

# Quantum Nanophotonics with Quantum Dots In Photonic Crystals

Benasque Workshop, July 2014

Peter Lodahl, Niels Bohr Institute,  
University of Copenhagen, Denmark

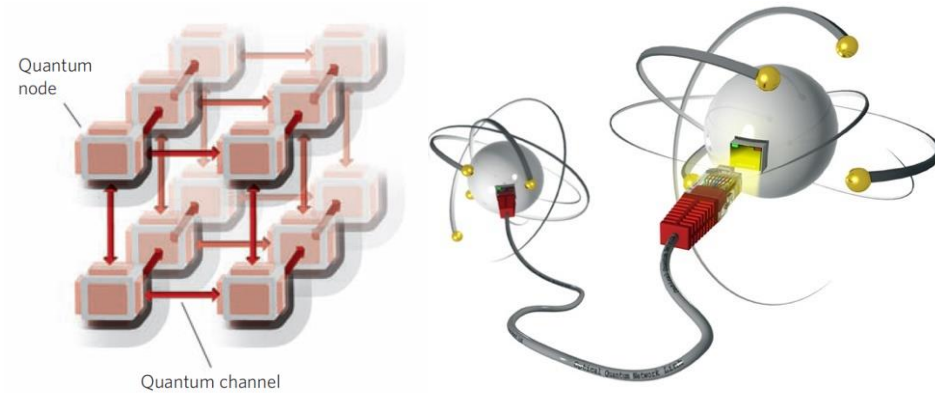
Quantum Photonics Group

[www.quantum-photonics.dk](http://www.quantum-photonics.dk)

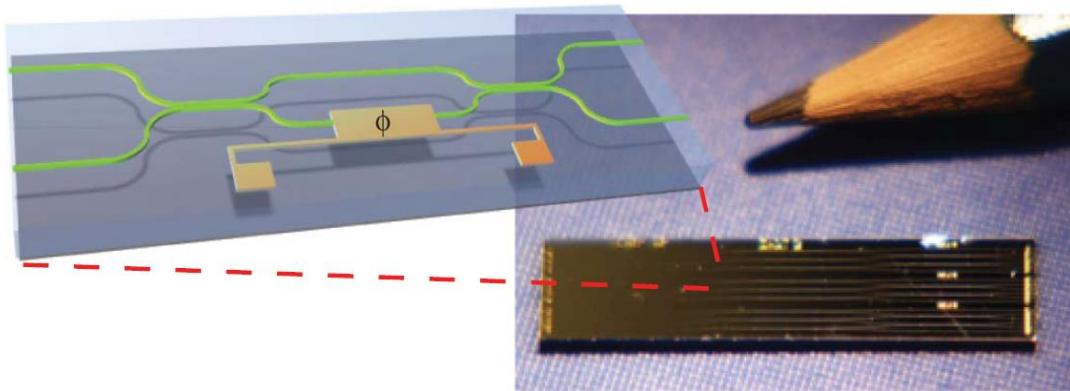


# Photonic Quantum Networks

Outstanding challenge in quantum physics:  
The scaling of small quantum systems into large architectures



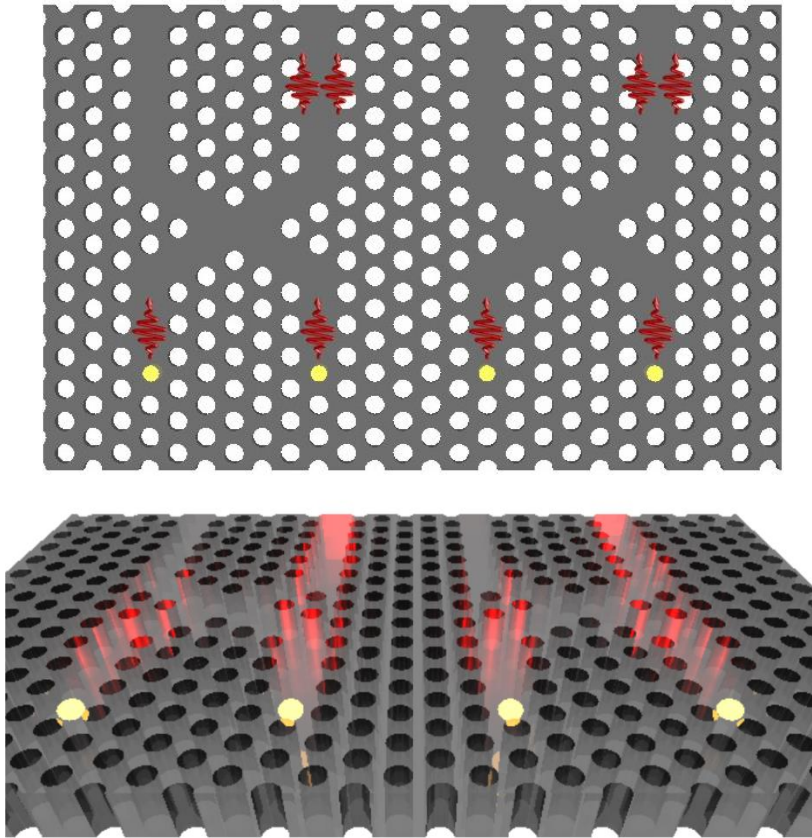
Kimble, Caltech & Rempe, Munich



Integrated photonic circuits:  
Stable and easy operation of photonic networks

Bristol, Oxford, Queensland,...

# Photonic Crystal Quantum Circuits with On-Chip Quantum Emitters



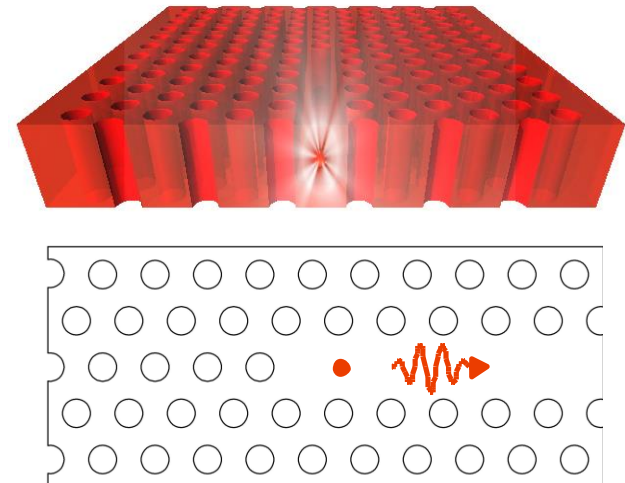
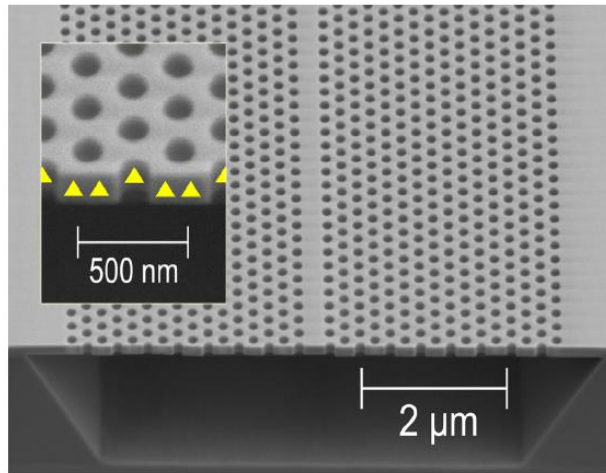
(Stanford, Munich, Zurich, Cambridge,  
Sheffield, Eindhoven, Copenhagen, ...)

- Deterministic single-photon sources on chip (quantum dots)
  - Tailor light-matter interaction strength
  - High-efficiency channeling of photons to a single mode
- On-chip quantum-information processing and computing

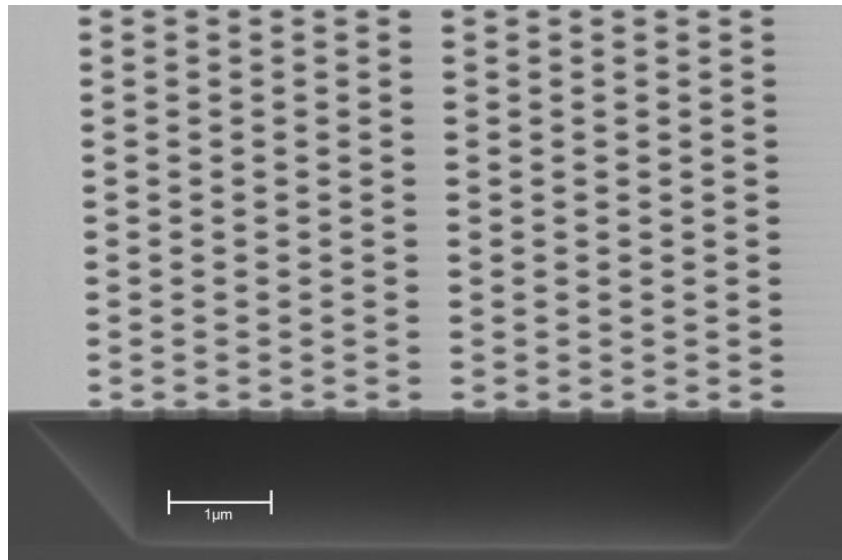


# Outline

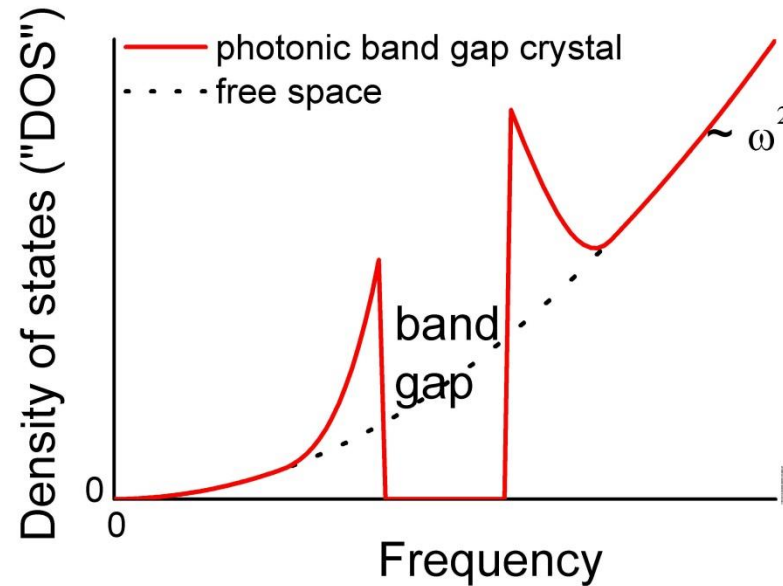
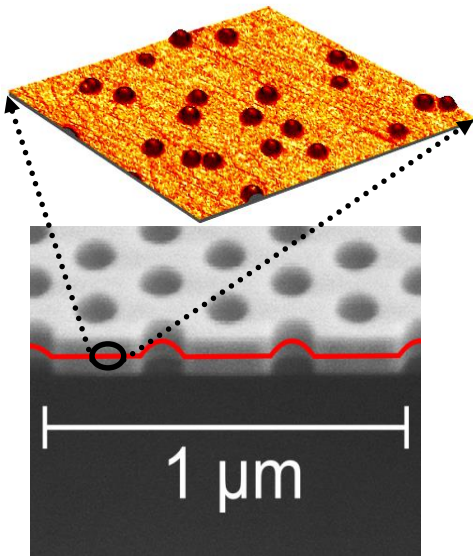
- All solid-state quantum optics with quantum dots in photonic crystals.
- Mesoscopic quantum optics effects.
- Role of fabrication imperfections.



# Controlling Light-Matter Interaction with Photonic Crystals



# Control of Spontaneous Emission with Photonic Crystals



Inhibited (enhanced) spontaneous emission rate in band gap (at band edge)

Yablonovitch, Phys. Rev. Lett. 58, 2059 (1987).

Lodahl, van Driel, Nikolaev, Irman, Overgaag, Vanmaekelberg & Vos, Nature 430, 654 (2004).

