

# Analytic reheating

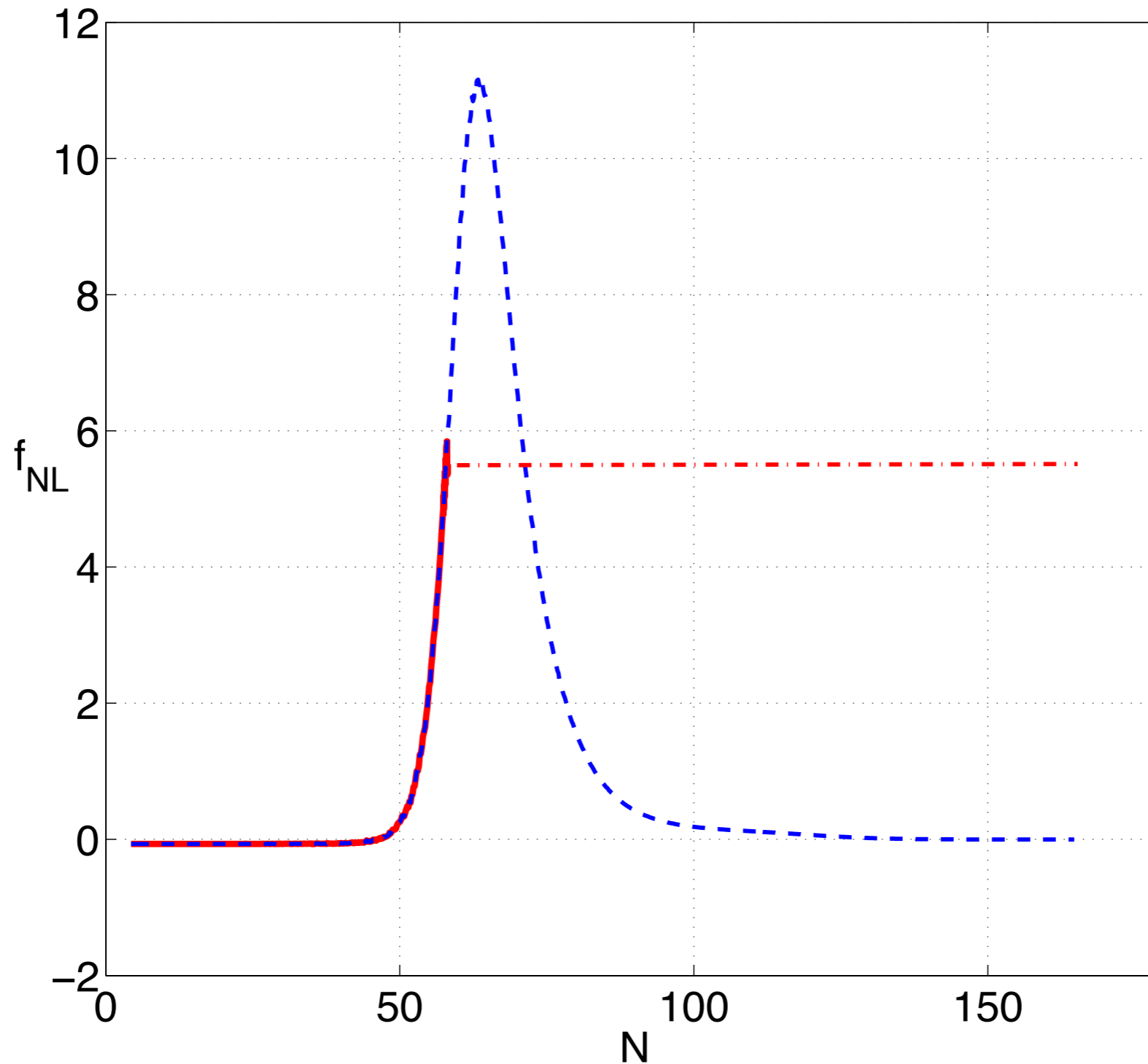
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arXiv: 1402.4800

In collaboration with Stefano Orani and David Mulryne

# Reheating matters...



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# Our result encapsulates:

