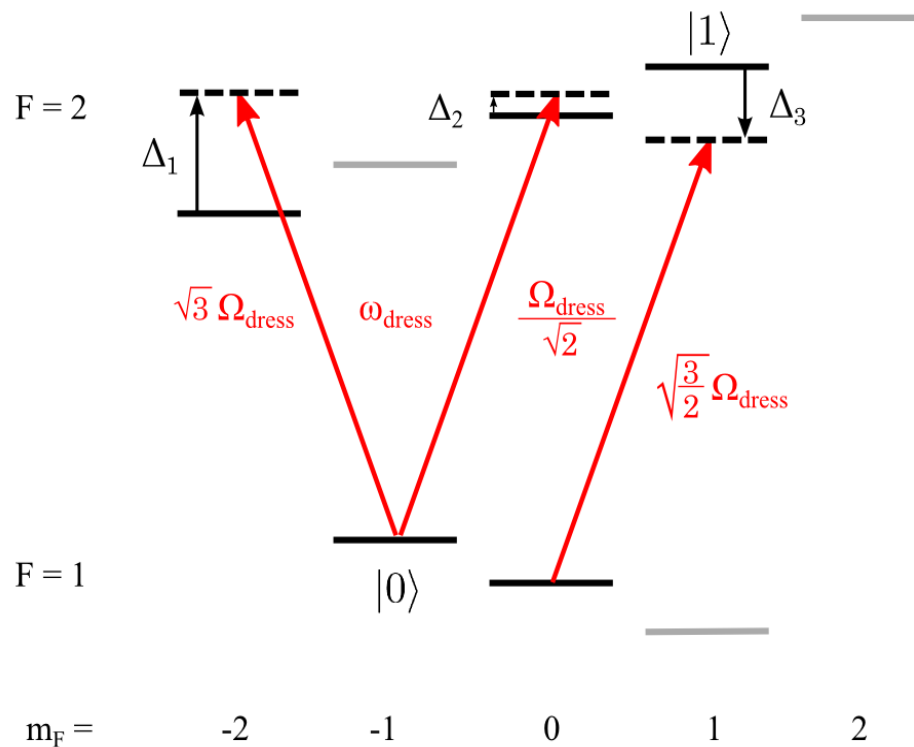
O. Zobay and B. M. Garraway
Phys. Rev. Lett. **86**, 1195 (2001)

L. A. Jones, J. D. Carter, and J. D. D. Martin
Phys. Rev. A **87**, 023423 (2013)

Zanon-Willette, de Clercq, Arimondo
Phys. Rev. Lett. **109**, 223003 (2012)



Dressing the clock transition



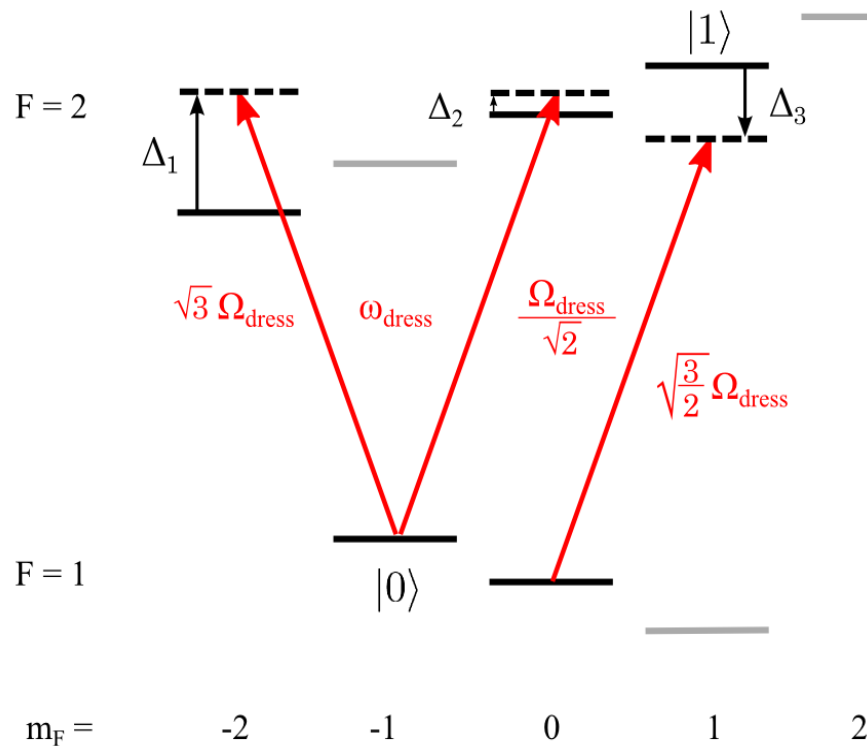
Dressing field with perpendicular polarisation to the magnetic field at the trap centre (quantisation axis).

$$H_0 = \hbar \begin{bmatrix} 0 & \sqrt{3}\Omega_{\text{dress}} & \frac{1}{\sqrt{2}}\Omega_{\text{dress}} \\ \sqrt{3}\Omega_{\text{dress}} & -\Delta_1 & 0 \\ \frac{1}{\sqrt{2}}\Omega_{\text{dress}} & 0 & -\Delta_2 \end{bmatrix}$$

$$H_1 = \hbar \begin{bmatrix} 0 & \sqrt{\frac{3}{2}}\Omega_{\text{dress}} \\ \sqrt{\frac{3}{2}}\Omega_{\text{dress}} & -\Delta_3 \end{bmatrix},$$



Dressing the clock transition



$$\Delta\omega(B) \cong \omega_f + \beta \cdot (B - B_0)^2$$

$$+ \Omega_{dress}^2 \cdot \left(\frac{3}{\Delta_1(B)} + \frac{1/2}{\Delta_2(B)} - \frac{3/2}{\Delta_3(B)} \right)$$