# The Local Density of Optical States

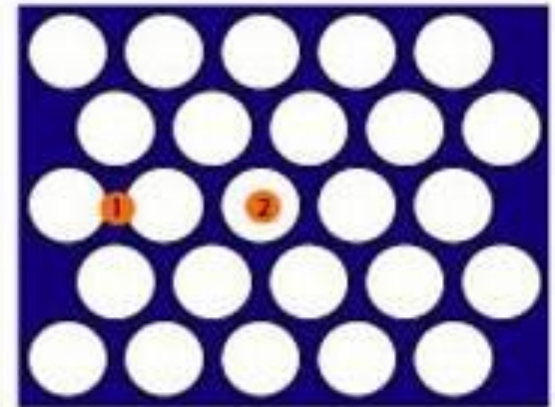
The local light-matter coupling strength is determined by the projected local density of states (LDOS)

$$\rho(\omega, \vec{r}) = \sum_n \int_{1BZ} d^3\vec{k} \left| \vec{e}_{\vec{d}} \cdot \vec{E}_{n,\vec{k}}(\vec{r}) \right|^2 \delta(\omega - \omega_n(\vec{k}))$$

The decay rate of single emitters is proportional to the LDOS

$$\gamma_{rad}(\omega, \vec{r}) = \frac{\pi\omega}{3\hbar\epsilon_0} d^2 \times \rho(\omega, \vec{r})$$

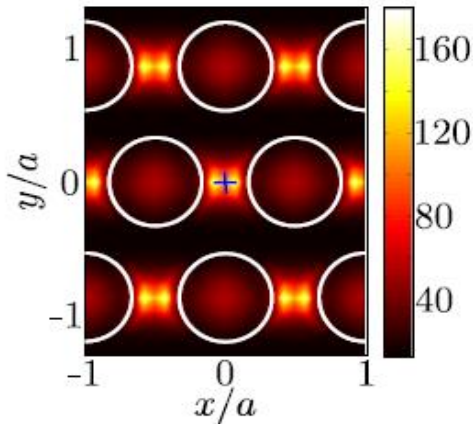
LDOS can be mapped by employing single emitters with known optical properties



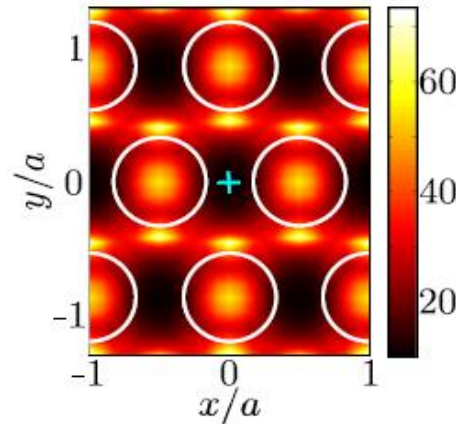
# Mapping the LDOS of a photonic crystal

Calculated spatial variation of the inhibition factor for an ideal photonic crystal

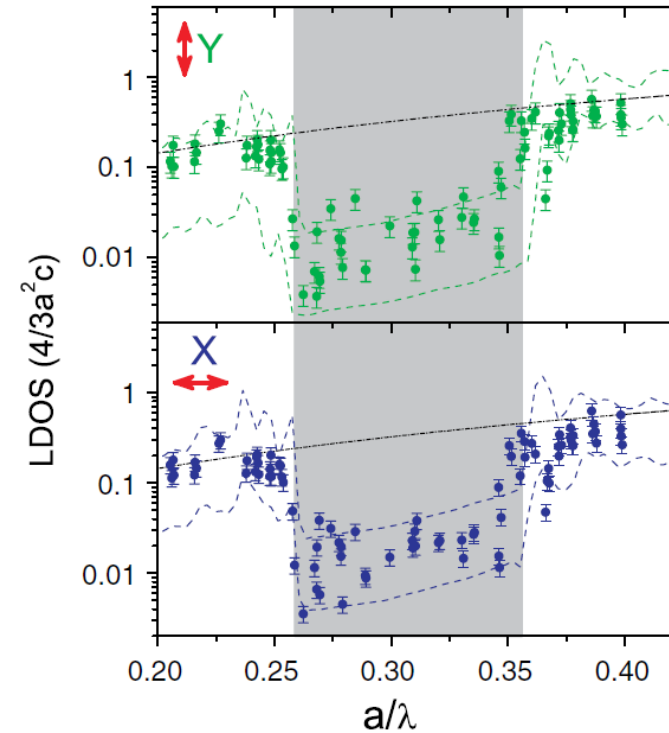
X dipole



Y dipole



Fix lattice wavelength and vary lattice constant  
→ LDOS frequency map



**x70 inhibition of spontaneous emission rate observed**

Wang, Stobbe & Lodahl, Phys. Rev. Lett. 107, 167404 (2011).

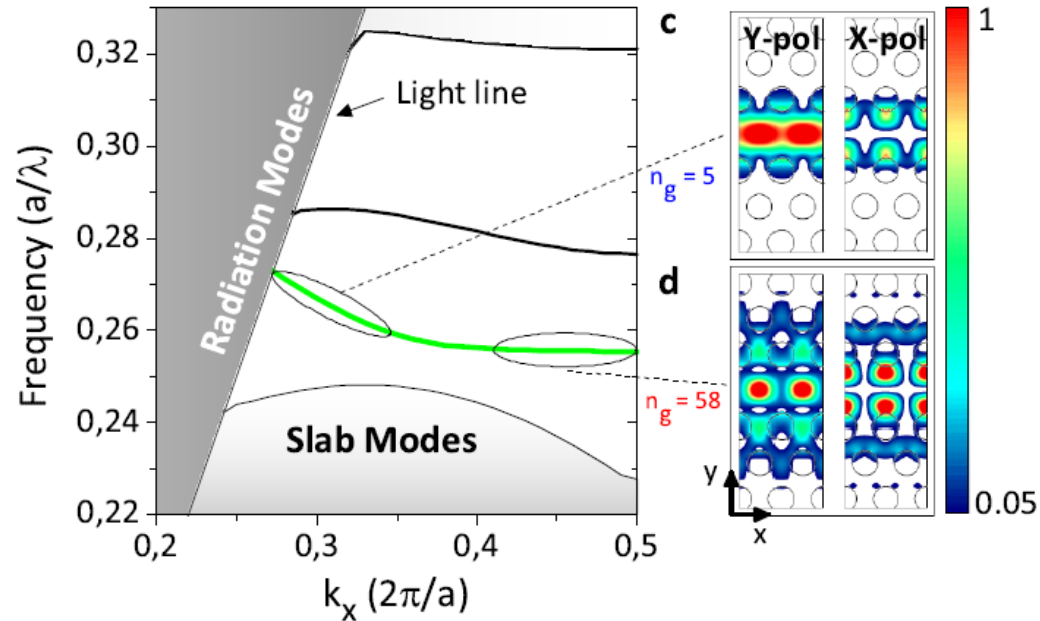
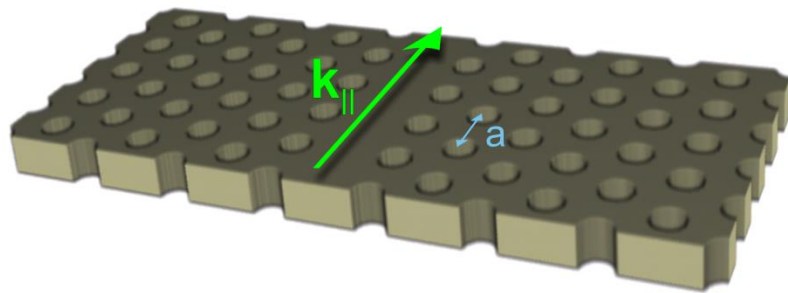
**Theory:** Koenderink, Kafesaki, Soukoulis & Sandoghdar, J. Opt. Soc. Am. B 23, 1196 (2006).



Niels Bohr Institutet



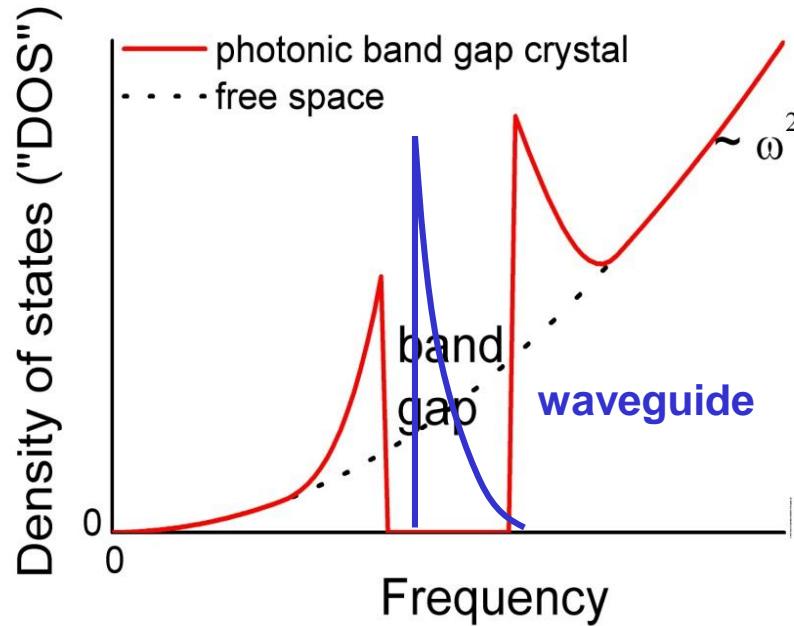
# Highly efficient photonic-crystal waveguide single-photon source



Single-photon coupling efficiency:

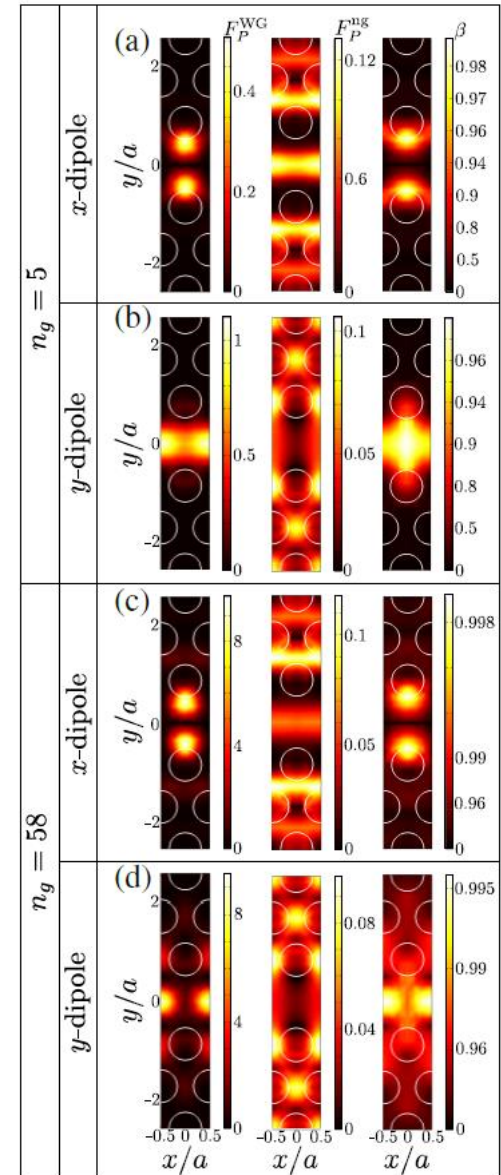
$$\beta = \frac{\gamma_{\text{wg}}}{\gamma_{\text{wg}} + \gamma_{\text{rad}} + \gamma_{\text{nrad}}}$$

# Density of States and Purcell Factor

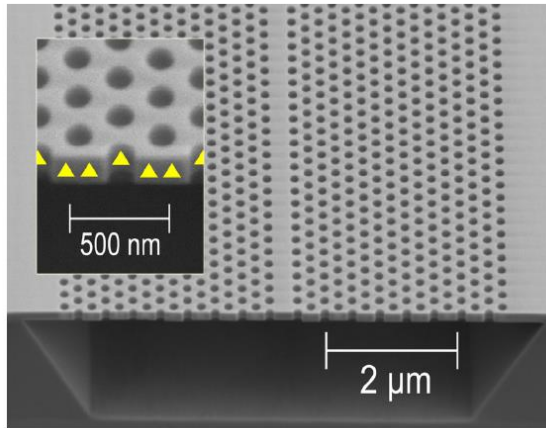


$$F_P(\vec{r}_{\text{QD}}) = \frac{\gamma_{\text{wg}}}{\gamma_{\text{hom}}} = \frac{3\pi c^3 a n_g}{n \omega^2 c} \times \left| \vec{f}(\vec{r}_{\text{QD}}) \cdot \vec{e}_{\text{QD}} \right|^2$$

