

Near-Field Heat Transfer for Anisotropic Media

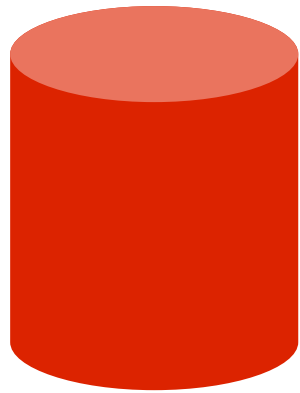
Felipe S. S. Rosa



Collaborators

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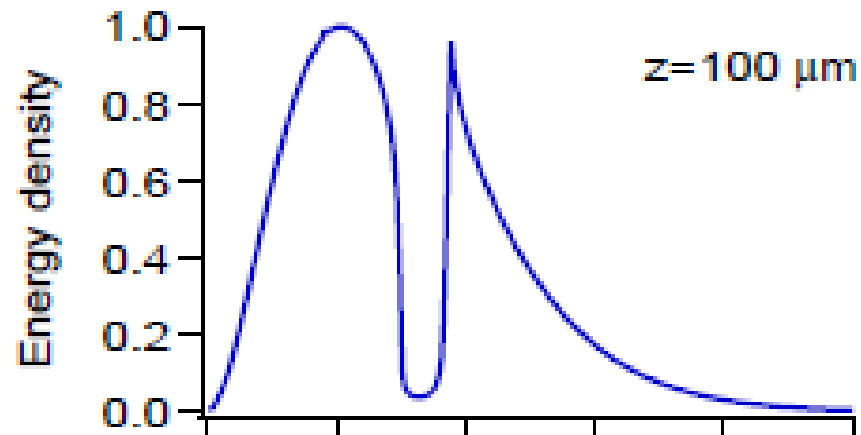
Near-Field Heat Transfer



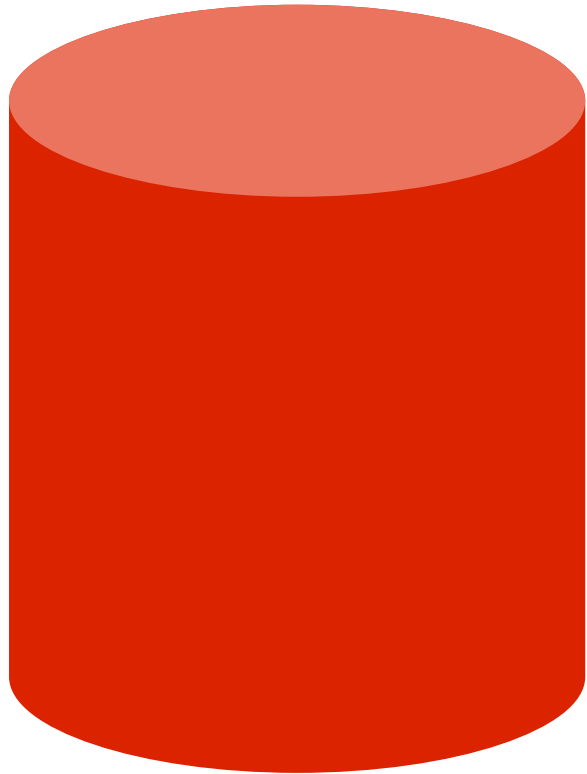
heat



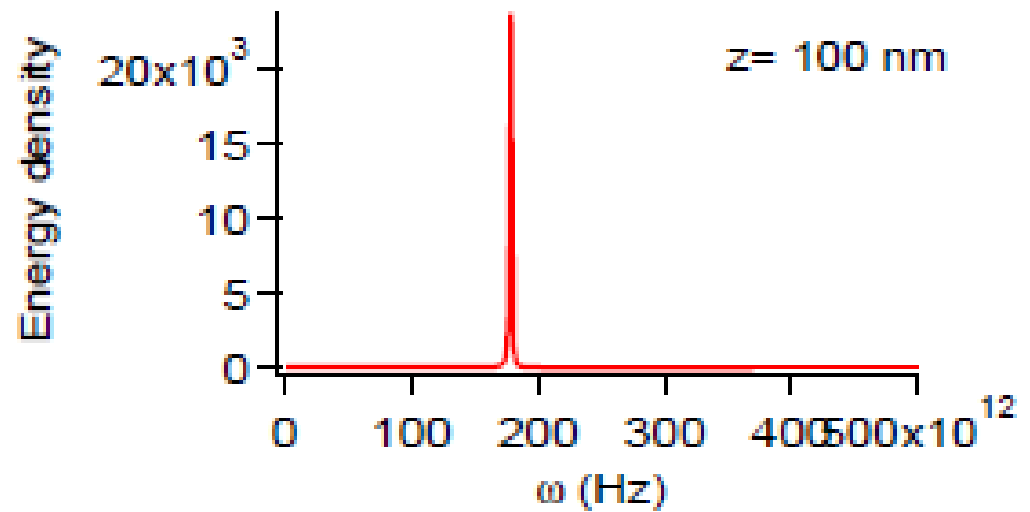
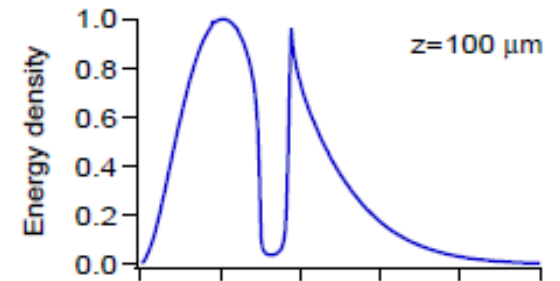
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But when we put the detector very close...