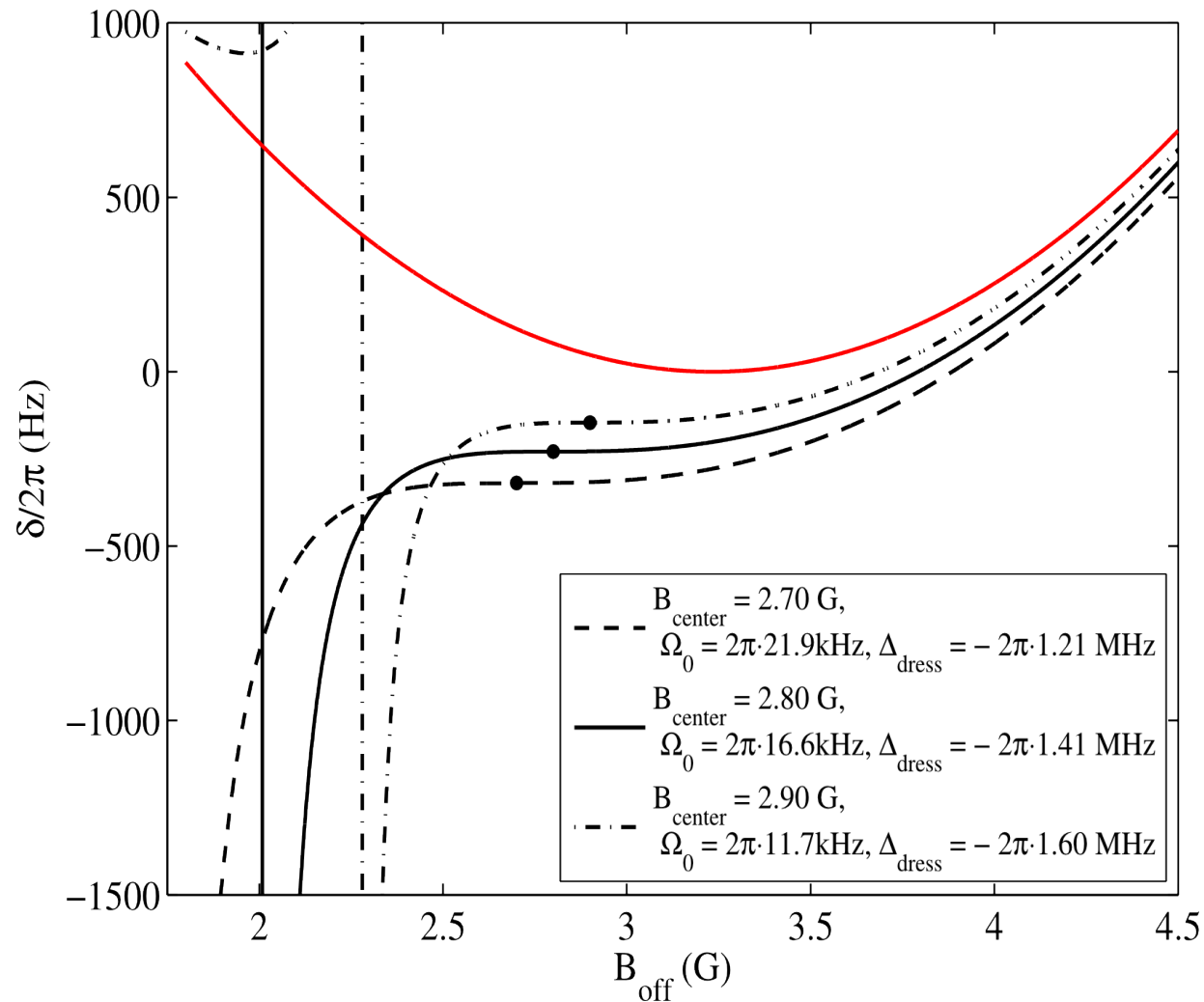
$$\frac{d\Delta\omega}{dB}, \frac{d^2\Delta\omega}{dB^2} = 0 \Rightarrow \Omega_{dress}, \omega_{dress}$$

$$\Omega_{dress} = \Omega_{dress}(B_{center}) !$$

$$\omega_{dress} = \omega_{dress}(B_{center}) !$$



Dressed clock

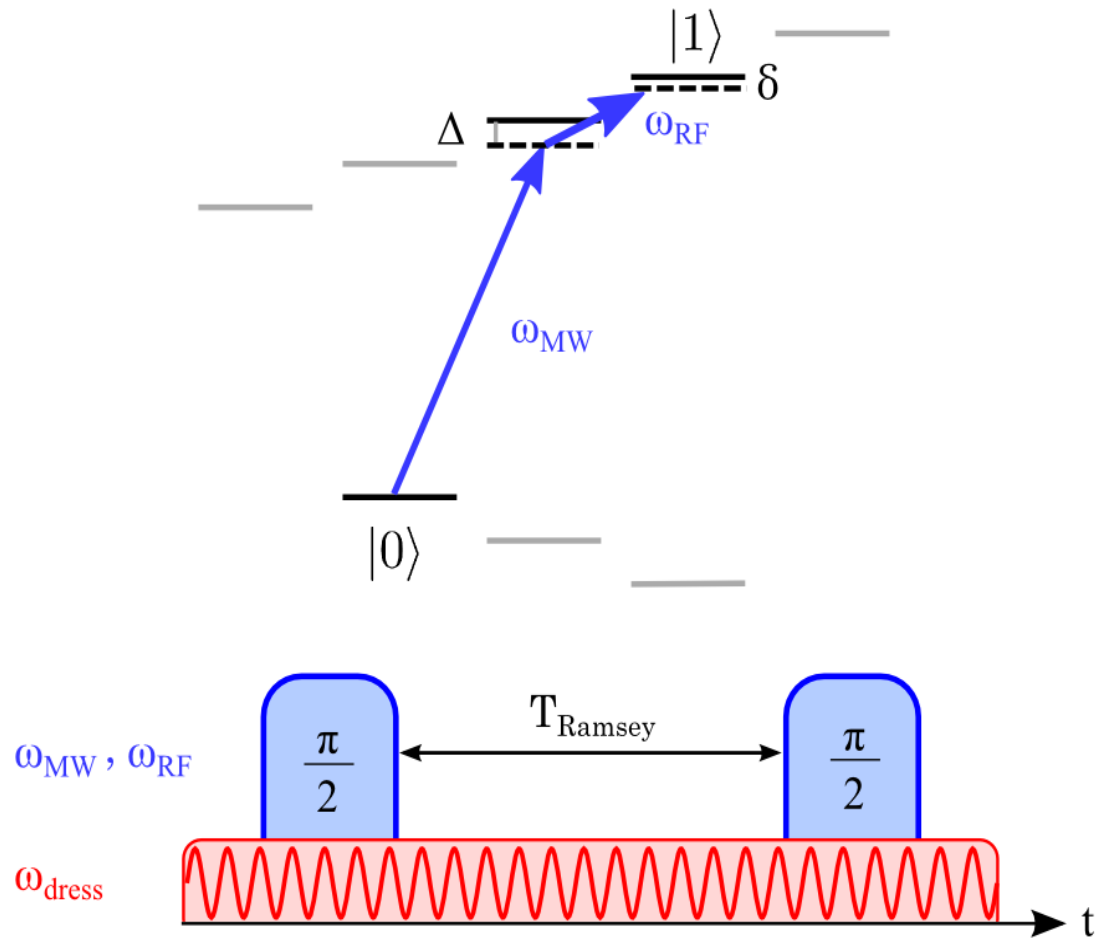


For any offset field
the differential shift
can be modified:

- suppressed
- enhanced
- structured.