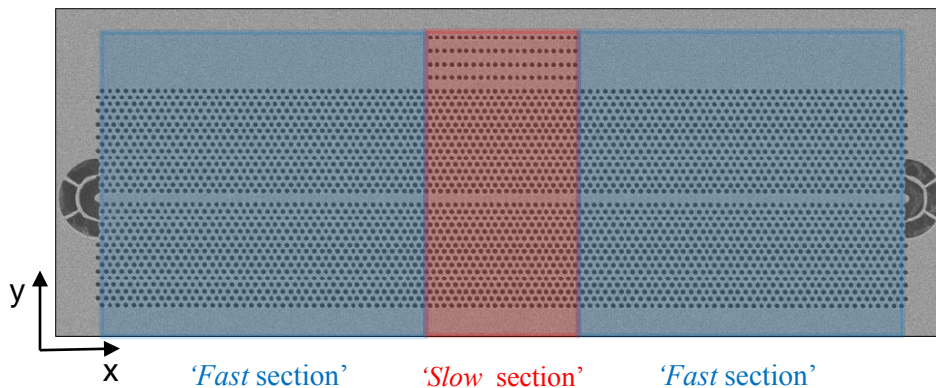
V.S.C. Manga Rao and S. Hughes, Phys. Rev. B 75, 205437 (2007).  
 Lodahl, Mahmoodian & Stobbe, submitted to Rev. Mod. Phys. (2013).  
 arXiv:1312.1079



# Engineered samples for efficient outcoupling



PC waveguide with a single layer of quantum dots embedded in the center of the membrane

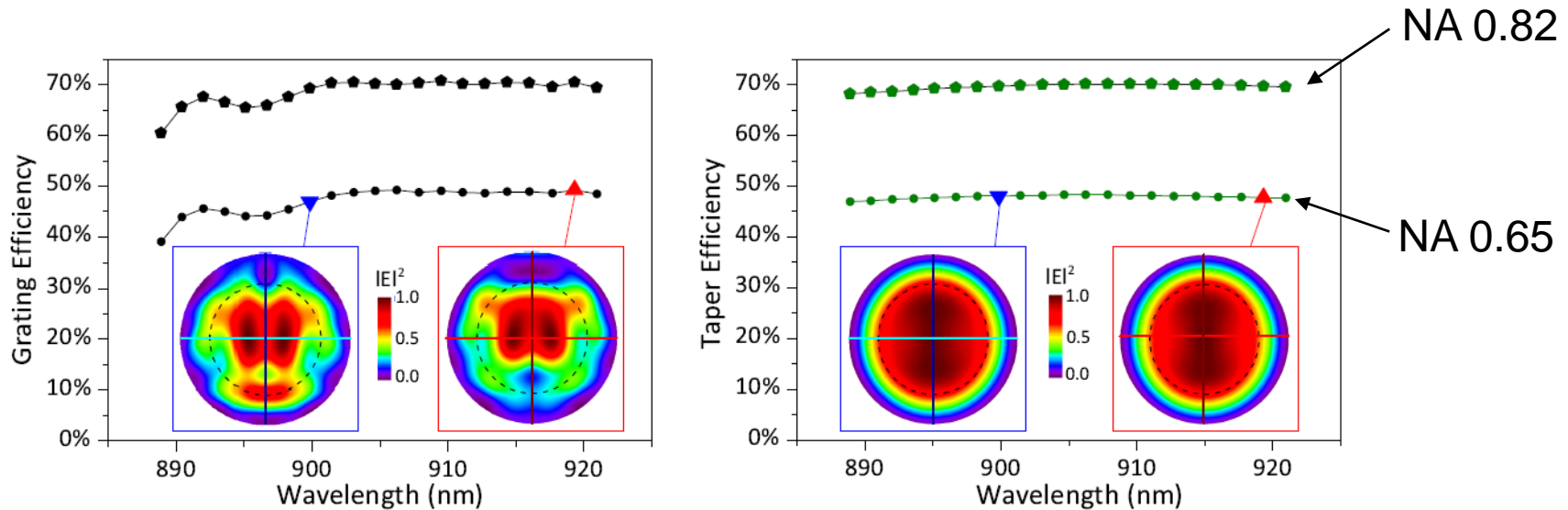
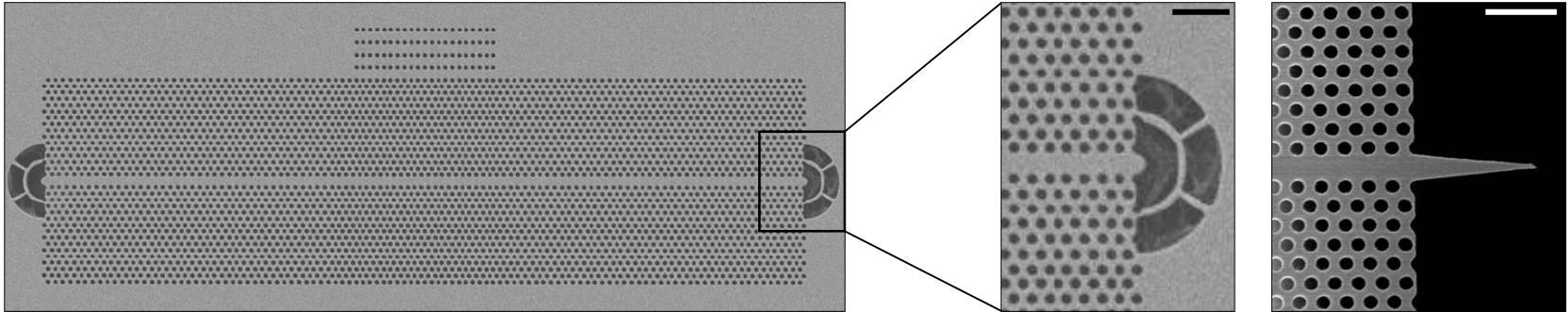


Lattice constant tailored for efficient outcoupling

$$a_f = 1.07 \cdot a_s$$

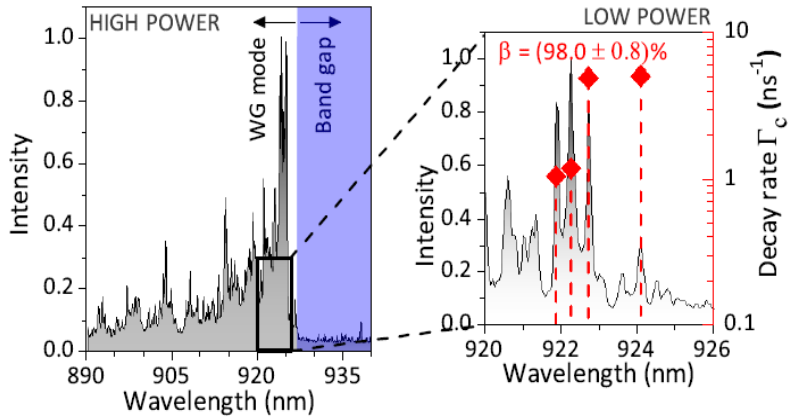
+ four row long transition region between slow and fast sections

# Outcoupling efficiency



~ 70% out coupling efficiency  
→ can be improved further by optimum design

# Near-unity coupling efficiency

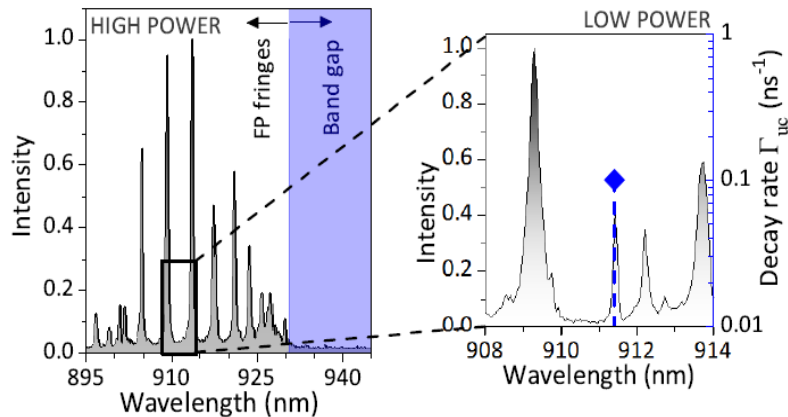


Efficiently coupled quantum dot in the slow-light regime of a waveguide:

$$\gamma_{\text{coup}} = 5.0 \text{ ns}^{-1}$$

Weakly coupled quantum dot in between two Fabry-Perot resonances:

$$\gamma_{\text{un-coup}} \leq 0.1 \text{ ns}^{-1}$$



Combining these measurements leads to:  $\beta = 98.0 \pm 0.8 \%$

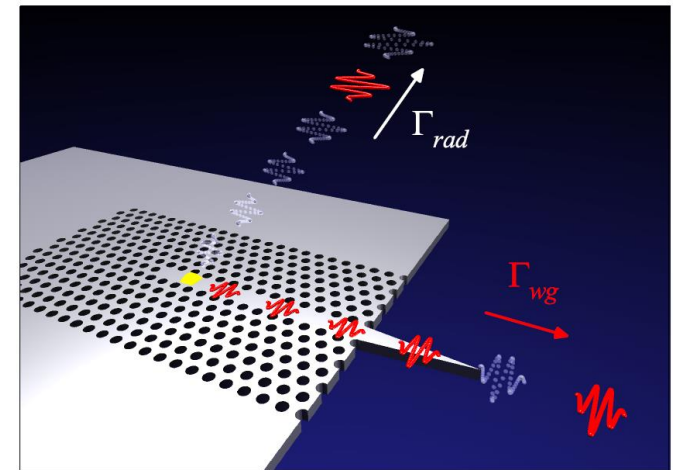
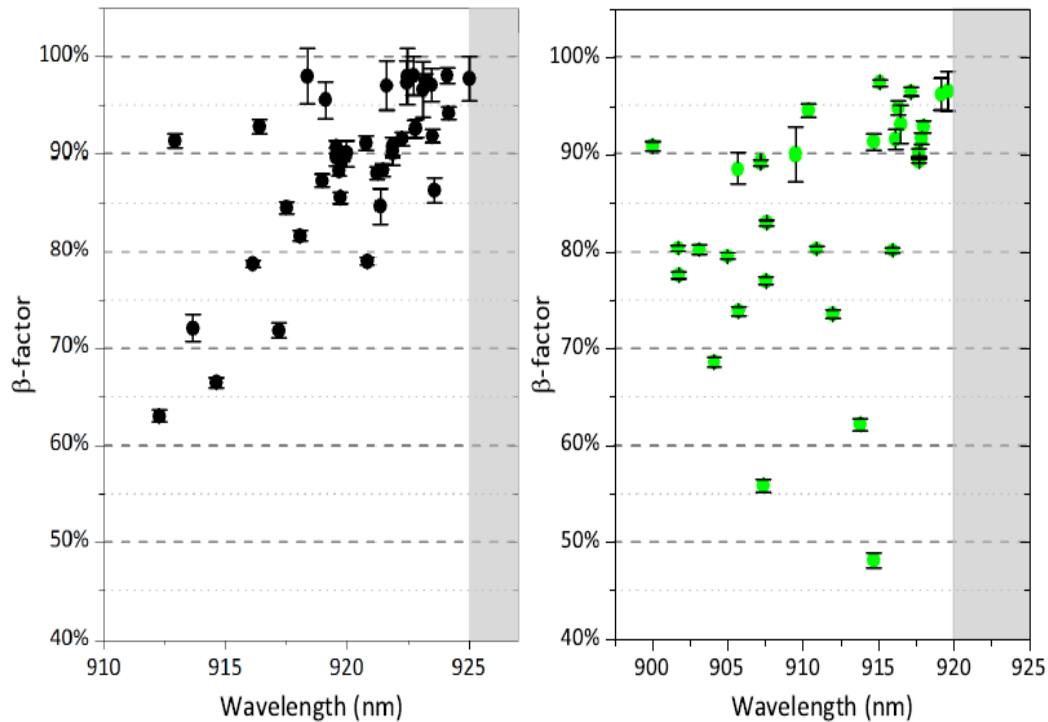
Lund-Hansen, Stobbe, Julsgaard, Thyrrestrup, Sunner, Kamp, Forchel & Lodahl,  
Phys. Rev. Lett. 101, 113903 (2008).

