



# *LEPTON FLAVOUR VIOLATION IN THE SIMPLEST LITTLE HIGGS MODEL*

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Tae 2013 Benasque

# *WHY THE LFV?*

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  - Neutrinos have a masses
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$$\tau \longrightarrow \mu + \textit{Hadrons}$$

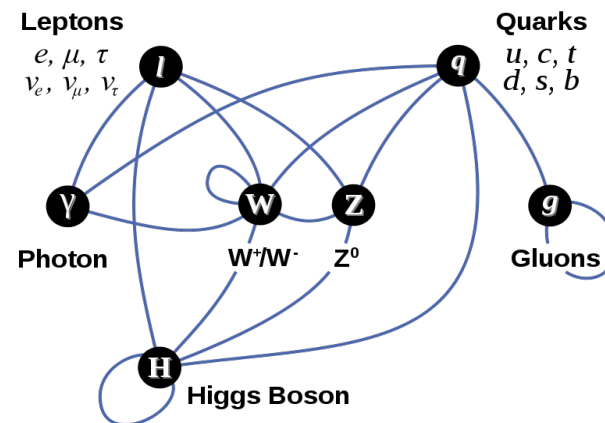
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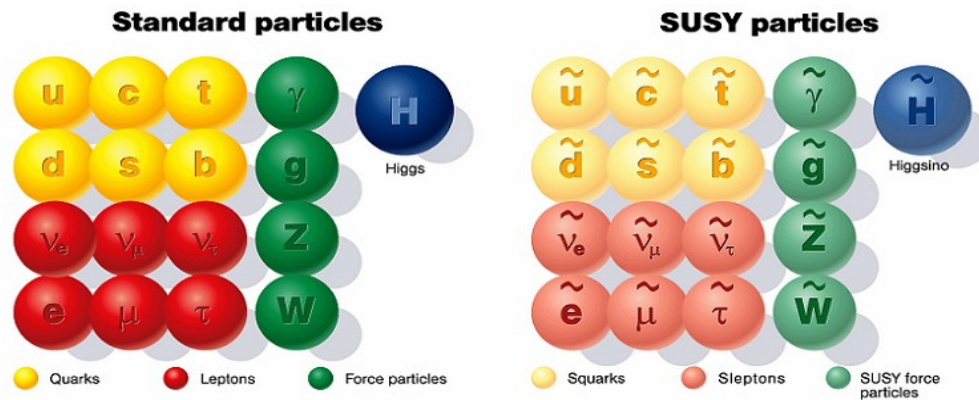
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Composite Higgs



# COMPOSITE & EFFECTIVE

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# COMPOSITE & EFFECTIVE

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- The Higgs like effective field coming out from new strong dynamic above 1 TeV (SILH)
- A small part of the coupling is Weak
- It has recently been obtained SILH with pseudoscalar Higgs

# COMPOSITE & EFFECTIVE

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## Little Higgs Theories:

Model	Global group	Gauge group	Type	Comments
Minimal moose [7]	$SU(3)^8/SU(3)^4$	$SU(3) \times SU(2) \times U(1)$	t.s.	can contain extra light triplet and singlet scalars
Minimal moose with $SU(2)_C$ [8]	$SO(5)^8/SO(5)^4$	$SO(5) \times SU(2) \times U(1)$	t.s.	less constrained from electroweak precision tests (EWPT)
Moose with T-parity [9]	$SO(5)^{10}/SO(5)^5$	$(SU(2) \times U(1))^3$	t.s.	very few constraints from EWPT, large spectrum, complicated plaquettes
Littlest Higgs [6]	$SU(5)/SO(5)$	$(SU(2) \times U(1))^2$	p.g.g.	Minimal field content
$SU(6)/Sp(6)$ model [10]	$SU(6)/Sp(6)$	$(SU(2) \times U(1))^2$	p.g.g.	Small field content, contains a heavy vector-like quark doublet
Littlest Higgs with $SU(2)_C$ [11]	$SO(9)/(SO(5) \times SO(4))$	$SU(2)^3 \times U(1)$	p.g.g.	less constraints from EWPT
Littlest Higgs with T-parity [12]	$SU(5)/SO(5)$	$(SU(2) \times U(1))^2$	p.g.g.	Minimal field content, very few constraints from EWPT
$SU(3)$ simple group [13, 14]	$(SU(3) \times U(1))^2 / (SU(2) \times U(1))^2$	$SU(3) \times U(1)$	s.g.g.	no large quartic
$SU(4)$ simple group [13]	$(SU(4) \times U(1))^4 / (SU(3) \times U(1))^4$	$SU(4) \times U(1)$	s.g.g.	Two Higgs doublets, large quartic
$SU(9)/SU(8)$ simple group [15]	$SU(9)/SU(8)$	$SU(3) \times U(1)$	s.g.g.	Two Higgs doublets, large quartic

# ***SIMPLEST LITTLE HIGGS***

*arXiv: 1101.2936 Àguila et al.*

- Solve the little hierarchy problem without the T-parity

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- E.W. Sector is in a group  $SU(3) \times U(1)$