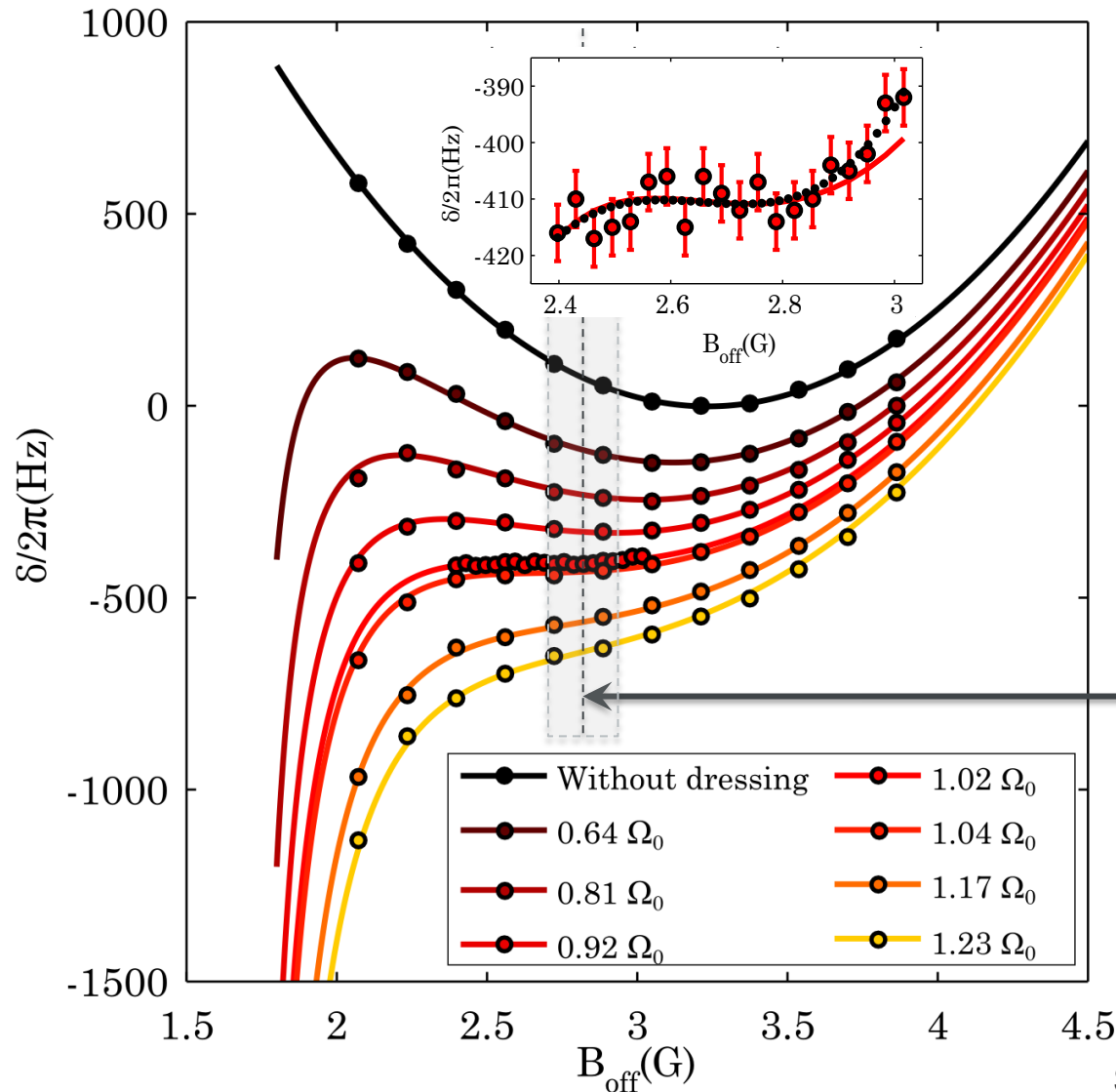


Ramsey interferometry with MW dressing





MW-control of the differential shift



$$\Delta_{\text{dress}} = -2\pi \times 1.19 \text{ MHz}$$

$$\Omega_0 = 2\pi \times 20.1 \text{ kHz}$$

$$B_{\text{center}} = 2.65 \text{ G}$$

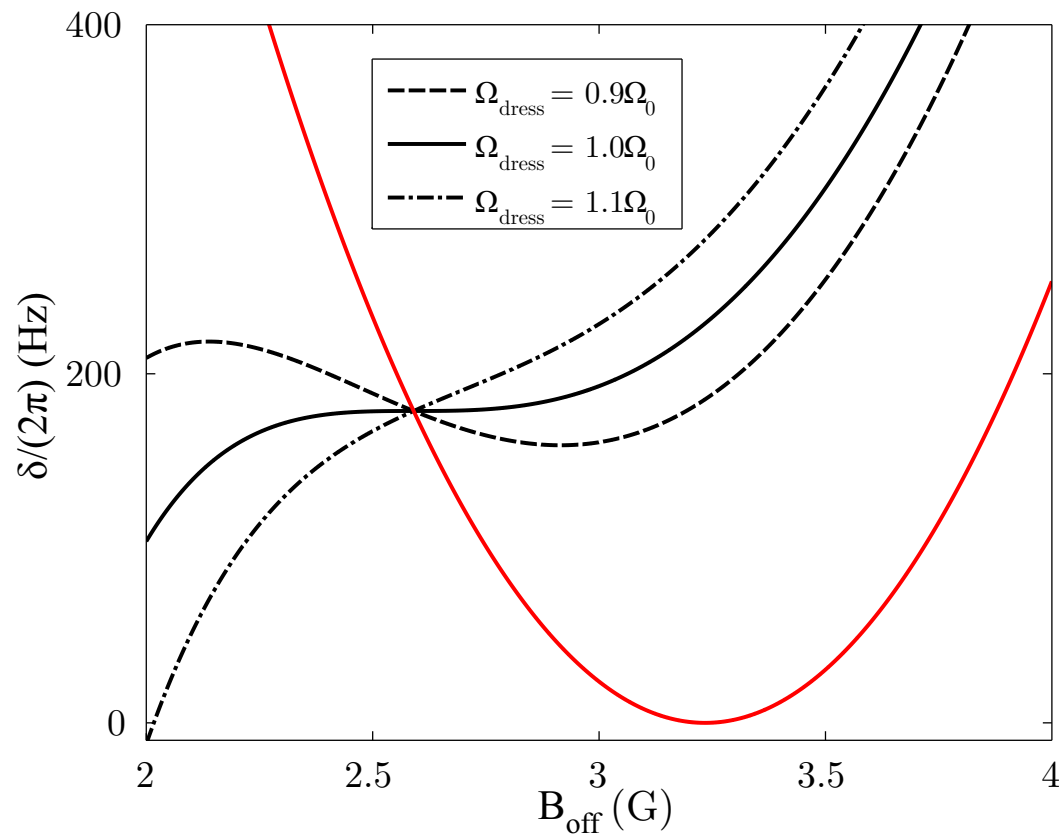
width (0.1 Hz): $\sim 100 \text{ mG}$

The the first and second order differential Zeeman-shifts are suppressed.