Two-field slow-roll  
inflation

Curvaton-type

Inhomogeneous End of  
Inflation

Modulated Reheating

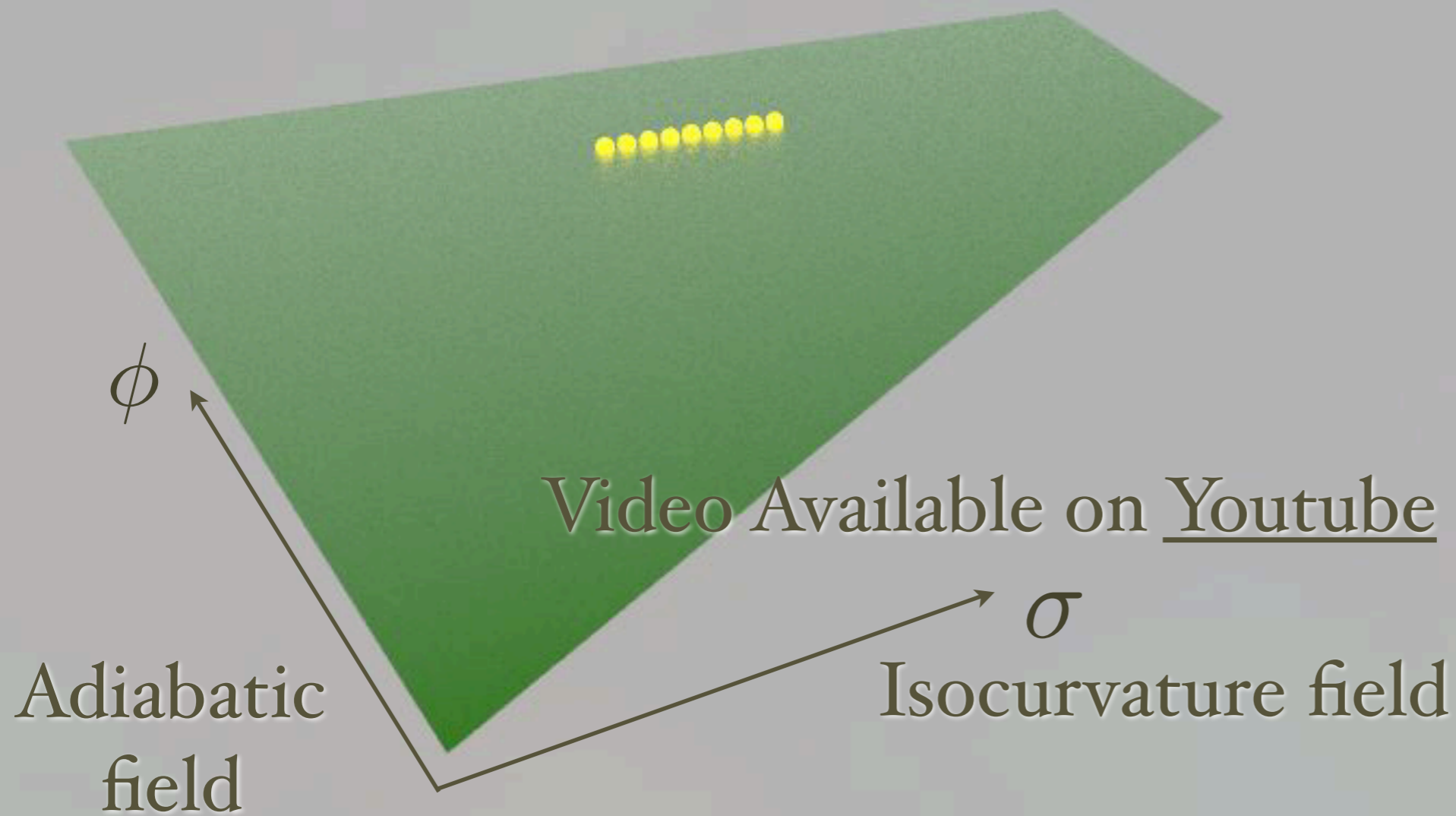