# ***SIMPLEST LITTLE HIGGS***

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- Solve the little hierarchy problem without the T-parity
- E.W. Sector is in a group  $SU(3) \times U(1)$
- LHT and SLH are equivalent but the last have new sources of LFV

# *SIMPLEST LITTLE HIGGS*

*arXiv: 1101.2936 Àguila et al.*

- Every lepton family consists of an SU(3) left-handed triplet and 2 right-handed singlets

$$L_m^T = (\nu_L, \ell_L, iN_L)_m, \quad \ell_{Rm}, \quad N_{Rm}$$



# *SIMPLEST LITTLE HIGGS*

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- For the quarks we have 2 embedding

$$L_m^T = (\nu_L, \ell_L, iN_L)_m, \quad \ell_{Rm}, \quad N_{Rm}$$

$$Q_m^T = (u_L, d_L, iU_L)_m, \quad u_{Rm}, \quad d_{Rm}, \quad U_{Rm}$$

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→ For the quarks we have 2 embedding

$$L_m^T = (\nu_L, \ell_L, iN_L)_m, \quad \ell_{Rm}, \quad N_{Rm}$$

$$Q_1^T = (d_L, -u_L, iD_L), \quad d_R, \quad u_R, \quad D_R$$

$$Q_2^T = (s_L, -c_L, iS_L), \quad s_R, \quad c_R, \quad S_R$$

$$Q_3^T = (t_L, b_L, iT_L), \quad t_R, \quad b_R, \quad T_R$$

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→ For the quarks we have 2 embedding

Universal embedding (U)							
Fermion	$Q_{1,2}$	$Q_3$	$u_{Rm}, U_{Rm}$	$d_{Rm}$	$L_m$	$N_{Rm}$	$e_{Rm}$
$Q_x$ charge	1/3	1/3	2/3	-1/3	-1/3	0	-1
SU(3) rep.	<b>3</b>	<b>3</b>	<b>1</b>	<b>1</b>	<b>3</b>	<b>1</b>	<b>1</b>
Anomaly-free embedding (AF)							
Fermion	$Q_{1,2}$	$Q_3$	$u_{Rm}, T_{Rm}$	$d_{Rm}, D_{Rm}, S_{Rm}$	$L_m$	$N_{Rm}$	$e_{Rm}$
$Q_x$ charge	0	1/3	2/3	-1/3	-1/3	0	-1
SU(3) rep.	<b><math>\bar{3}</math></b>	<b>3</b>	<b>1</b>	<b>1</b>	<b>3</b>	<b>1</b>	<b>1</b>

# SIMPLEST LITTLE HIGGS

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→ Other basic fields and expansions

$$D_\mu = \partial_\mu - igA_\mu^a T_a + ig_x Q_x B_\mu^x, \quad g_x = \frac{gt_W}{\sqrt{1 - t_W^2/3}}$$
$$A^a T_a = \frac{A^3}{2} \begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 0 \end{pmatrix} + \frac{A^8}{2} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -2 \end{pmatrix} + \frac{1}{\sqrt{2}} \begin{pmatrix} 0 & W^+ & Y^0 \\ W^- & 0 & X^- \\ Y^{0\dagger} & X^+ & 0 \end{pmatrix}$$
$$\Phi_1 = \exp\left(\frac{i\Theta'}{f}\right) \exp\left(\frac{it_\beta\Theta}{f}\right) \begin{pmatrix} 0 \\ 0 \\ fc_\beta \end{pmatrix}$$
$$\Phi_2 = \exp\left(\frac{i\Theta'}{f}\right) \exp\left(-\frac{i\Theta}{t_\beta f}\right) \begin{pmatrix} 0 \\ 0 \\ fs_\beta \end{pmatrix}$$
$$\Theta = \begin{pmatrix} 0 & 0 & h^0 \\ 0 & 0 & h^- \\ h^{0\dagger} & h^+ & 0 \end{pmatrix}$$
$$h^0 = (v + H)/\sqrt{2} - i\chi \text{ and } h^\pm = -\phi^\pm.$$

# SIMPLEST LITTLE HIGGS

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→ Scalar Lagrangian and physical states

$$\mathcal{L}_\Phi = |D_\mu \Phi_1|^2 + |D_\mu \Phi_2|^2$$

$$W^\pm \rightarrow W^\pm \pm \frac{iv^3}{3\sqrt{2}f^3} \left( \frac{c_\beta^3}{s_\beta} - \frac{s_\beta^3}{c_\beta} \right) X^\pm$$

$$X^\pm \rightarrow X^\pm \pm \frac{iv^3}{3\sqrt{2}f^3} \left( \frac{c_\beta^3}{s_\beta} - \frac{s_\beta^3}{c_\beta} \right) W^\pm$$

$$\phi^\pm \rightarrow \mp i \left( 1 + \frac{v^2}{12f^2} \left( \frac{c_\beta^4}{s_\beta^2} + \frac{s_\beta^4}{c_\beta^2} \right) \right) \phi^\pm$$