Doubly protected clock states

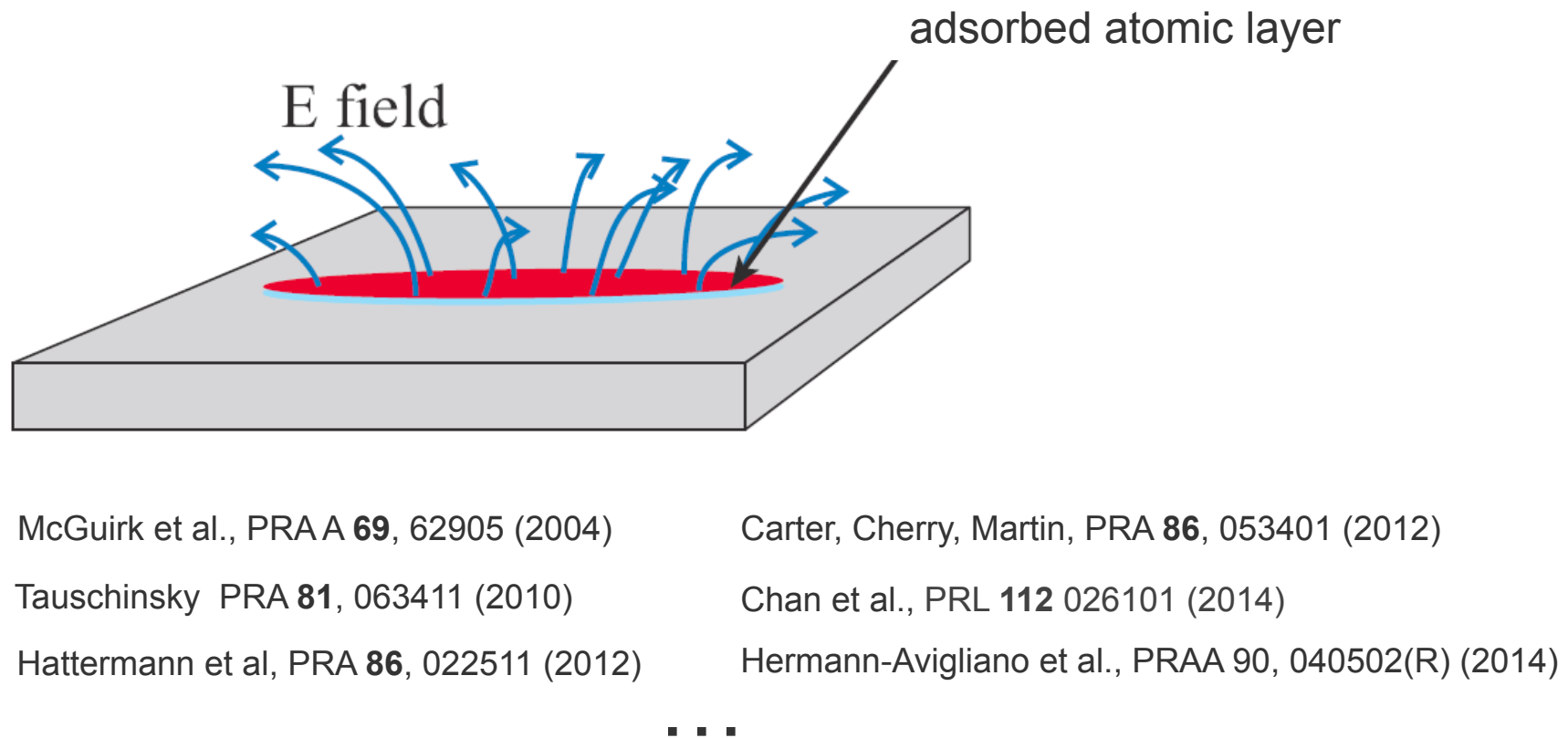
For certain offset fields the differential shift becomes independent also from the microwave power.



These “**double magic points**” are the preferable working points of trapped atomic clocks and quantum memories.



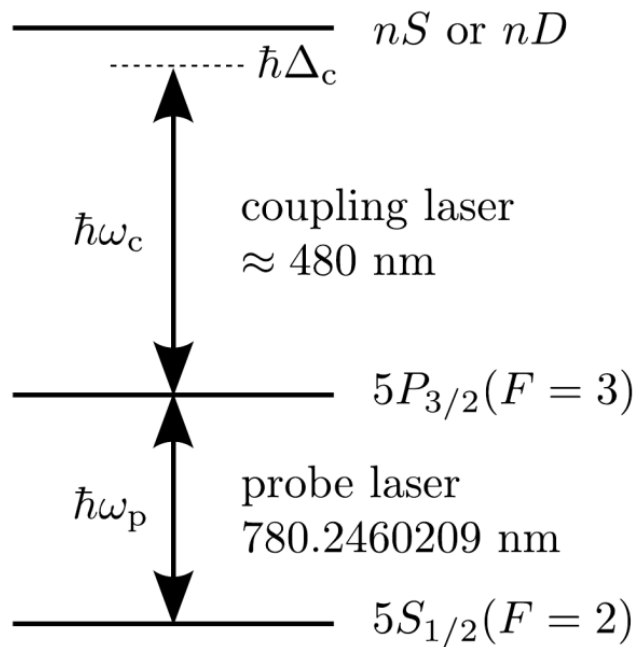
Polarized adatoms at the surface





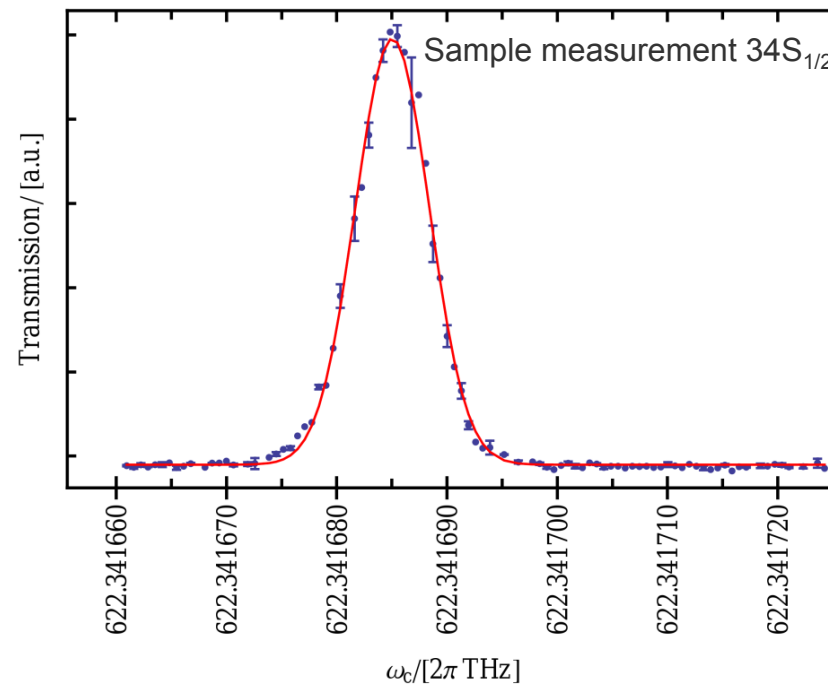
Spectroscopy of ^{87}Rb Rydberg states

Electromagnetically induced transparency (EIT)