Arcari, Sollner, Javadi, Hansen, Liu, Thyrrestrup, Lee, Song, Stobbe & Lodahl, arXiv:1402.2081.



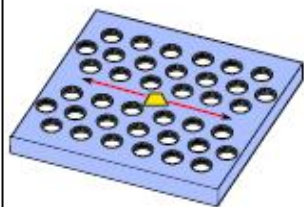
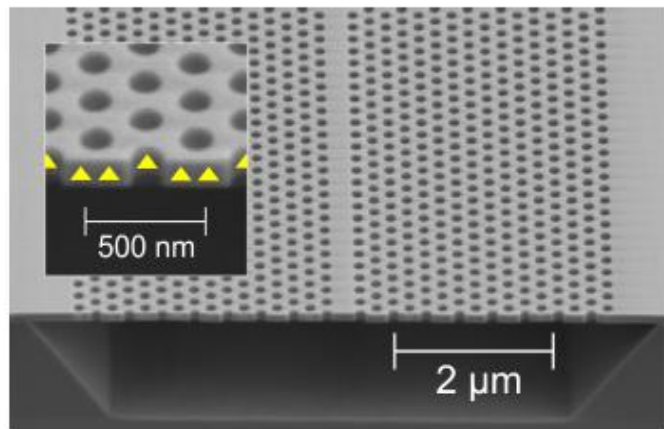
# Statistics of $\beta$ -factor measurements

Near unity  $\beta$ -factors are observed for many quantum dots over a wide spectral range



# Comparison to other methods

(a) Photonic-crystal waveguide



$$\beta^e = 0.98 \dagger$$

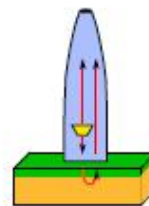
$$F_P^e = 5 \dagger$$

$$\beta^t \rightarrow 1 \ddagger$$

$$F_P^t \rightarrow \infty \ddagger$$

$\dagger$ (Arcari *et al.*, 2013)  
 $\ddagger$ (Manga Rao and Hughes, 2007b)

(b) Photonic nanowire



$$\beta^e \gtrsim 0.72 \dagger$$

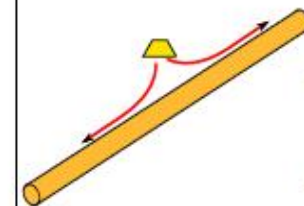
$$F_P^e = 1.5 \dagger$$

$$\beta^t \sim 0.95 \ddagger$$

$$F_P^t \sim 1.7 \ddagger$$

$\dagger$ (Claudon *et al.*, 2010)  
 $\ddagger$ (Bleuse *et al.*, 2011)

(c) Plasmonic nanowire



$$\beta^e \sim 0.7 \dagger$$

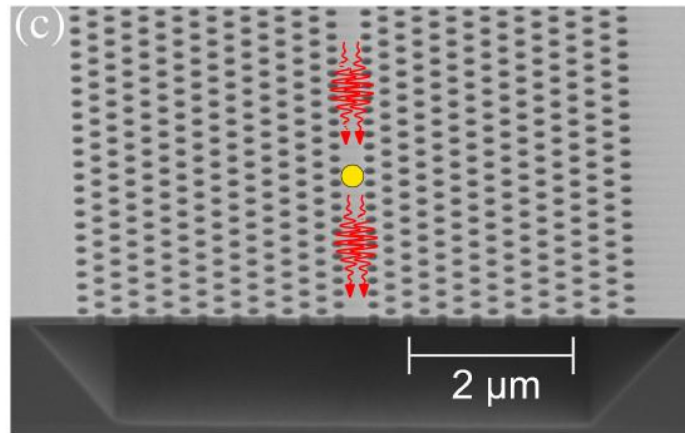
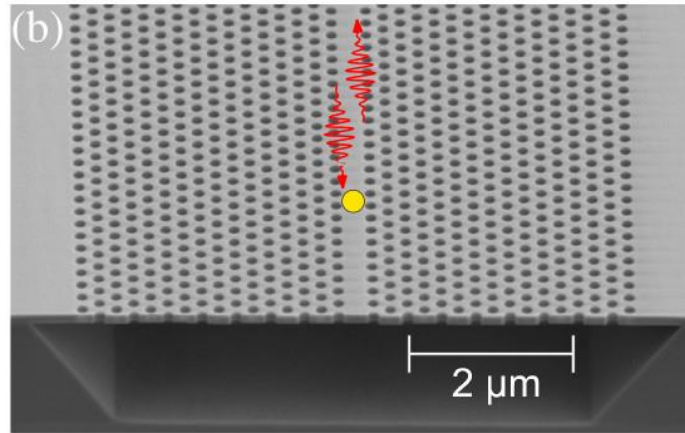
$$F_P^e = 2.5 \dagger$$

$$\beta^t \sim 1 \ddagger$$

$$F_P^t \sim 500 \ddagger$$

$\dagger$ (Akimov *et al.*, 2007)  
 $\ddagger$ (Chang *et al.*, 2006)

# Few-photon nonlinearity



Single quantum dot efficiently coupled to a photonic-crystal waveguide as a nonlinear medium.

1-photon reflection coefficient:

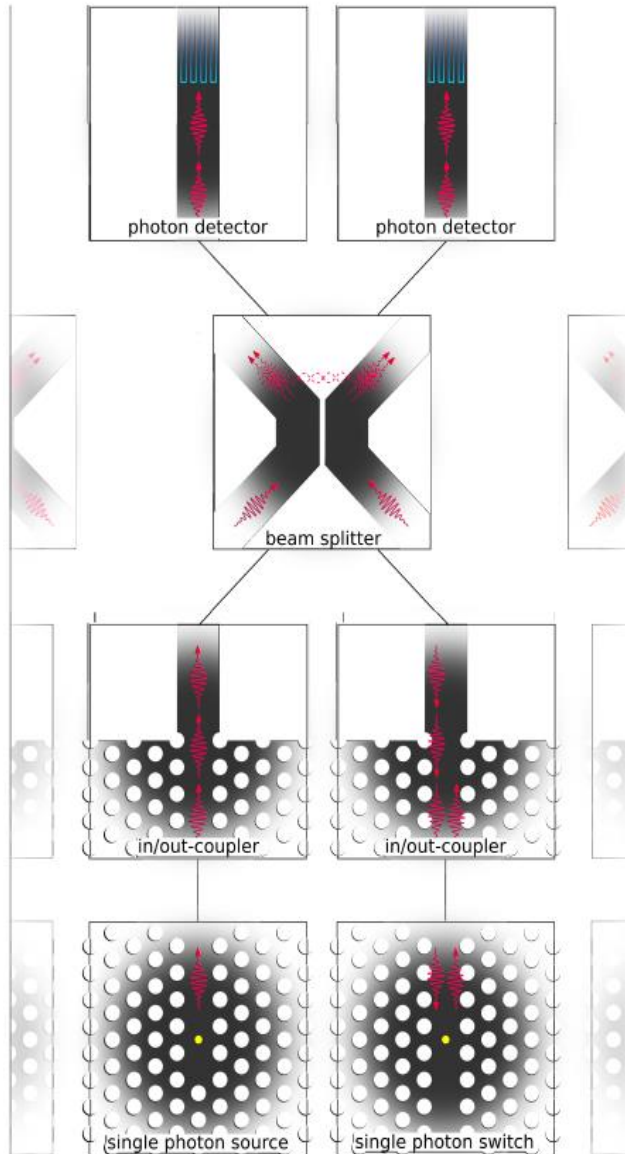
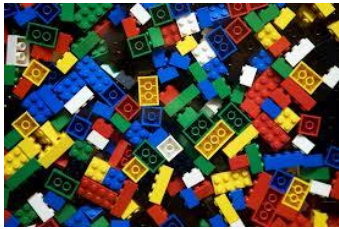
$$R \approx \frac{1}{1 + 2\gamma_{\text{dp}}/\gamma} \beta^2 \quad \frac{\gamma_{\text{dp}}}{\gamma} \approx 0.2$$

Applications:

Single-photon switch and quantum-phase gates



# Building blocks for integrated photonic circuits



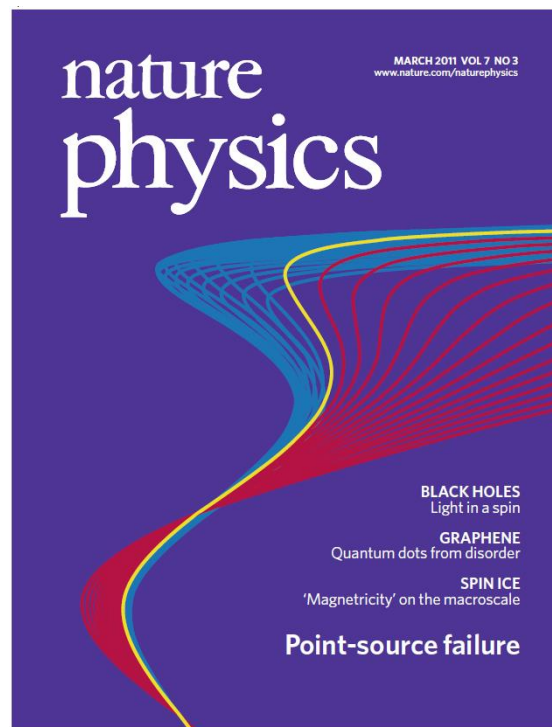
On-chip single-photon detectors based on superconducting nanowires

Photon circuits based on dielectric waveguides

Efficient coupling to dielectric waveguides for long-range propagation

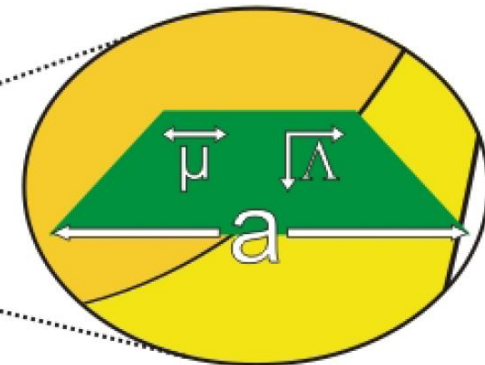
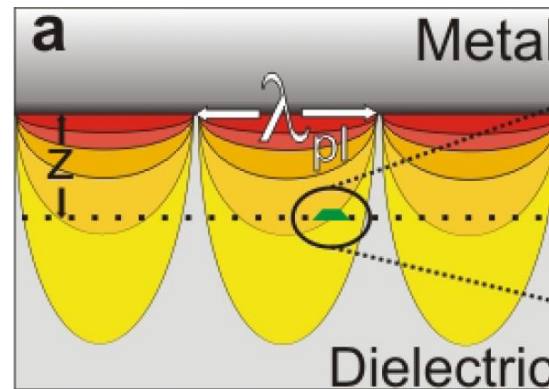
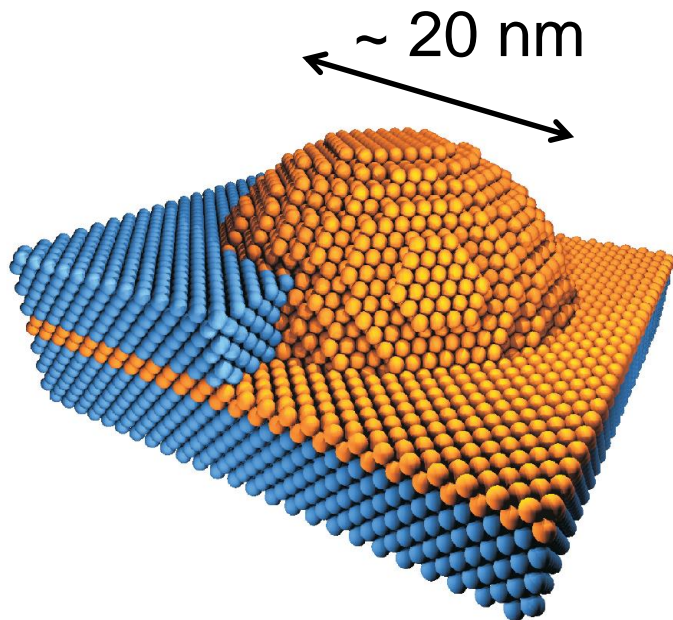
Single-photon source and nonlinearity