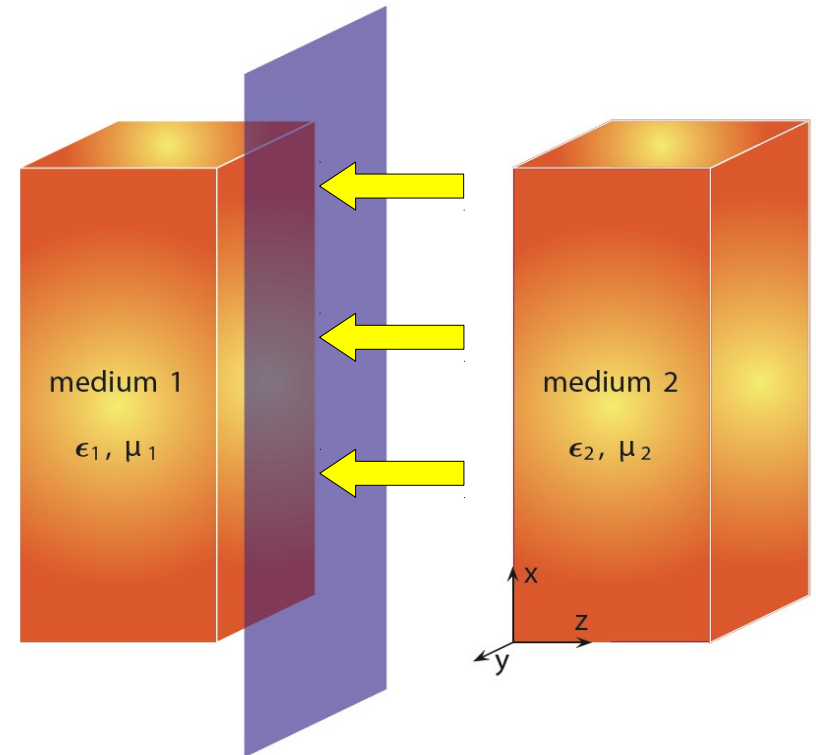
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The heat flux is given in by the Poynting vector

$$\Phi = \int_A d\mathbf{A} \cdot \langle \mathbf{S} \rangle = A \langle S_z \rangle$$

$$\mathbf{S} = \mathbf{E} \times \mathbf{H}$$



Expressing the fields in terms of the stochastic sources

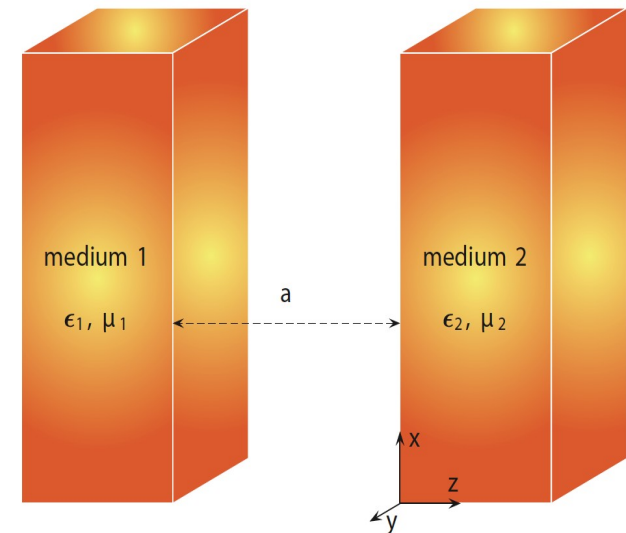
$$\tilde{\mathbf{E}}^f(\mathbf{r}, \omega) = i\omega\mu_0 \int_V d\mathbf{r}'' G^E(\mathbf{r}, \mathbf{r}'', \omega) \cdot \tilde{\mathbf{j}}^f(\mathbf{r}'', \omega)$$

$$\tilde{\mathbf{H}}^f(\mathbf{r}, \omega) = i\omega\mu_0 \int_V d\mathbf{r}'' G^H(\mathbf{r}, \mathbf{r}'', \omega) \cdot \tilde{\mathbf{j}}^f(\mathbf{r}'', \omega),$$

and assuming local equilibrium for each body

$$\langle j_i^{\mathcal{F}}(\mathbf{r}, \omega) j_j^{\mathcal{F}}(\mathbf{r}', \omega') \rangle = 2\pi\omega\Theta(\omega, T) [\tilde{\epsilon}_{i,j}(\omega) - \tilde{\epsilon}_{j,i}^*(\omega)] \delta(\omega - \omega') \delta(\mathbf{r} - \mathbf{r}').$$

$$\Theta(\omega, T) = \frac{\hbar\omega}{2} + \frac{\hbar\omega}{e^{i\hbar\omega/(k_B T)} - 1}$$



we get an expression for the HT in terms of Green's functions

$$\Phi \sim A \int d\mathbf{r}' d\mathbf{r}'' G_E(\mathbf{r}, \mathbf{r}') G_H(\mathbf{r}, \mathbf{r}'') \dots$$