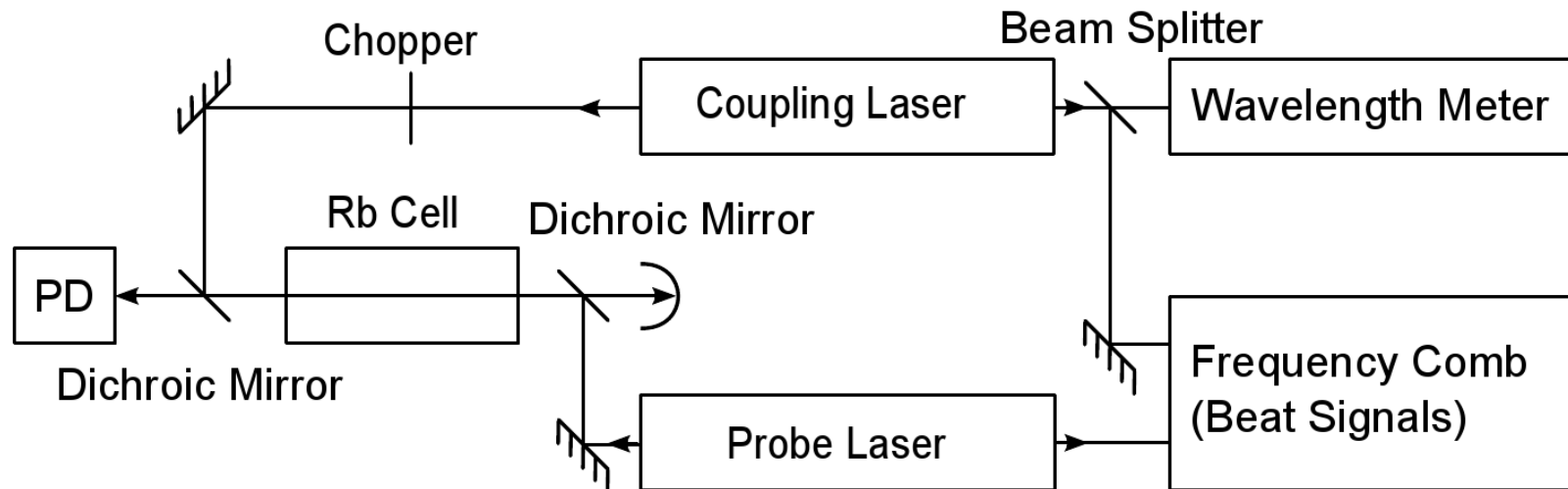
Mohapatra et al., PRL 98, 113003 (2002)

Karlewski et al., PRA 91, 043422 (2015)





EIT setup



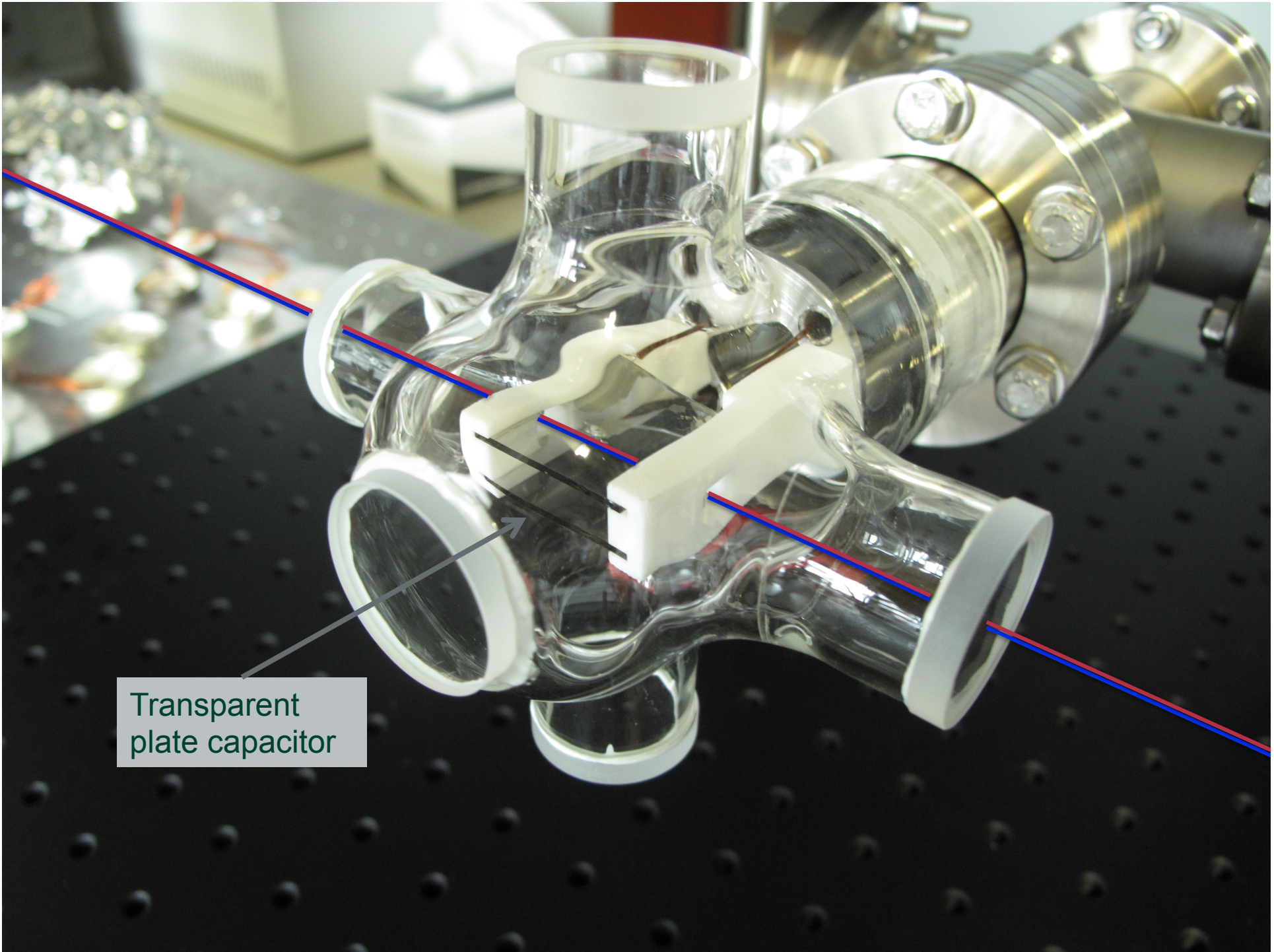
Precise measurement of quantum defects and ground state ionization energy of ^{87}Rb

(≤ 1 MHz abs. accuracy)

Mack et al., Phys. Rev. A **83**, 052515 (2011)

Quasi-classical quantum defect theory for describing the fine splitting of Rydberg states

Sanayei et al., PRA **91**, 032509 (2015)