# Mesoscopic Effects with Quantum Dots in Photonic Nanostructures



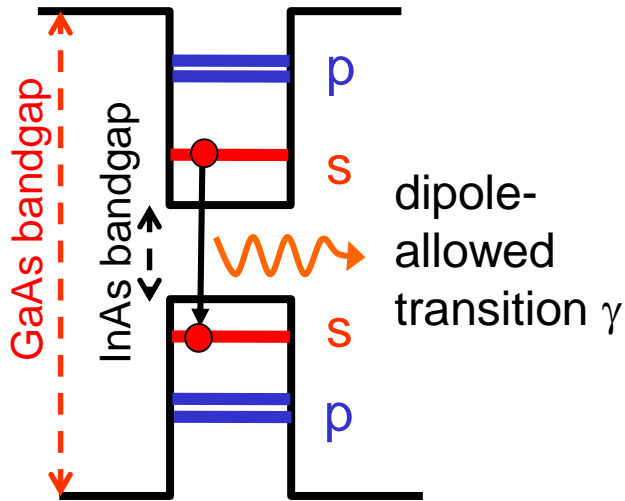
# Break-down of dipole approximation for quantum dots coupled to plasmons

Mesoscopic dimensions of quantum dots  
→ traditional point dipole description may not apply



Strong field gradients at metal interface due to coupling to surface plasmon polaritons

# Modified excitation of plasmons



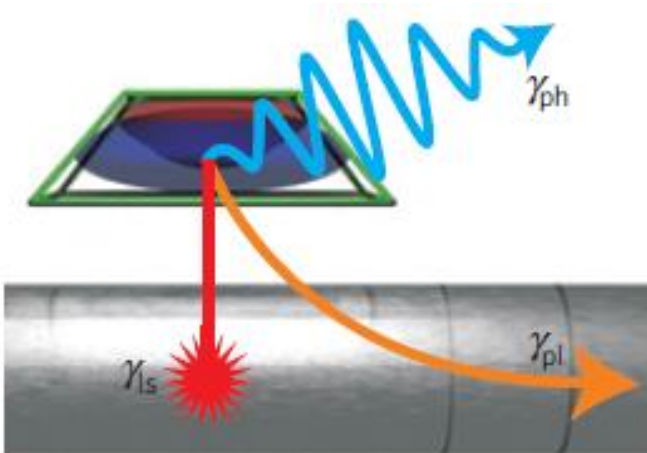
$$\hat{H}_I(\vec{r}) \propto \vec{p} \cdot \vec{A}(\vec{r})$$

$$\hat{A}_j(\vec{r}) \approx \hat{A}_j(\vec{r}_0) + \sum_n (\vec{r} - \vec{r}_0)_n \left[ \nabla_n \hat{A}_j \right]_{\vec{r}_0}$$

Rate of decay to plasmons

$$\gamma_{pl} = \gamma_{pd} + \xi_{me}$$

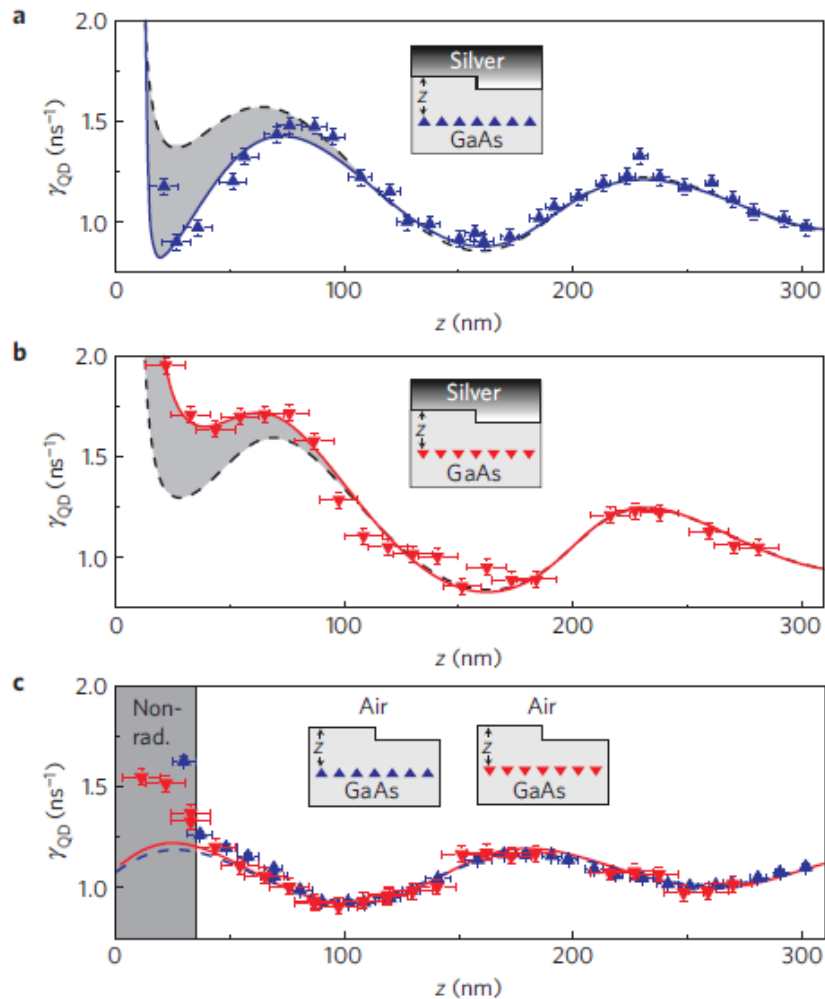
$\swarrow$  point dipole       $\downarrow$  mesoscopic  
 (i.e. magnetic dipole and electric quadrupole)



Mesoscopic contribution can either add or subtract depending on geometry



# Observation of break down of dipole approximation



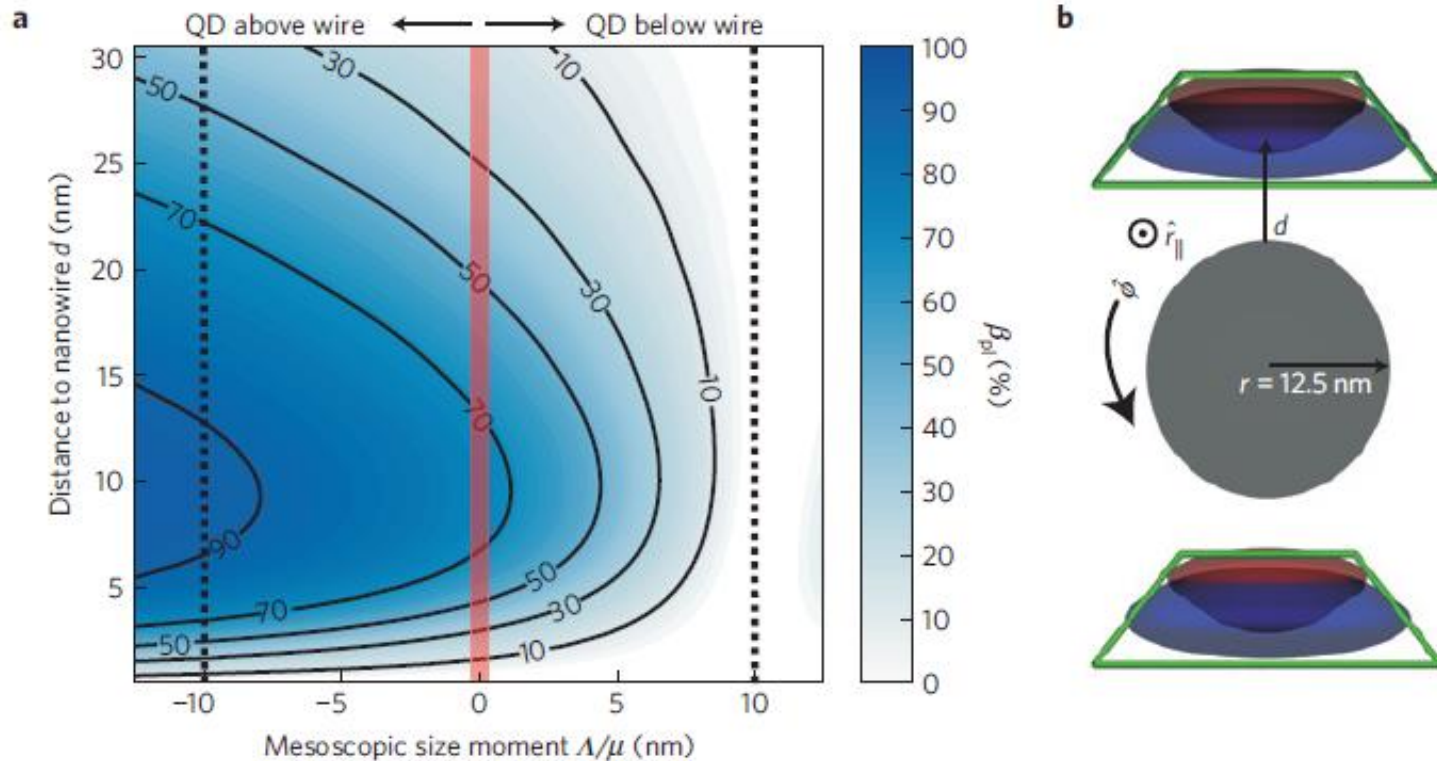
Direct structure:  
suppressed excitation  
of plasmons

Inverted structure:  
enhanced excitation  
of plasmons

Reference measurement  
before metal deposition

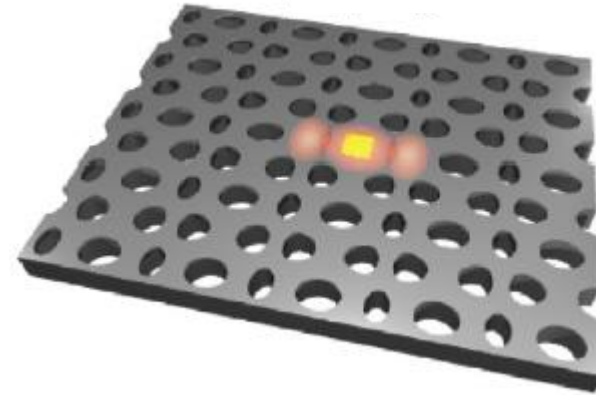
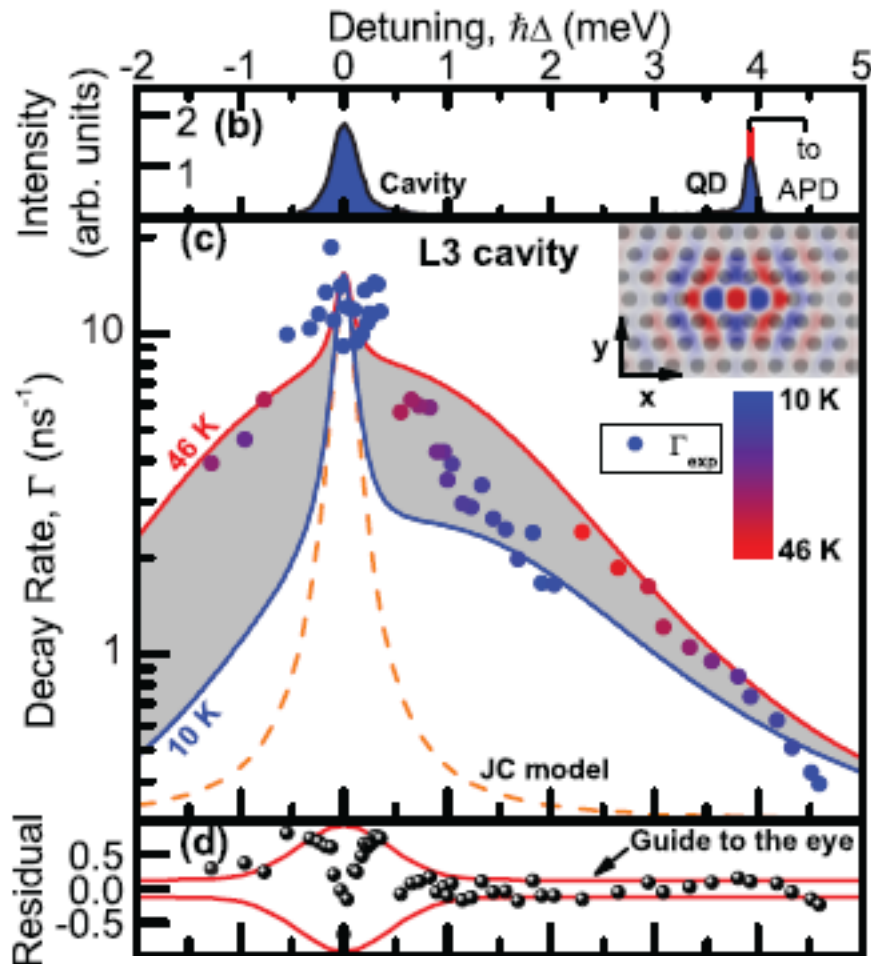
# Improving plasmon single-photon sources