In the isotropic case we have the famous Polder & van Hove result

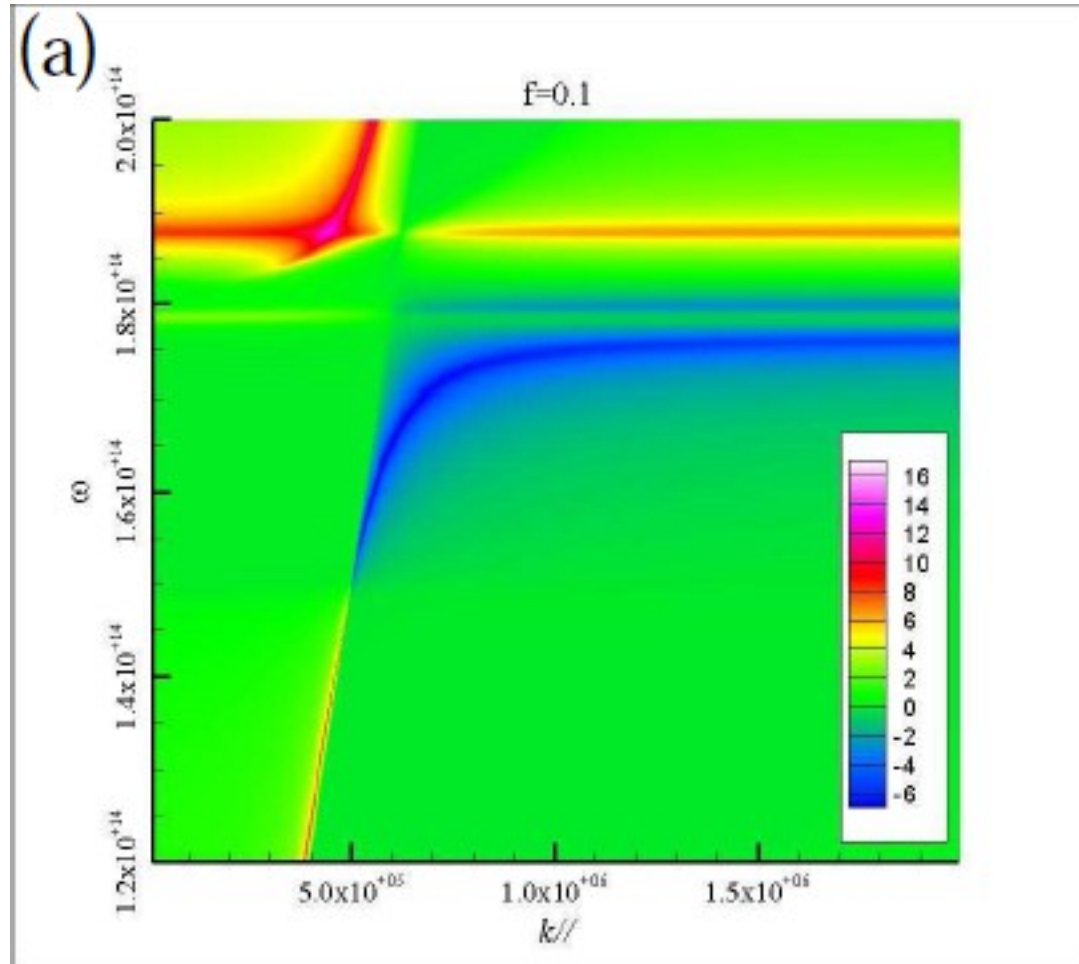
$$\begin{aligned} \Phi(d, T_1, T_2) = & \int_0^\infty \frac{d\omega}{2\pi} [\Theta(\omega, T_1) - \Theta(\omega, T_2)] \\ & \sum_{j=s,p} \left[\int_0^{k_0} \frac{d^2\kappa}{4\pi^2} \frac{(1 - |r_j^1|^2)(1 - |r_j^2|^2)}{|1 - r_j^1 r_j^2 e^{-2i\gamma d}|^2} \right. \\ & \left. + \int_{k_0}^\infty \frac{d^2\kappa}{4\pi^2} \frac{4\text{Im}(r_j^1)\text{Im}(r_j^2) e^{-2\text{Im}(\gamma)d}}{|1 - r_j^1 r_j^2 e^{-2\text{Im}(\gamma)d}|^2} \right] \end{aligned}$$

$$r_j^{s,s}(\omega, \kappa) = \frac{\gamma - \gamma_s}{\gamma + \gamma_s}$$

$$r_j^{p,p}(\omega, \kappa) = \frac{\epsilon_j \gamma - \gamma_s}{\epsilon_j \gamma + \gamma_s}$$