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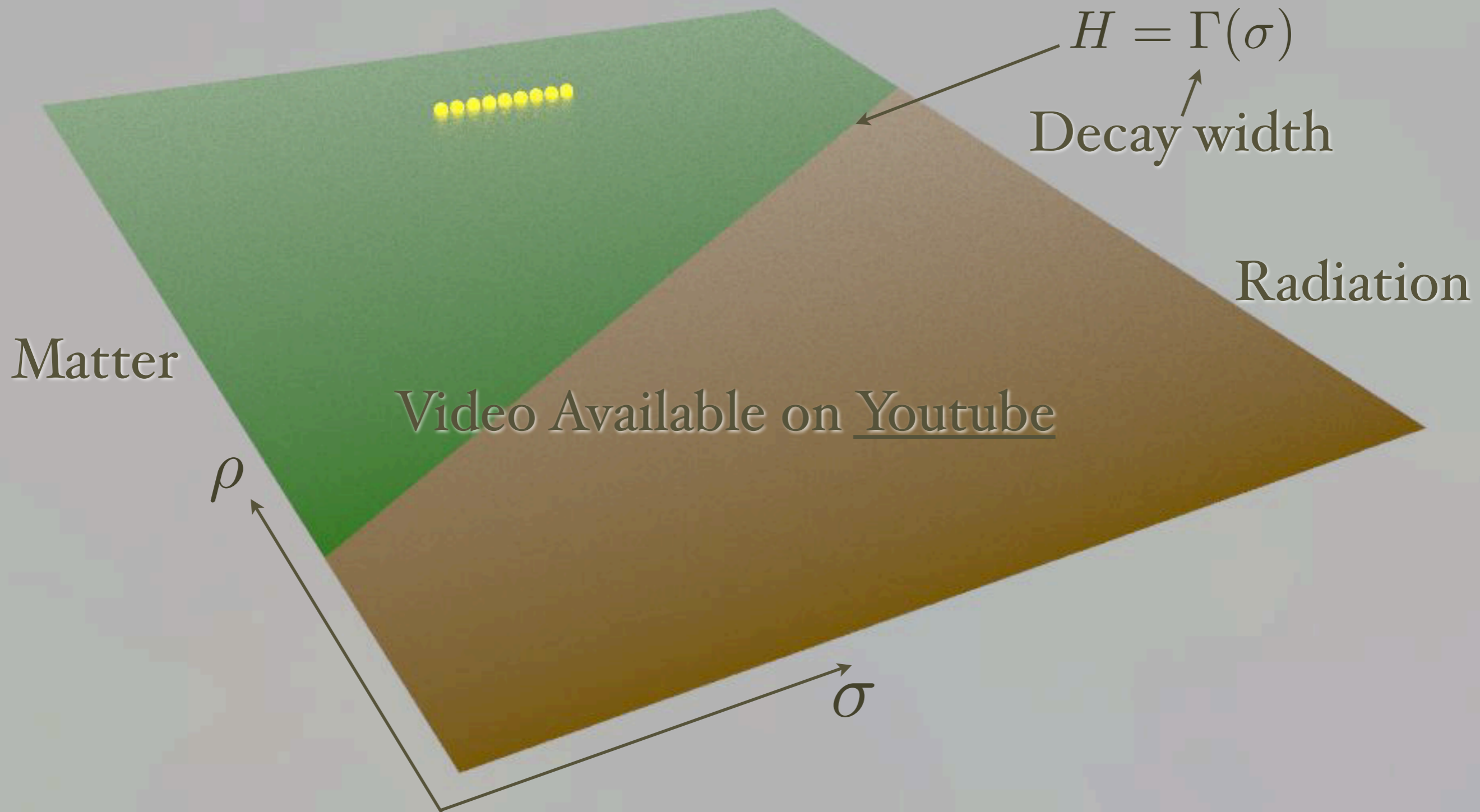
# Inhomogeneous End of Inflation