Quantum dot coupled to a plasmon nanowire for efficient single-photon source



[Proposal of:  
Chang, Sørensen,  
Hemmer & Lukin,  
PRL 97 053002  
(2006)]

# Phonon-assisted Purcell enhancement in a photonic-crystal cavity

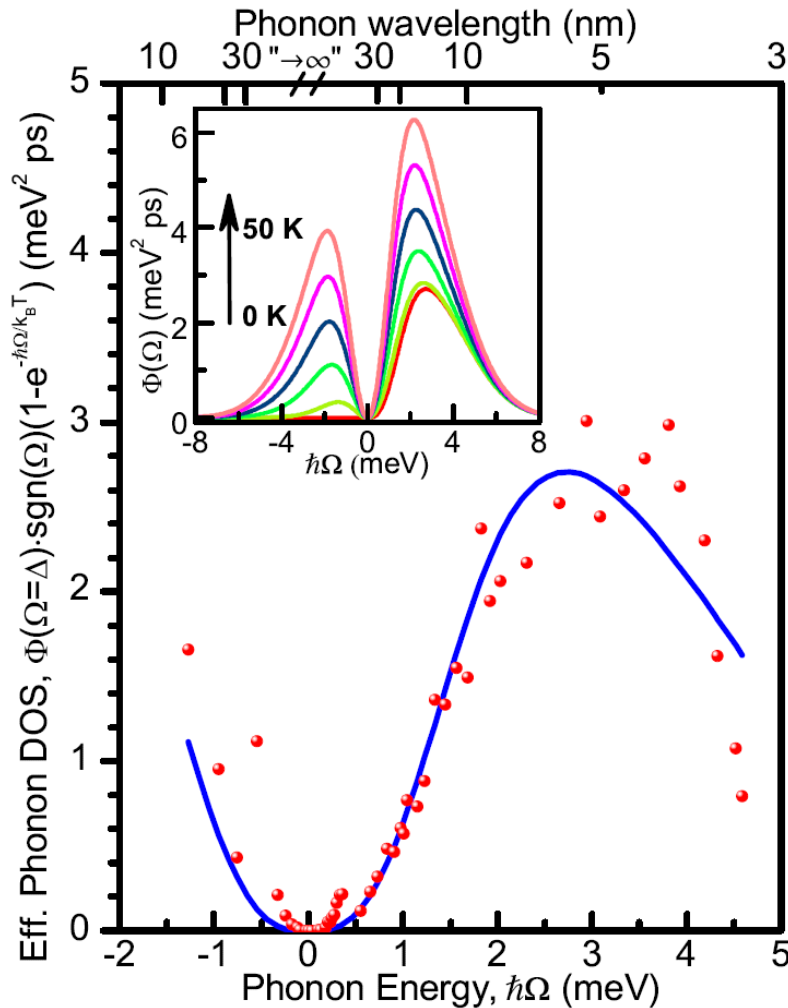


Wide bandwidth of Purcell enhancement due to coupling to phonons

**Theory:** Kaer, Nielsen, Lodahl, Jauho & Mørk, Phys. Rev. Lett. 104, 157401 (2010).  
Kaer, Nielsen, Lodahl, Jauho & Mørk, Phys. Rev. B 86, 085302 (2012).

**Exp:** Madsen, Kaer, Kreiner-Møller, Stobbe, Nysteen, Mørk, and Lodahl, Phys. Rev. B 88, 045316 (2013).

# The effective phonon density of states



Effective phonon density of states can be extracted from the QD decay rate:

$$\Gamma = \gamma + 2g^2 \frac{\gamma_{\text{tot}}}{\gamma_{\text{tot}}^2 + \Delta^2} \left[ 1 + \frac{1}{\hbar^2 \gamma_{\text{tot}}} \Phi(\Omega = \Delta) \right]$$

Probe intrinsic QD phonon dephasing process by cavity QED

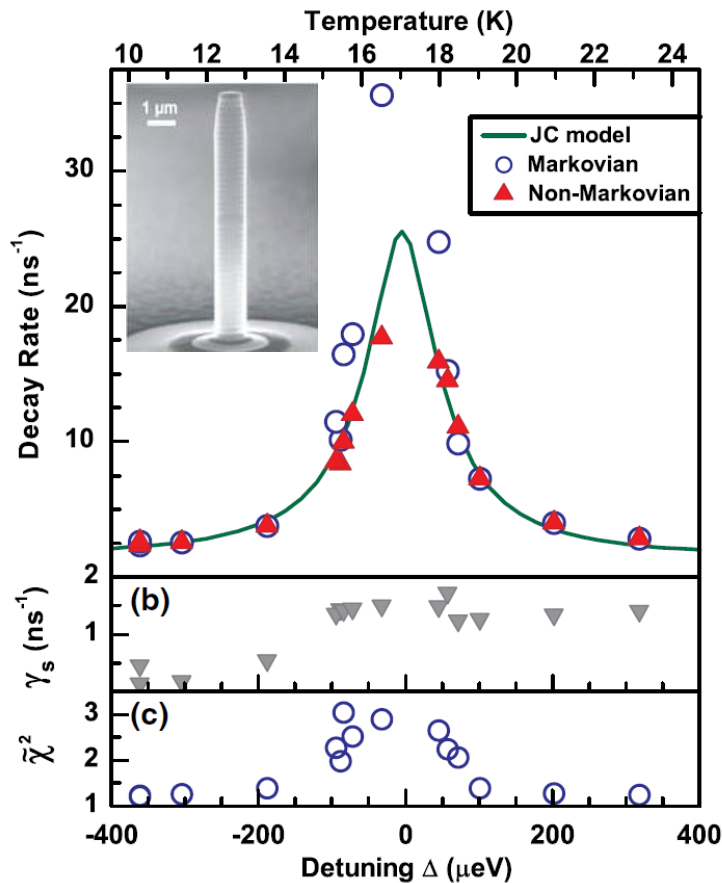
**Theory:** Kaer, Nielsen, Lodahl, Jauho & Mørk, Phys. Rev. Lett. 104, 157401 (2010).  
Kaer, Nielsen, Lodahl, Jauho & Mørk, Phys. Rev. B 86, 085302 (2012).

**Exp:** Madsen, Kaer, Kreiner-Møller, Stobbe, Nysteen, Mørk, and Lodahl, Phys. Rev. B 88, 045316 (2013).



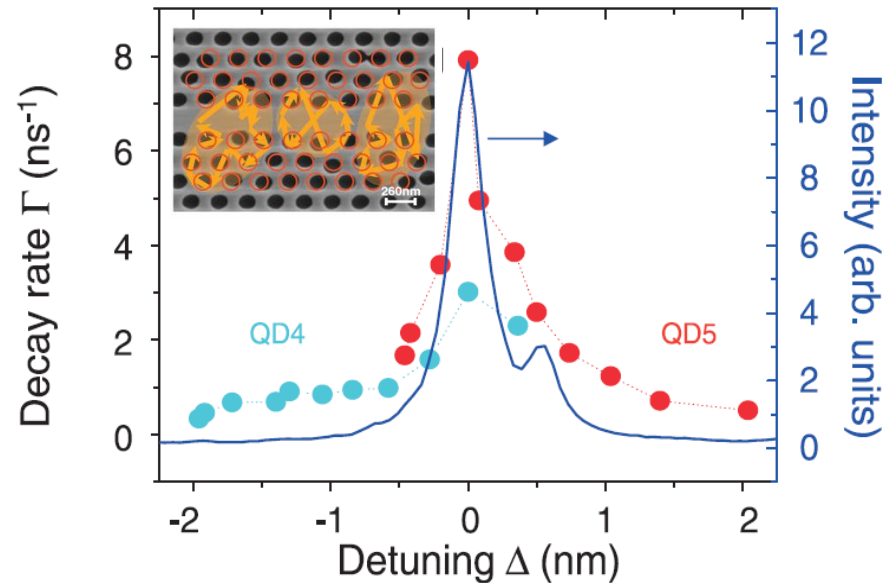
# Purcell effect in other cavities

## Micropillar cavity



Madsen, Ates, Lund-Hansen, Löffler, Reitzenstein, Forchel, and Lodahl, Phys. Rev. Lett. 106, 233601 (2011).

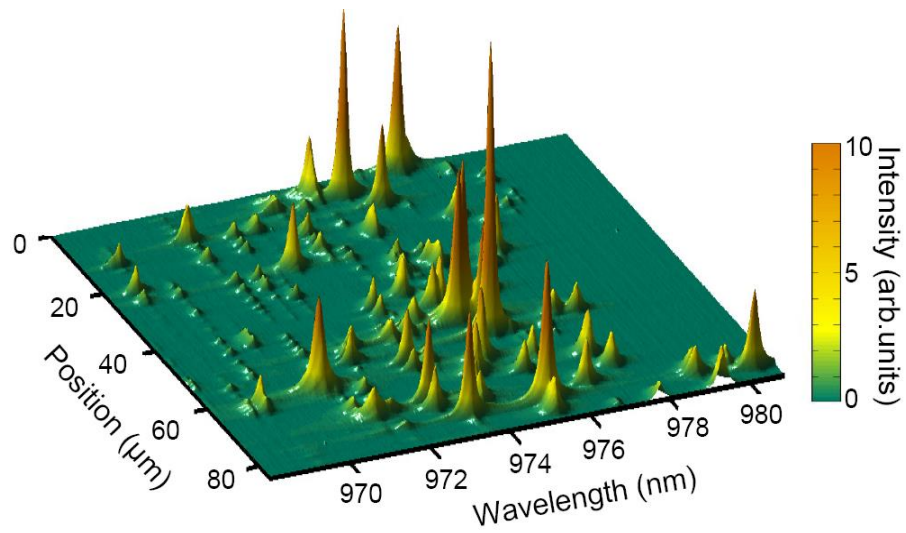
## Anderson-localized cavity



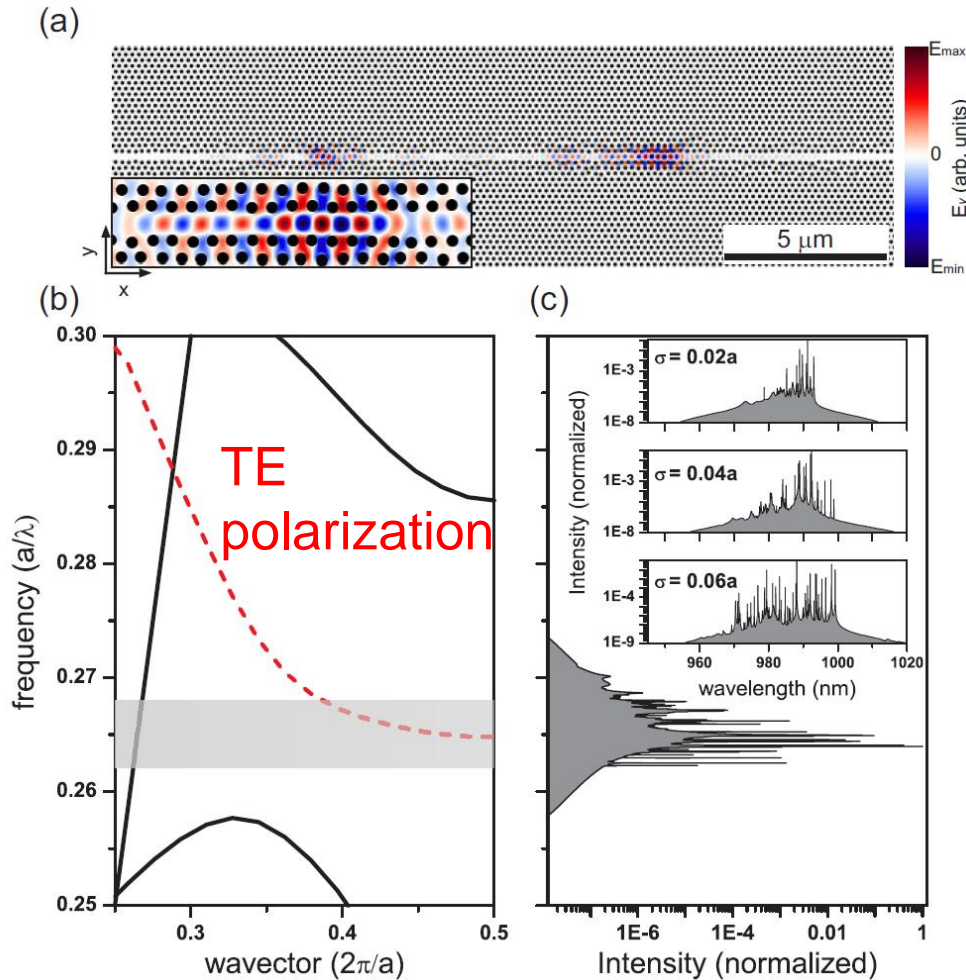
Sapienza, Thyrrstrup, Stobbe, Garcia, Smolka & Lodahl, Science 327, 1352 (2010).