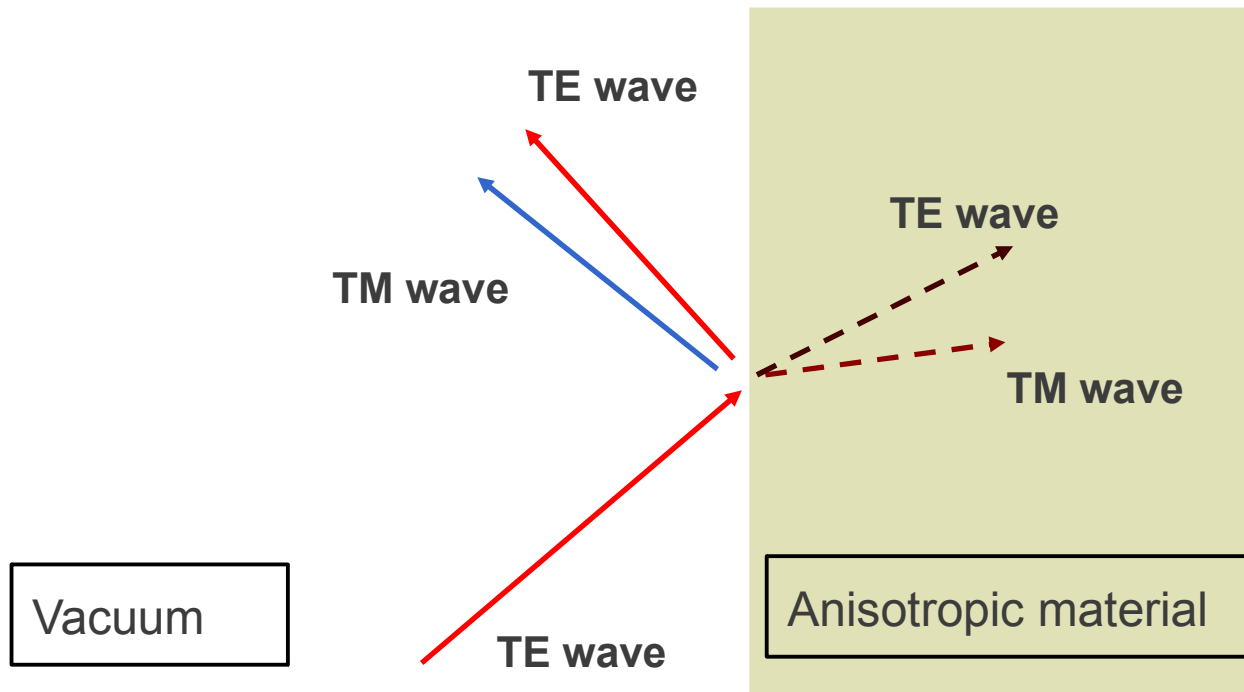
$$\gamma = \sqrt{k_0^2 - \kappa^2}$$

$$\gamma_s = \sqrt{\epsilon_j k_0^2 - \kappa^2}$$



Anisotropy

Anisotropy mixes TE and TM components



the reflection matrices are now given by

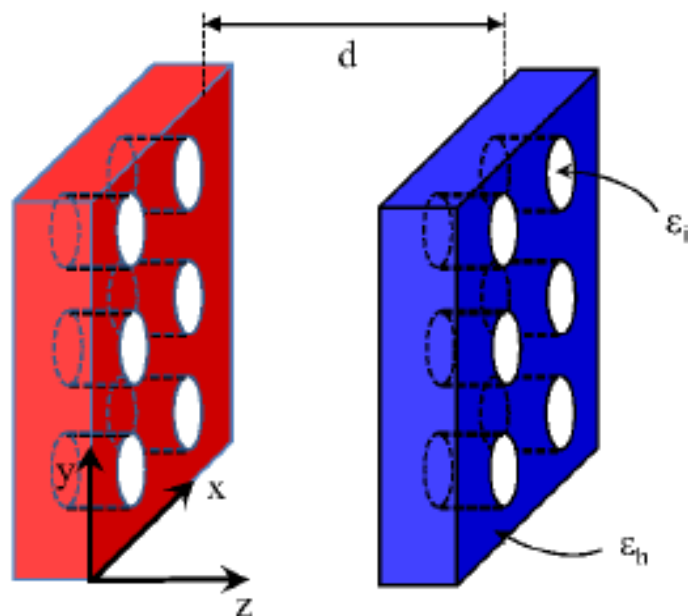
$$\mathbb{R}_i = \begin{bmatrix} r_i^{s,s}(\omega, \kappa) & r_i^{s,p}(\omega, \kappa) \\ r_i^{p,s}(\omega, \kappa) & r_i^{p,p}(\omega, \kappa) \end{bmatrix}$$