$$\zeta = \delta N$$

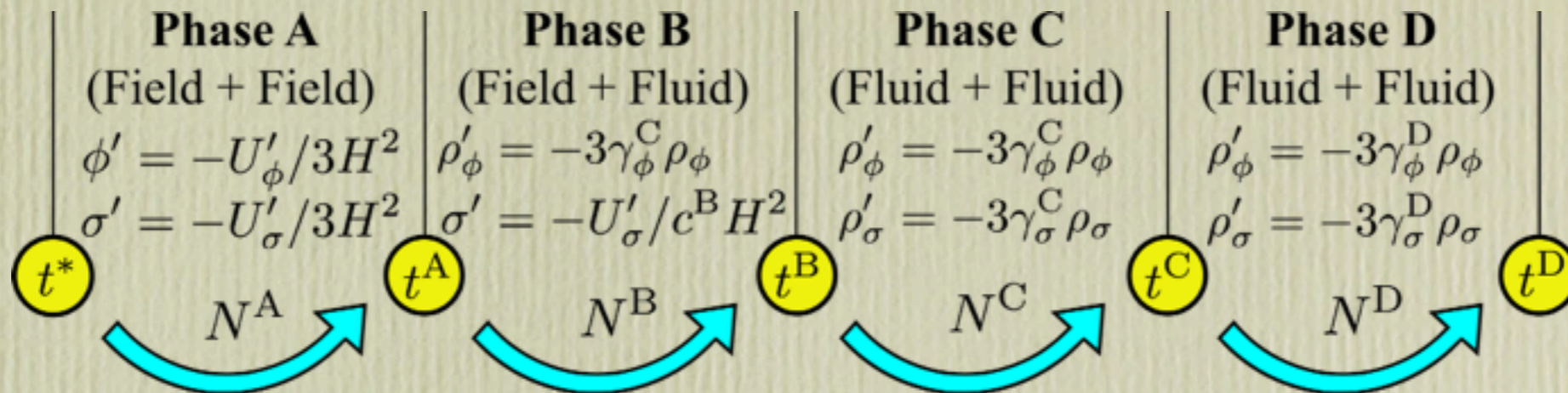


# Modulated Reheating



Equivalence between Inhomogeneous End of Inflation  
and Modulated Reheating: see arXiv: 1307.7095

# Analytic calculations...

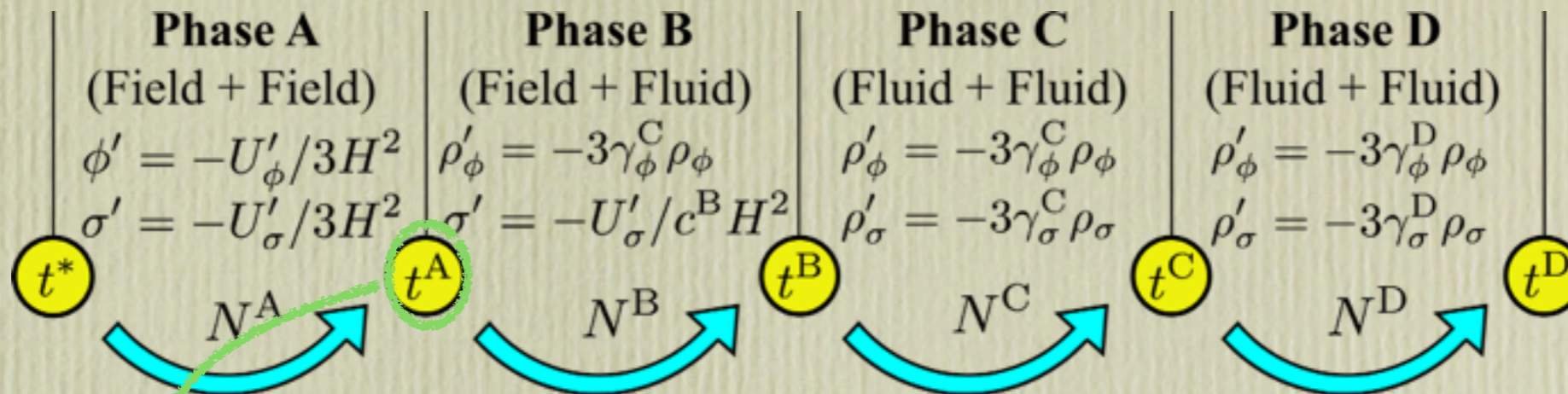


$$N = - \int_*^A \frac{U_\phi}{M_{\text{pl}}^2 U'_\phi} d\phi - \int_*^A \frac{U_\sigma}{M_{\text{pl}}^2 U'_\sigma} d\sigma$$

$$- \frac{1}{3\gamma_\phi^C} \ln \frac{\rho_\phi^C}{\rho_\phi^A} - \frac{1}{3\gamma_\phi^D} \ln \frac{\rho_\phi^D}{\rho_\phi^C} .$$

Phase A is just repeating Vernizzi and Wands (2006)...