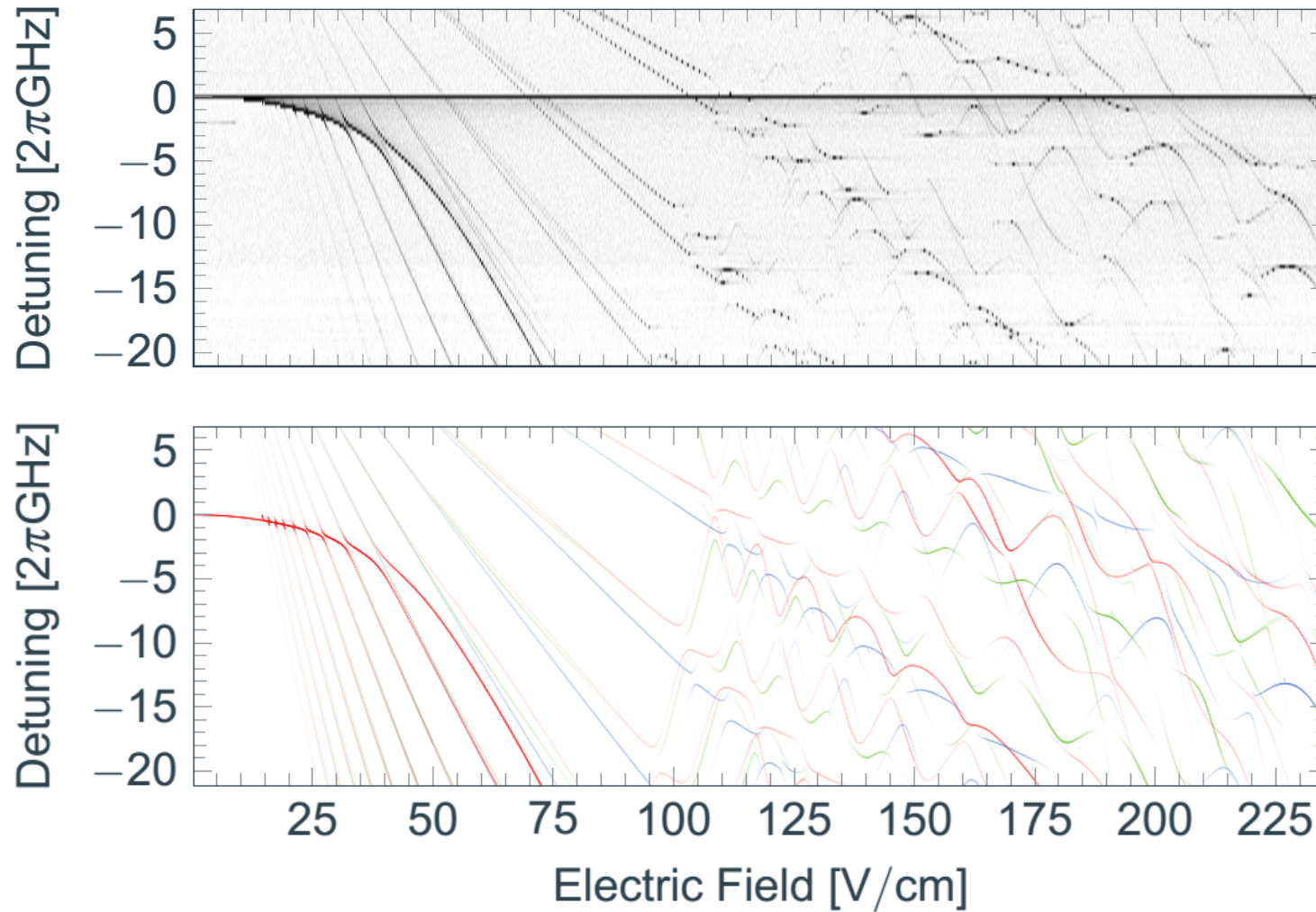


Transparent plate capacitor



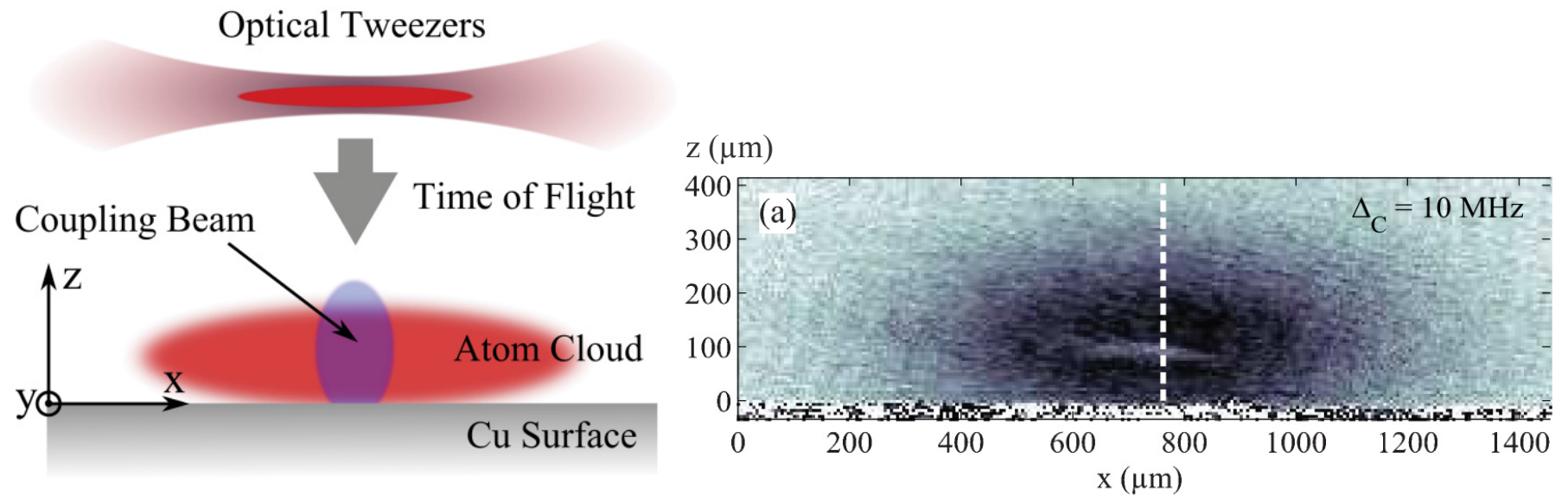
Stark-map in a cell

^{87}Rb 35S





Stark shift near a dipole layer (copper surface with Rb adsorbates)



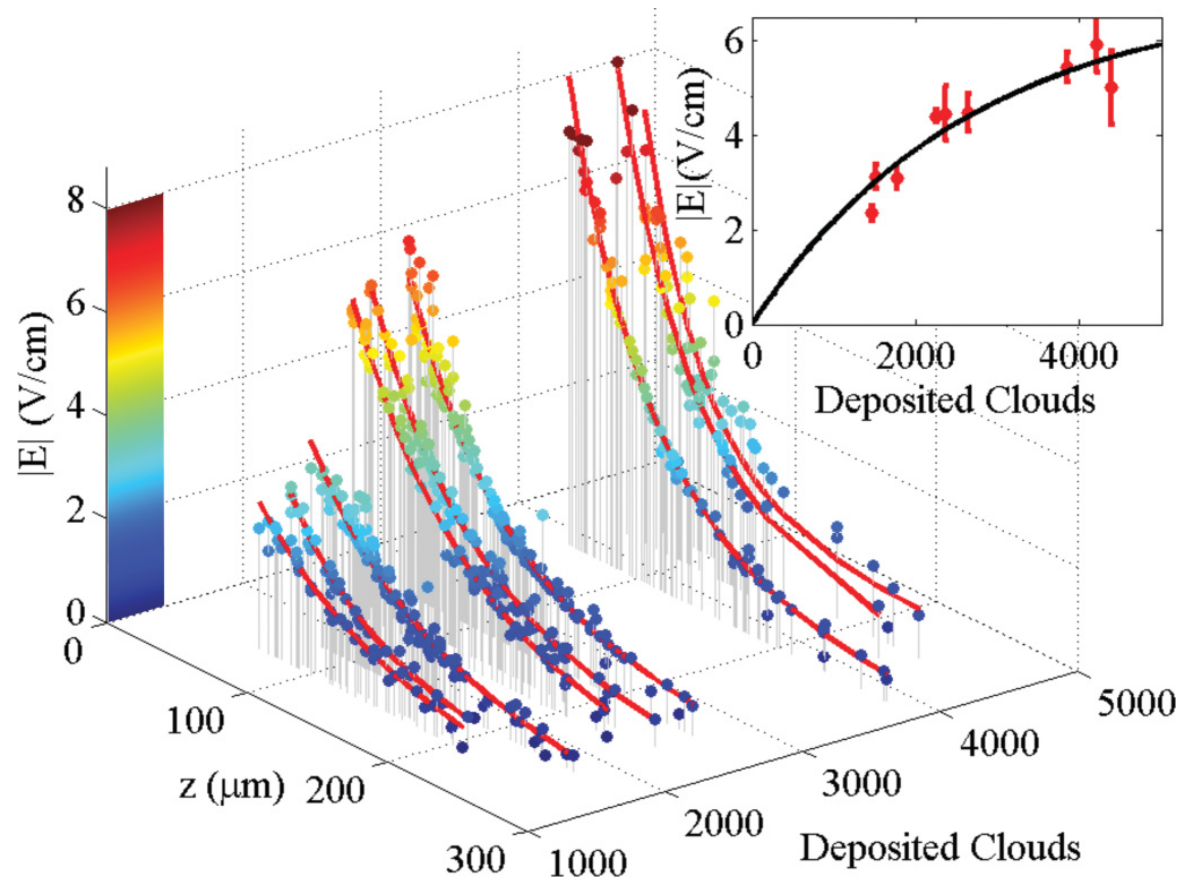
Energy shift measured with electromagnetically induced transparency (EIT)