Figure-of-merit for broadband Purcell:  $g^2/\gamma$

# Anderson Localization in Disordered Photonic Crystals



# Formation of 1D Anderson-localized modes



Disorder breaks up Bloch modes leading to localized states in the slow-light regime

# Adding disorder to photonic-crystal waveguides

Random disorder on position of holes

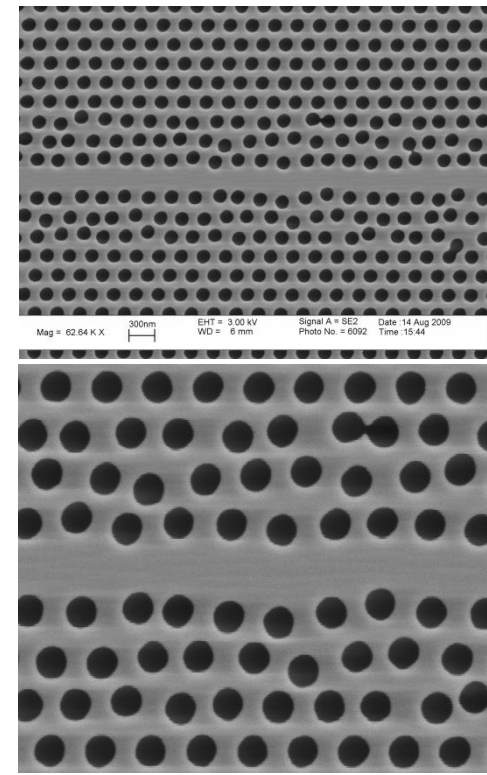
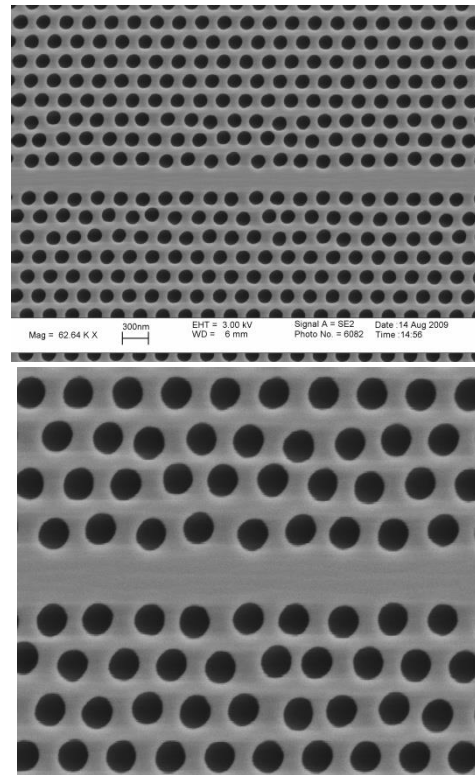
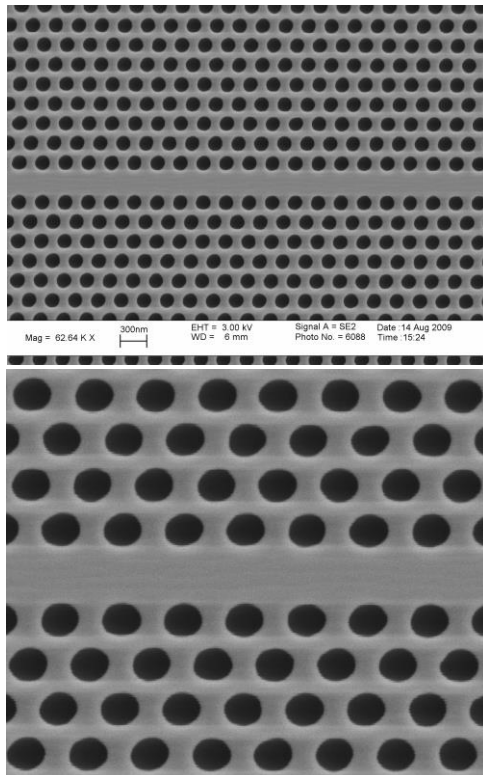
Standard deviations in percentage of the lattice constant

$\delta=0\%$

$\delta=6\%$

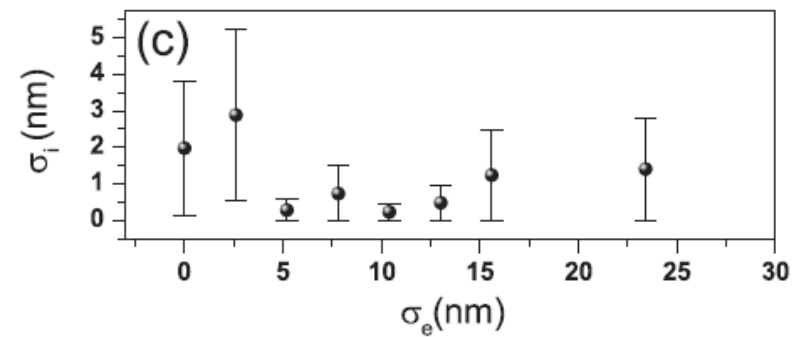
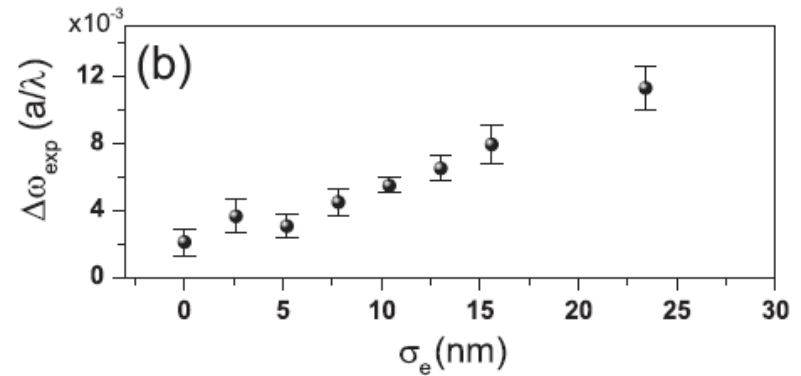
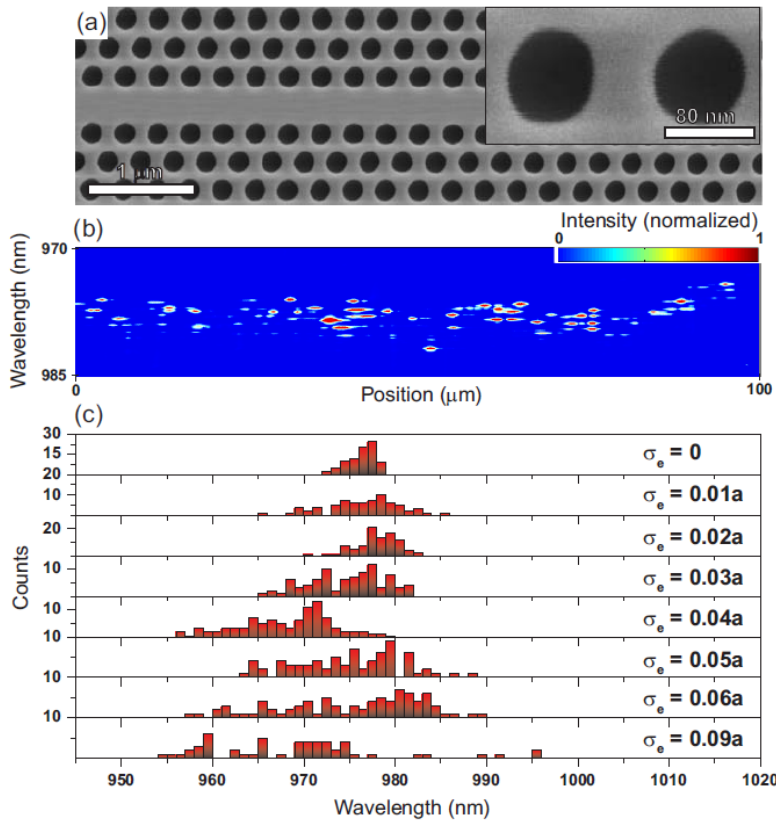
$\delta=12\%$

300nm

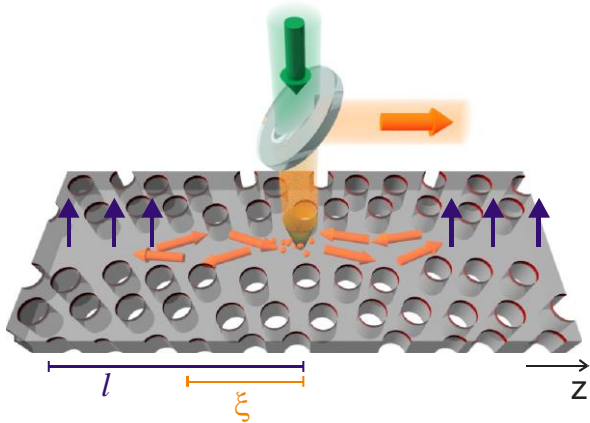


# Quantifying Intrinsic Disorder

Intrinsic disorder ( $\sigma_i$ ) can be measured from the width of the region of localized modes

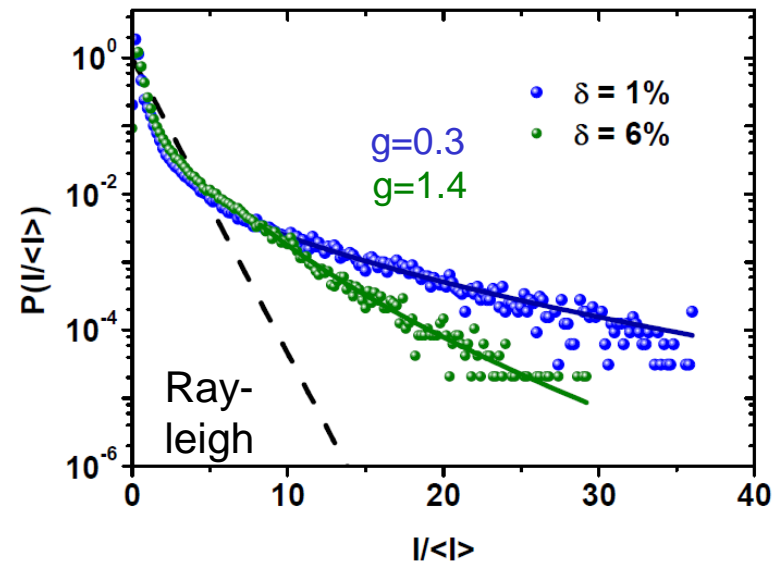
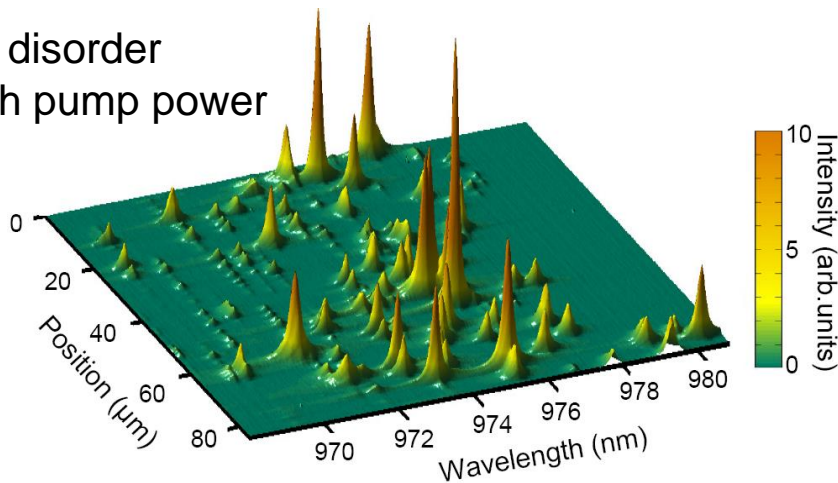