# Analytic calculations...



Allows arbitrary hypersurfaces

$$\int_*^A \frac{1}{U'_\phi} d\phi = \int_*^A \frac{1}{U'_\sigma} d\sigma.$$

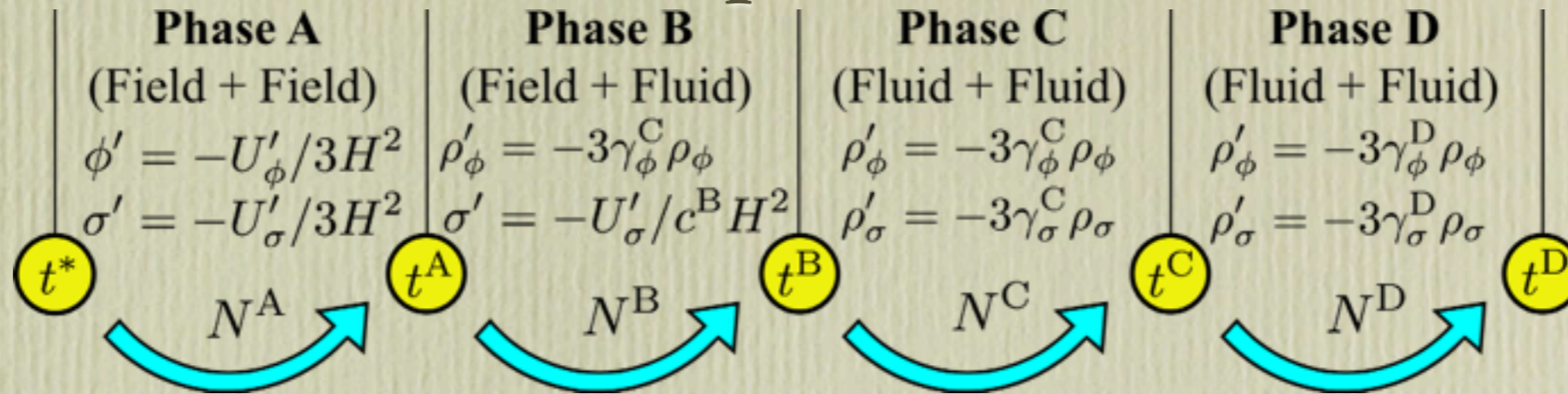
$$\frac{1}{U'_\phi{}^A} r^A \delta\phi^A = \frac{-1}{U'_\sigma{}^A (1 - r^A)} \delta\sigma^A = \frac{\delta\phi^*}{U'_\phi{}^*} - \frac{\delta\sigma^*}{U'_\sigma{}^*}$$

$$r = \frac{\rho'_\sigma}{\rho'_{\text{total}}}$$

(uniform density limit)



# Principle result



“Oscillation parameter”  
degenerate with  $r$

Modulation effects  
=1 if standard curvaton

$$\delta N = \left[ \frac{U_\sigma^A}{M_{\text{pl}}^2} + \frac{1 - x_\phi}{M_{\text{pl}}^2 x_\phi} \rho^A r^A - Q^A Q^B Q^C Q^S \frac{r^D}{3\gamma_\sigma^D} \frac{U_\sigma'^{B^2}}{U_\sigma^B} \right] \times \left( \frac{\delta\phi_*}{U_\phi'^*} - \frac{\delta\sigma_*}{U_\sigma'^*} \right) + \delta N_{\text{HCA}}$$

Horizon Crossing  
Approximation piece  
(constant)

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# Conclusions

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- Reheating can alter the predictions of inflation
- We have a general but simple formula for perturbative reheating with two-components
- Combines the Curvaton, Inhomogeneous End of Inflation and Modulated Reheating models.
- Our work is a test bed for investigating the analytic criterion for phase transitions.