The generalization of heat transfer to the anisotropic case turns out to be the intuitive guess

$$\Phi = \int_0^\infty \frac{d\omega}{2\pi} [\Theta(\omega, T_1) - \Theta(\omega, T_2)] \sum_{j=\{s,p\}} \int \frac{d^2\kappa}{(2\pi)^2} T_j(\omega, \kappa; d)$$

$$T(\omega, \kappa; d) = \begin{cases} \text{Tr}[(\mathbf{1} - \mathbb{R}_2^\dagger \mathbb{R}_2) \mathbb{D}^{12} (\mathbf{1} - \mathbb{R}_1 \mathbb{R}_1^\dagger) \mathbb{D}^{12\dagger}], & \kappa < \omega/c \\ \text{Tr}[(\mathbb{R}_2^\dagger - \mathbb{R}_2) \mathbb{D}^{12} (\mathbb{R}_1 - \mathbb{R}_1^\dagger) \mathbb{D}^{12\dagger}] e^{-2|\gamma_{\text{r}}|d}, & \kappa > \omega/c \end{cases}$$

Out-of-plane Anisotropy



The media still supports TE and TM waves, meaning that

$$r_i^{S,P}(\omega, \mathbf{\kappa}) = r_i^{P,S}(\omega, \mathbf{\kappa}) = 0,$$

and also

$$r^{S,S}(\omega, \kappa) = \frac{\gamma - \gamma_s}{\gamma + \gamma_s}$$

$$\gamma_s = \sqrt{\epsilon_{\parallel} \omega^2 / c^2 - \kappa^2},$$

$$r^{P,P}(\omega, \kappa) = \frac{\epsilon_{\parallel} \gamma - \gamma_p}{\epsilon_{\parallel} \gamma + \gamma_p}$$

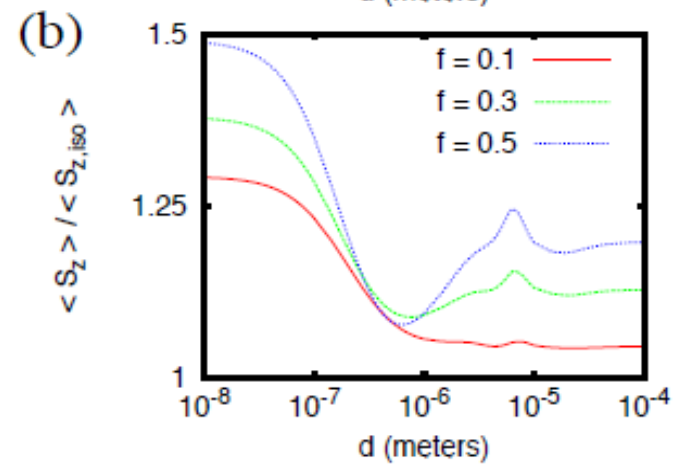
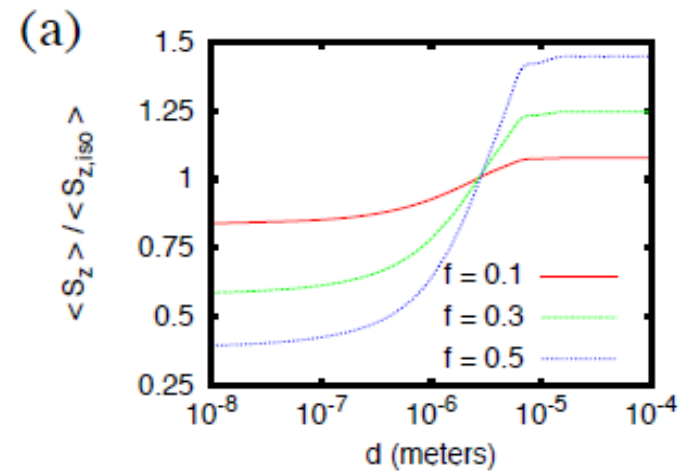
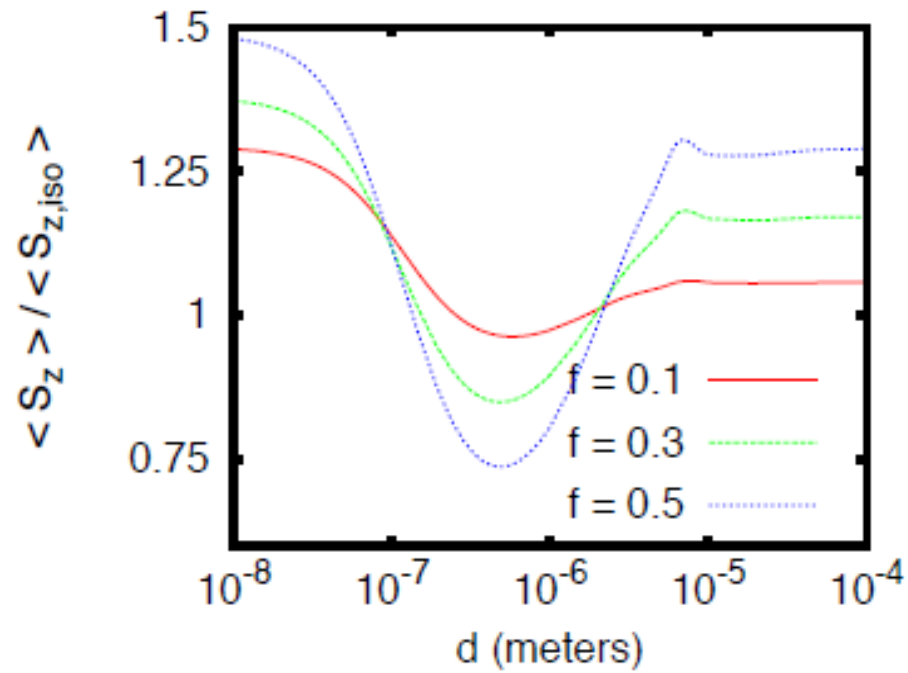
$$\gamma_p = \sqrt{\epsilon_{\parallel} \omega^2 / c^2 - \frac{\epsilon_{\parallel}}{\epsilon_{\perp}} \kappa^2},$$