# Observation of Anderson-localized modes



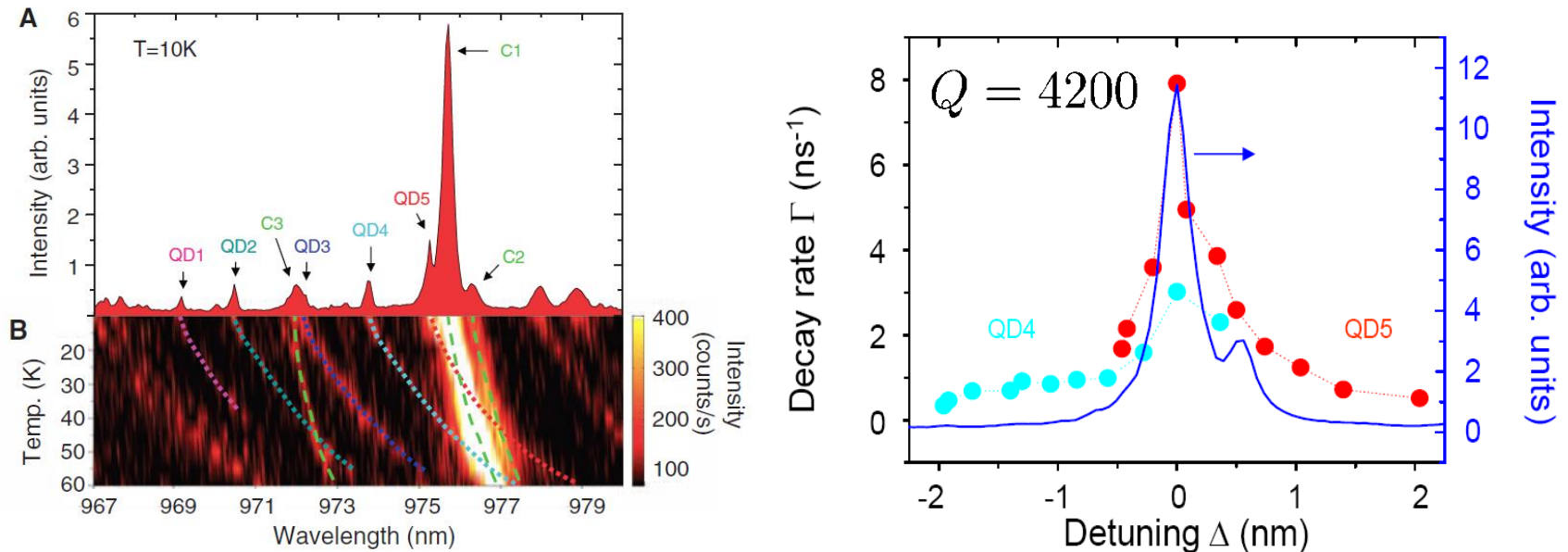
Quantum dot spectra recorded when scanning along waveguide

3% disorder  
High pump power



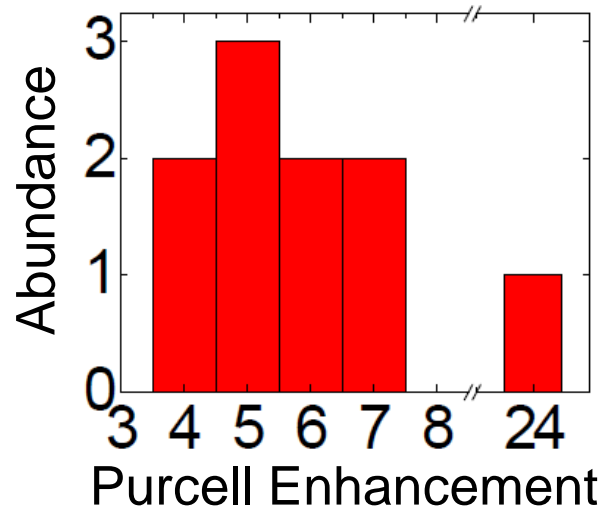
# Cavity QED with Anderson-localized modes

Low excitation power: single quantum dot lines are revealed

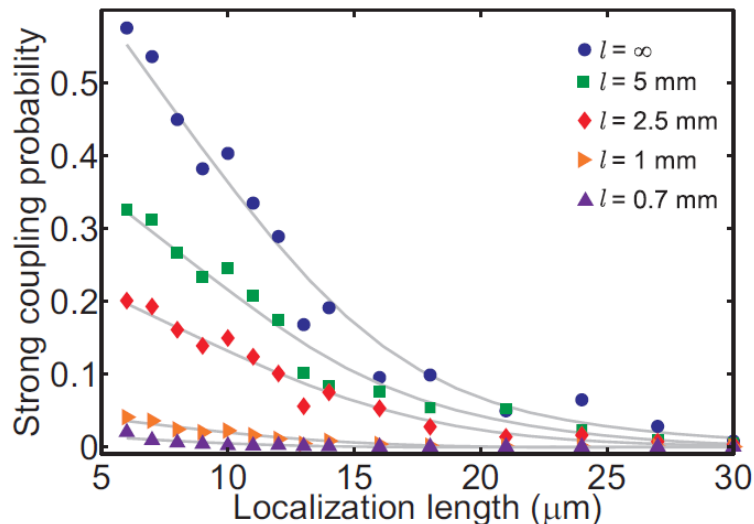


x15 enhancement of emission rate  
→ 94% efficient channeling of photons into cavity

# Statistics of Purcell enhancement and strong-coupling probability



Recorded statistics of Purcell enhancement (high Purcell factor tail of distribution)

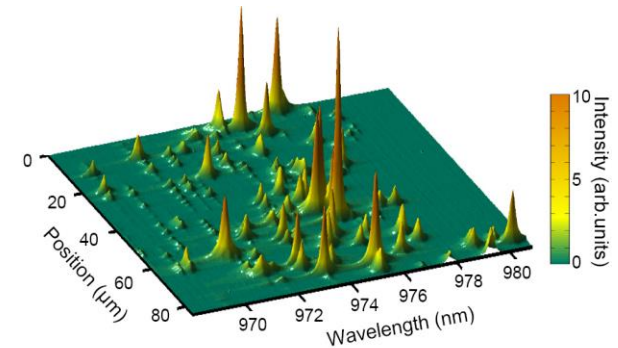
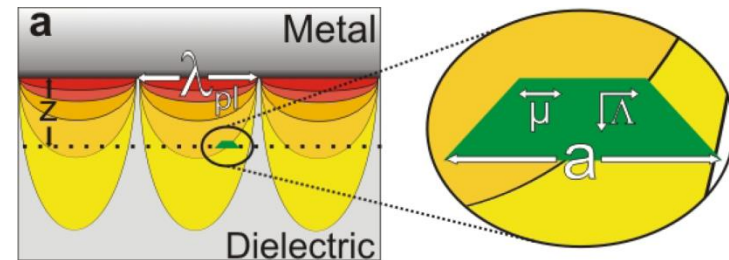
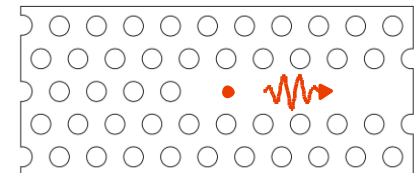
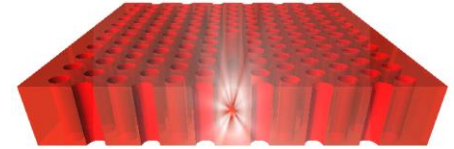


The probability of observing strong coupling of a randomly positioned quantum dot for realistic values of localization and loss lengths



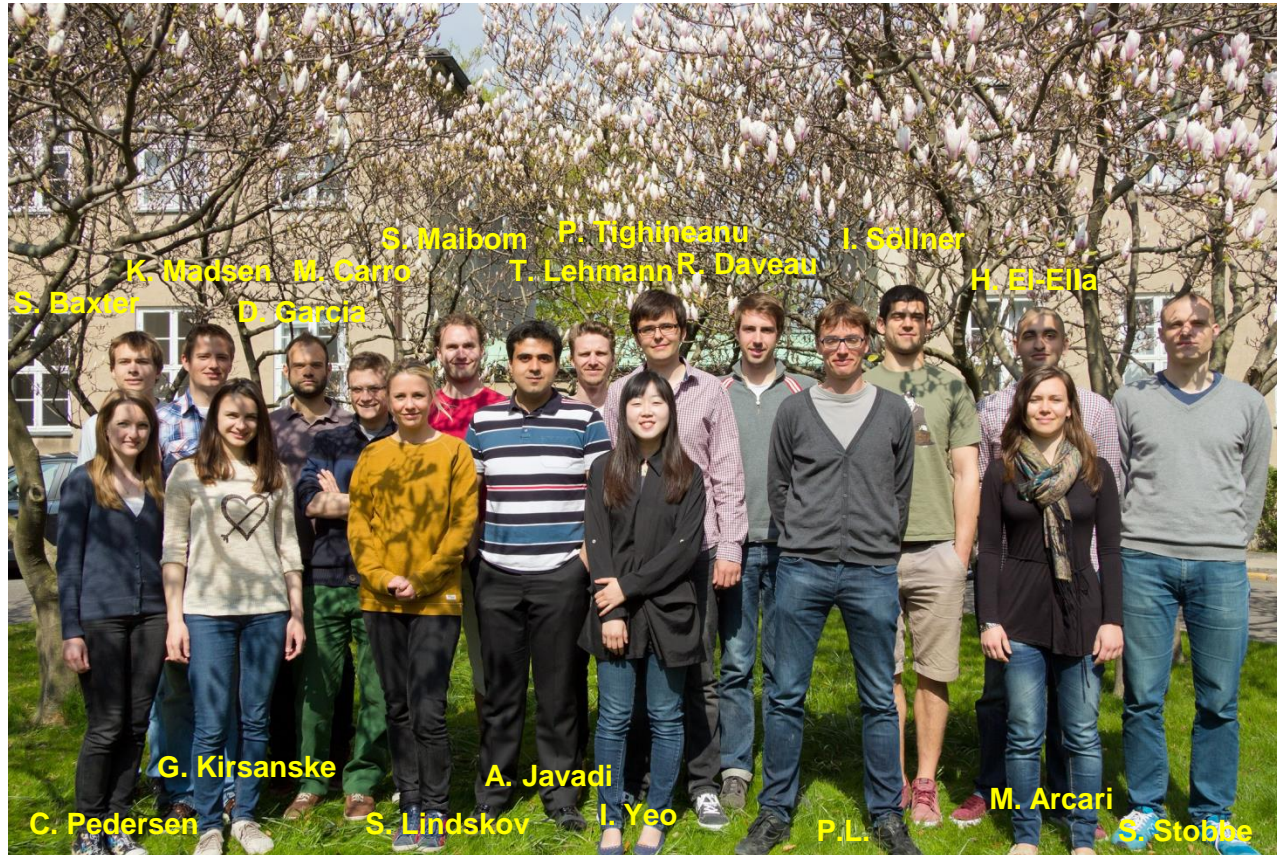
# Conclusions

- Photonic crystals enable spontaneous emission control and enhancement of the interaction between a single photon and a single quantum dot
- Solid-state emitters behave fundamentally different than atomic emitters
- Disorder leads to new physics: formation of Anderson-localized modes enabling cavity QED



# Acknowledgements

## Quantum Photonics Group at the Niels Bohr Institute



+  
Sahand Mahmoodian  
Leonardo Midolo  
Tommaso Pregolato

Growth of quantum dots:  
E.H. Lee and J.D. Song  
(KIST, Korea)

Recent review on quantum nanophotonics with quantum dot light sources:  
Lodahl, Mahmoodian & Stobbe, submitted to Rev. Mod. Phys. (2013). arXiv:1312.1079