Amsterdam: Tauschinsky Phys. Rev. A **81**, 063411 (2010)

Tübingen: Hattermann et al, Phys. Rev. A **86**, 022511 (2012)



Build up of electric fields due to adsorbates

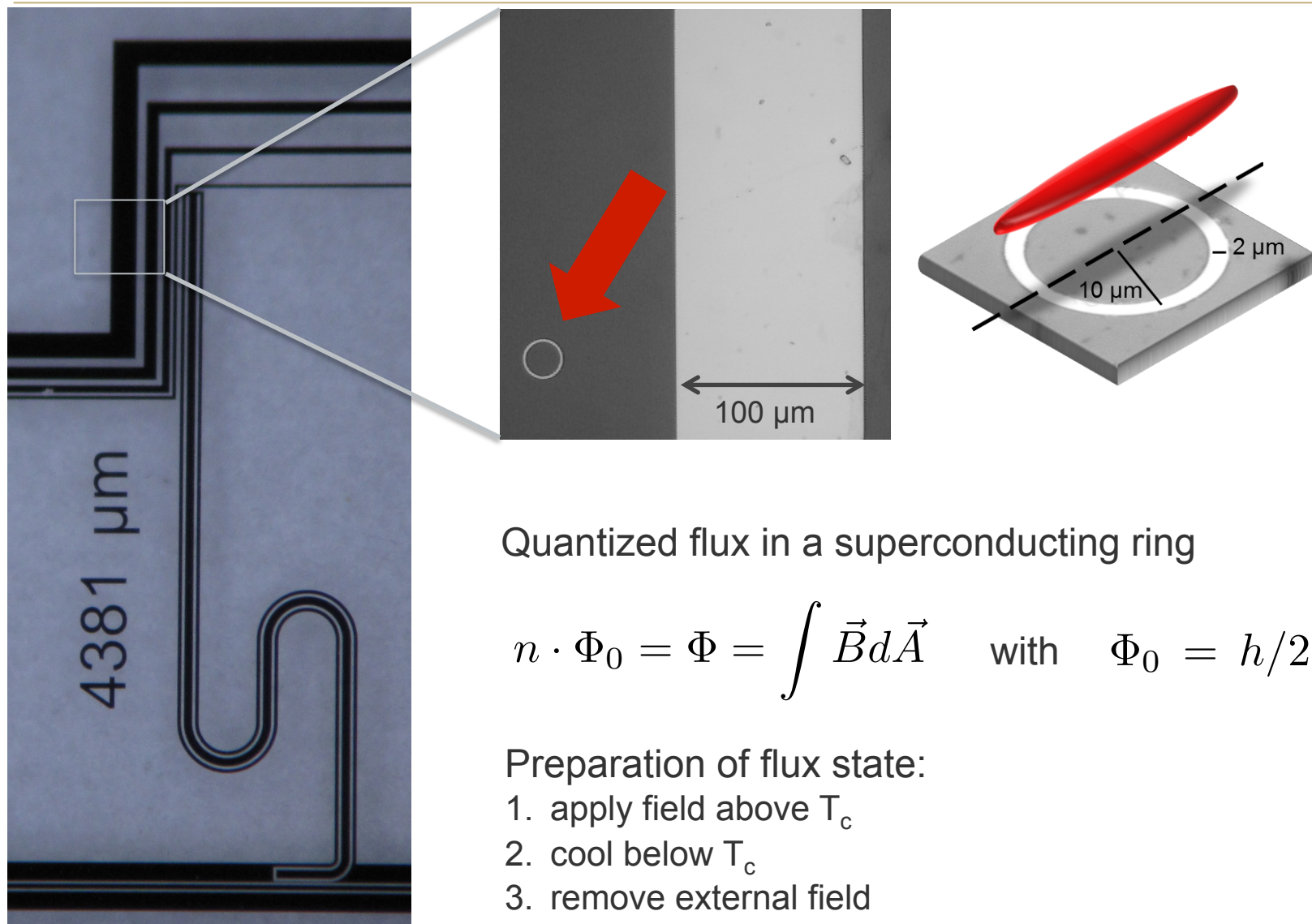


Hattermann et al,
Phys. Rev. A **86**, 022511 (2012)

Inversion of the electric field when cooling the chip to cryogenic temperatures:
Chan, Siercke, Hufnagel, Dumke, PRL **112**, 026101 (2014)



Superconducting ring



Quantized flux in a superconducting ring

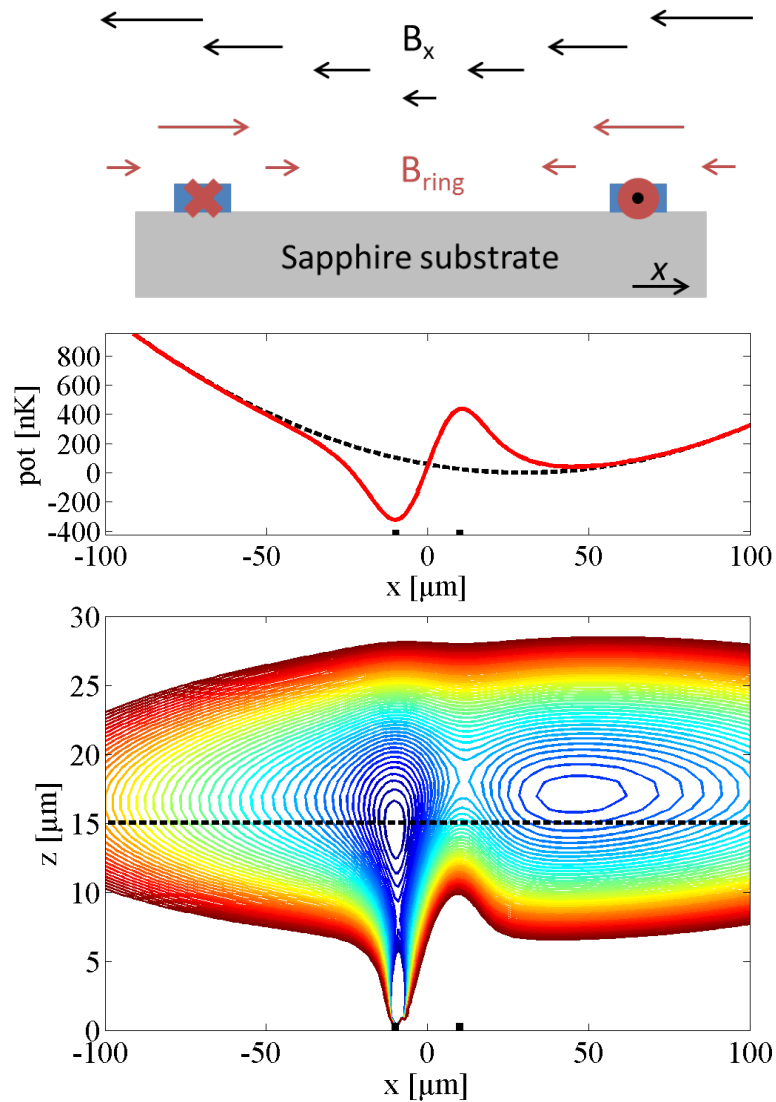
$$n \cdot \Phi_0 = \Phi = \int \vec{B} d\vec{A} \quad \text{with} \quad \Phi_0 = h/2e$$