and so the problem is similar to the isotropic one.
Using a Maxwell-Garnett approximation for the materials

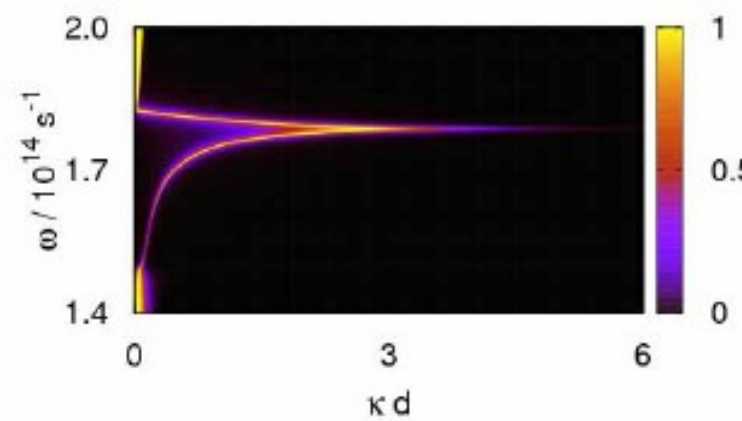
$$\epsilon_{\parallel} = \epsilon_h \frac{\epsilon_i(1+f) + \epsilon_h(1-f)}{\epsilon_i(1-f) + \epsilon_h(1+f)},$$

$$\epsilon_{\perp} = \epsilon_h(1-f) + \epsilon_i f,$$

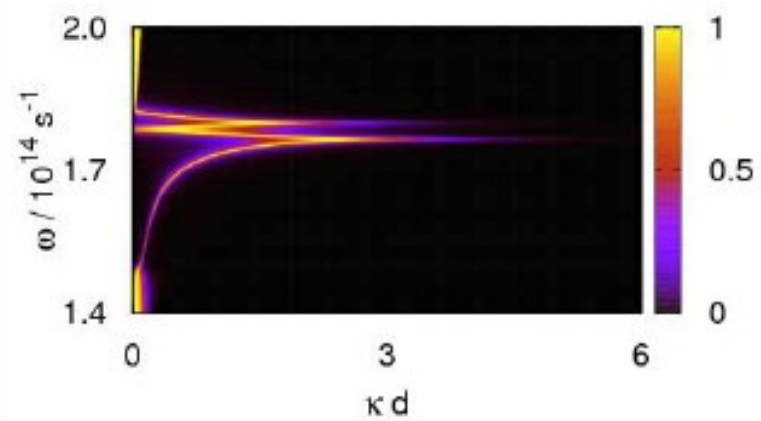
we get



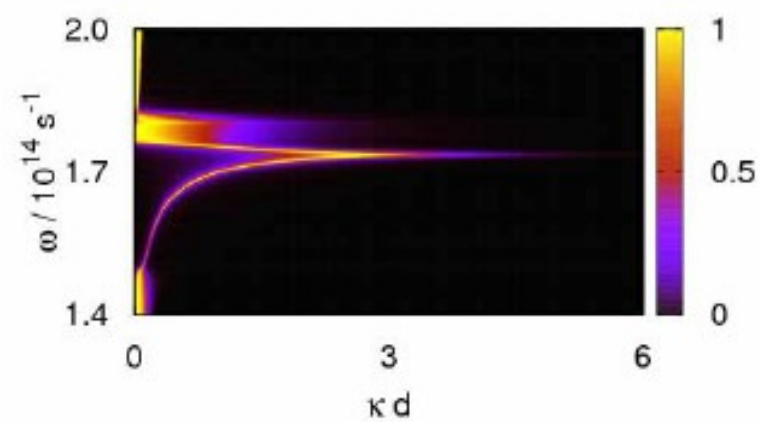
(a)