# SIMPLEST LITTLE HIGGS

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→ Scalar Lagrangian and physical states

$$\mathcal{L}_\Phi = |D_\mu \Phi_1|^2 + |D_\mu \Phi_2|^2$$

$$\begin{pmatrix} A^3 \\ A^8 \\ B_x \end{pmatrix} = \begin{pmatrix} 0 & c_W & -s_W \\ \frac{1}{\sqrt{3}} \sqrt{3-t_W^2} & \frac{s_W^2}{\sqrt{3}c_W} & \frac{s_W}{\sqrt{3}} \\ -\frac{t_W}{\sqrt{3}} & \frac{s_W}{\sqrt{3}} \sqrt{3-t_W^2} & \frac{c_W}{\sqrt{3}} \sqrt{3-t_W^2} \end{pmatrix} \begin{pmatrix} Z' \\ Z \\ A \end{pmatrix}$$

$$Z' \rightarrow Z' + \delta_Z Z,$$

$$Z \rightarrow Z - \delta_Z Z',$$

$$\delta_Z = -\frac{(1-t_W^2)\sqrt{3-t_W^2} v^2}{8c_W f^2}$$

# SIMPLEST LITTLE HIGGS

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## → Vector and Yukawa Lagrangians

$$\mathcal{L}_V = -\frac{1}{2}\text{Tr}\{\tilde{G}_{\mu\nu}\tilde{G}^{\mu\nu}\} - \frac{1}{4}B_x^{\mu\nu}B_{x\mu\nu}, \quad \tilde{G}_{\mu\nu} = \frac{i}{g}[D_\mu, D_\nu]$$

$$\mathcal{L}_Y \supset i\lambda_N^m \bar{N}_{Rm} \Phi_2^\dagger L_m + \frac{i\lambda_\ell^{mn}}{\Lambda} \bar{\ell}_{Rm} \epsilon_{ijk} \Phi_1^i \Phi_2^j L_n^k + \text{h.c.}$$

$$\delta_\nu = -\frac{v}{\sqrt{2}ft_\beta} \quad \begin{pmatrix} \nu_L \\ N_L \end{pmatrix}_m \rightarrow \left[ \begin{pmatrix} 1 - \frac{\delta_\nu^2}{2} & -\delta_\nu \\ \delta_\nu & 1 - \frac{\delta_\nu^2}{2} \end{pmatrix} \begin{pmatrix} V_\ell \nu_L \\ N_L \end{pmatrix} \right]_m \quad \ell_{Lm} \rightarrow (V_\ell \ell_L)_m = V_\ell^{mi} \ell_{Li}$$

# *SIMPLEST LITTLE HIGGS*

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→ Fermion Lagrangian

$$\mathcal{L}_F = \bar{\psi}_m i \not{D} \psi_m, \quad \psi_m = \{L_m, \ell_{Rm}, N_{Rm}\}$$



# *OUR WORK*

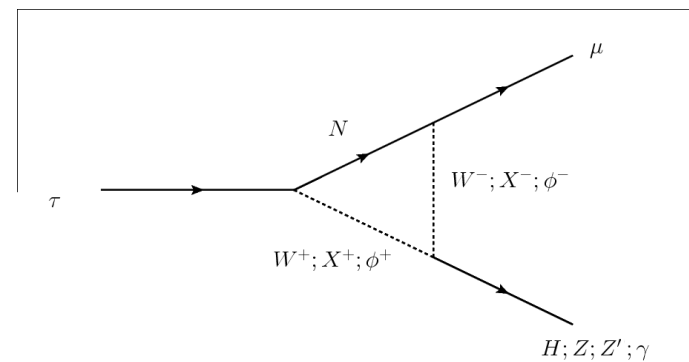
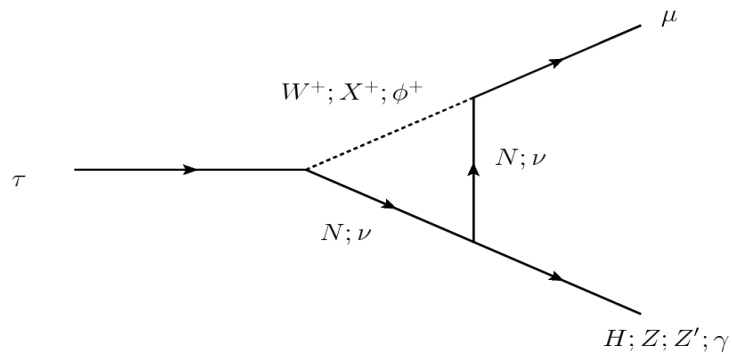
- Finally we can write the Feynman rules for the channels of our interest



# OUR WORK

$$\tau \longrightarrow \mu + H \longrightarrow \mu + P$$

$$\tau \longrightarrow \mu + Z; Z'; \gamma \longrightarrow \mu + V; PP$$



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- We are calculating the amplitudes of LFV with the SLH model and after we'll study the hadronization with the chiral symmetry
- Then the parameters obtained should be compared with the results of tree-level hadronic processes

***Muchas Gracias!***