Preparation of flux state:

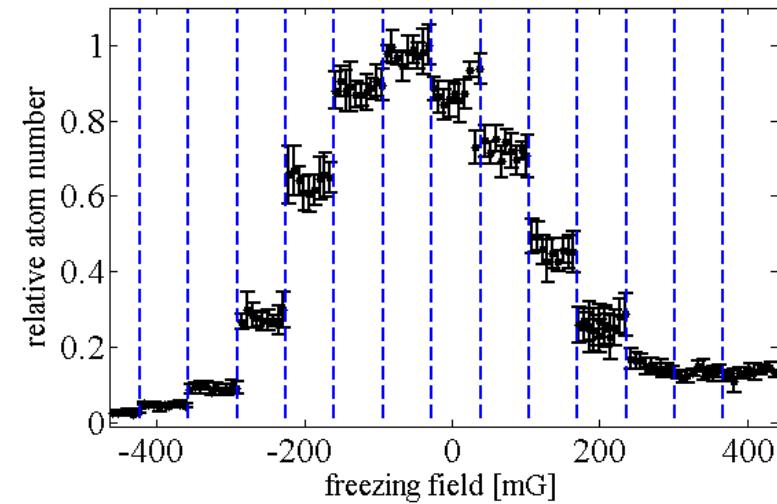
1. apply field above T_c
2. cool below T_c
3. remove external field



Mapping the flux state of the ring to atomic clouds



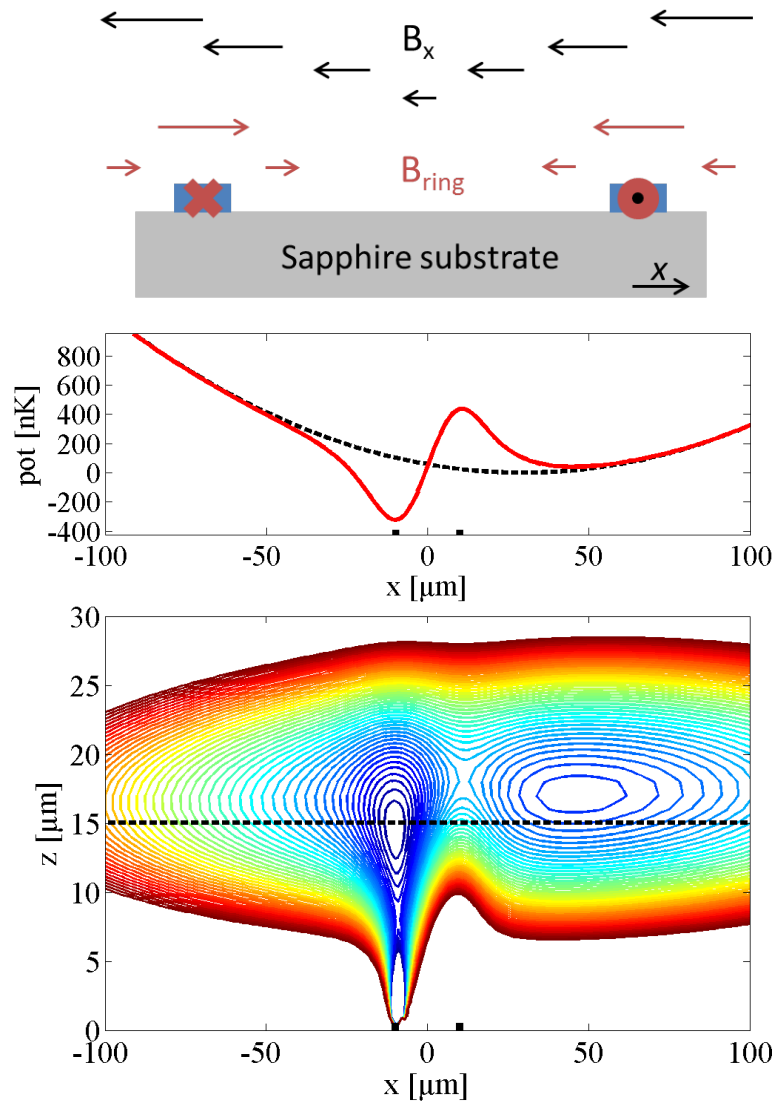
Total atom number after
1s holding time



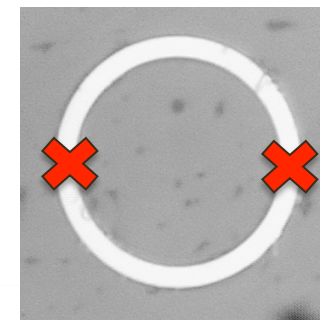
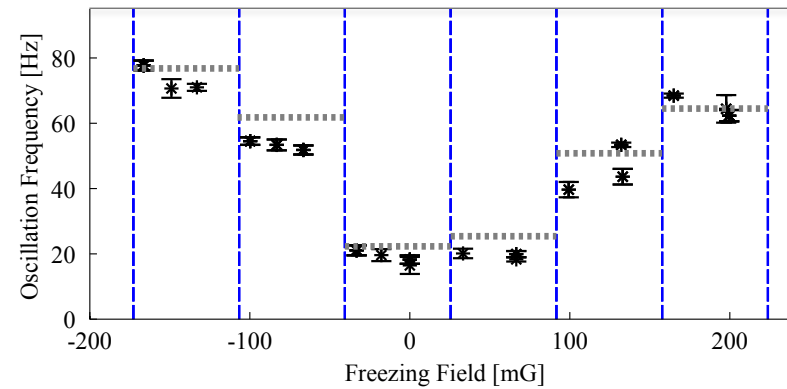
Weiss et al., PRL 114, 113003 (2015)



Mapping the flux state of the ring to atomic clouds



Dipole oscillation frequency
in the left well



SQUID



Cold-atoms & superconductors

Helge Hattermann
Patrizia Weiß
Lőrinc Sárkány
Florian Jessen

In collaboration with the
solid state physics group of
R. Kleiner & D. Kölle

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DFG, EC
BW Stiftung, Zeiss Stiftung

Rydberg atoms

Florian Karlewski
Markus Mack
Jens Grimmel
Nóra Sándor

Single atom detection

Andreas Günther
Peter Federsel
Carola Rogulj
Tobias Menold

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