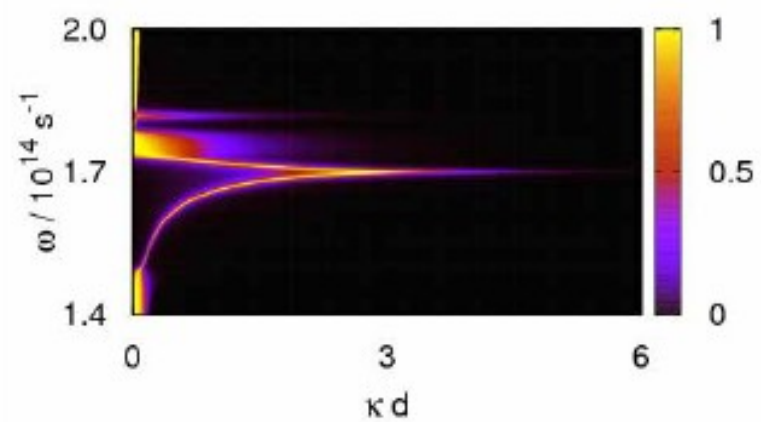
(b)



(c)

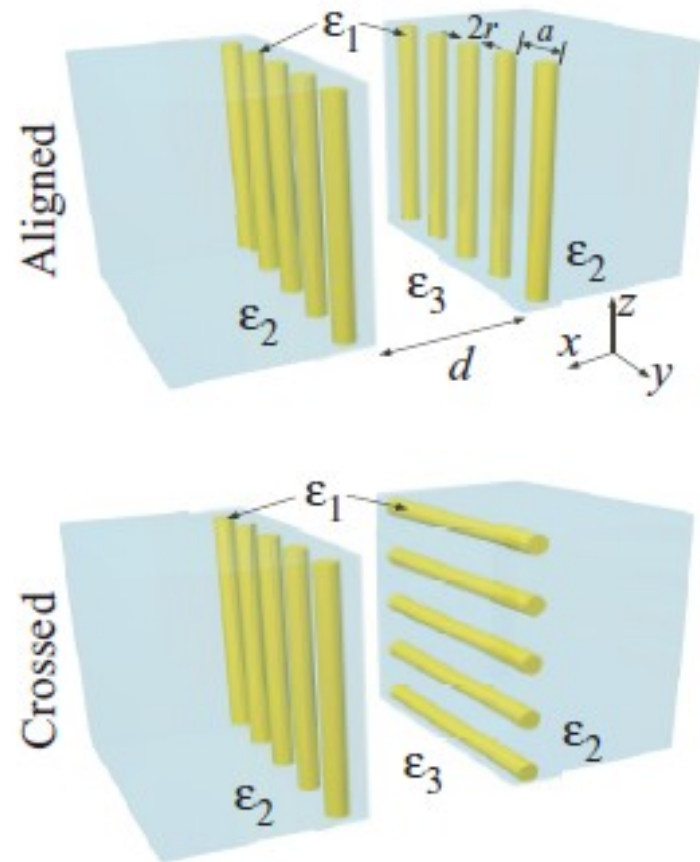
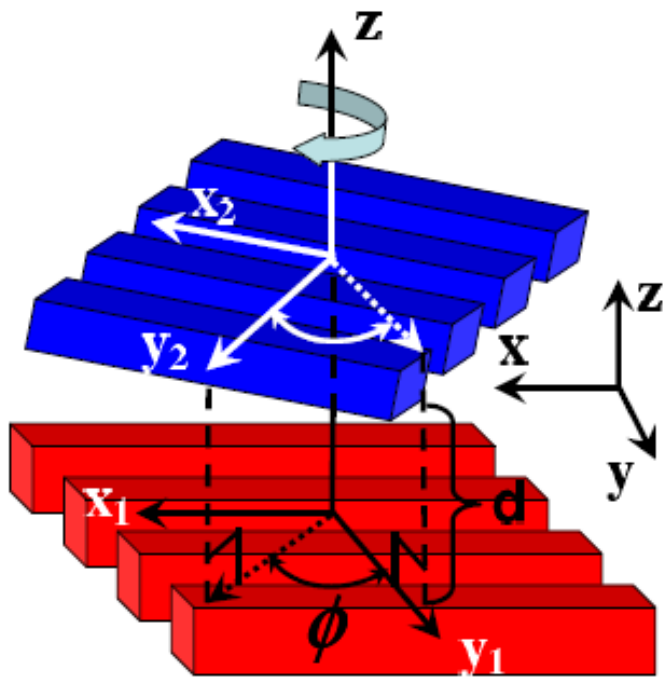


(d)



S.-A. Biehs et al., Opt. Exp. 19, A1088 (2011).

In-plane Anisotropy



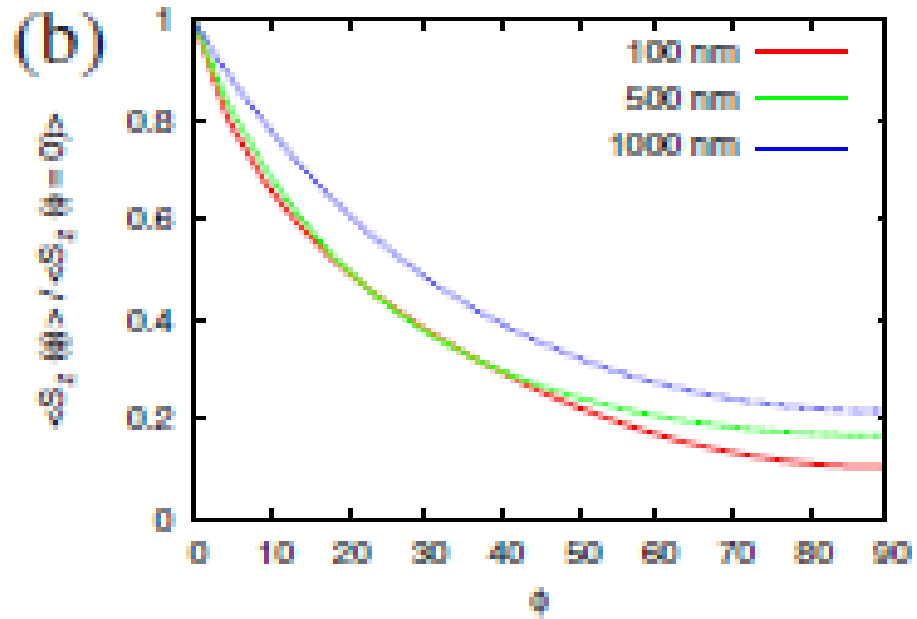
In this case we have full-fledged anisotropy

$$\Phi = \int_0^\infty \frac{d\omega}{2\pi} [\Theta(\omega, T_1) - \Theta(\omega, T_2)] \sum_{j=\{s,p\}} \int \frac{d^2\kappa}{(2\pi)^2} T_j(\omega, \kappa; d)$$

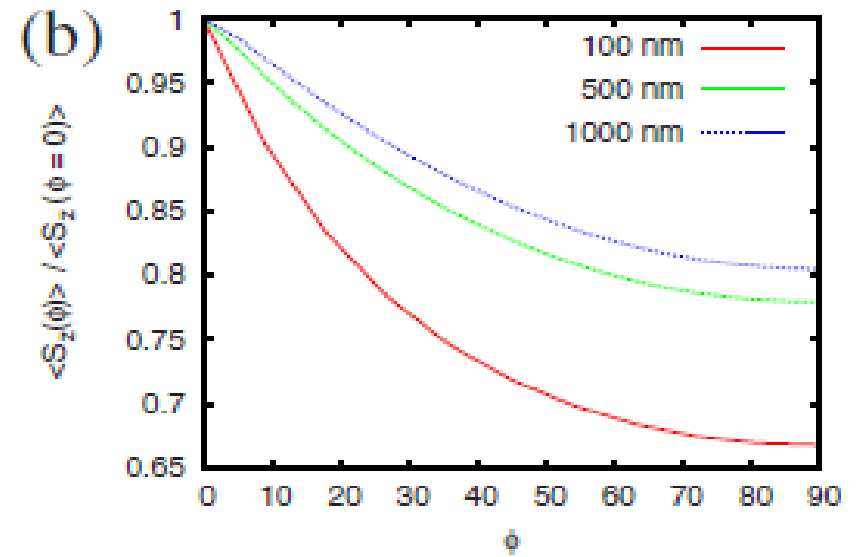
$$T(\omega, \kappa; d) = \begin{cases} \text{Tr}[(\mathbf{1} - \mathbf{R}_2^\dagger \mathbf{R}_2) \mathbf{D}^{12} (\mathbf{1} - \mathbf{R}_1 \mathbf{R}_1^\dagger) \mathbf{D}^{12\dagger}], & \kappa < \omega/c \\ \text{Tr}[(\mathbf{R}_2^\dagger - \mathbf{R}_2) \mathbf{D}^{12} (\mathbf{R}_1 - \mathbf{R}_1^\dagger) \mathbf{D}^{12\dagger}] e^{-2|\gamma_{\text{r}}|d}, & \kappa > \omega/c \end{cases}$$

- FSSR et al., PRA 78 032117 (2008)
- S. Teitler and B.W. Hennis, J. Opt. Soc. Am. **60**, 830 (1970)
- V.A. Parsegian and G.H. Weiss, J. Adhes. **3**, 259 (1972).
- Y. Barash, Izv. Vyssh. Uchebn. Zaved. Radiofiz. **12**, 1637 (1978)
- T.G. Philbin and U. Leonhardt, arXiv:0806.4752, (2008).
- ...

Metals



Dielectrics



S.-A. Biels, FSSR, P. Ben-Abdallah, APL
98, 243102 (2011).

Prospects

- To go beyond effective medium theory
- To consider simple thermalization problems
- Temperature in the surface ?

Lecture Notes in Physics 834

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...and thank you!