

Introducción a la información cuántica

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Instituto de Física Fundamental





CSID



CSI : C

www.csic.es



sobre el csic

actualidad

investigación

ciencia y
sociedad

fuentes
documentales

formación y
empleo

transferencia de
conocimiento

CONCLUYE LA VUELTA AL MUNDO DE MALASPINA

La expedición ha recogido 120.000 muestras que dejan un valioso legado a la comunidad científica

español | català | galego | euskara |



prensa intranet o

Consejo Superior de Investigación Científicas

[PERFIL DEL CONTRATANTE »](#)

[SEDE ELECTRÓNICA »](#)

PLAN DE ACTUACIÓN

La estrategia de la institución de 2010 a 2013

EJES ESTRATÉGICOS

Investigación transdisciplinar orientada a problemas

... LLEGA LA EXPEDICIÓN MALASPINA DE SU...



CSIC
CONSEJO SUPERIOR DE INVESTIGACIONES CIENTÍFICAS

IFF Instituto de Física Fundamental

► Quinfog

Miembros

Actividades

Publicaciones

Investigación

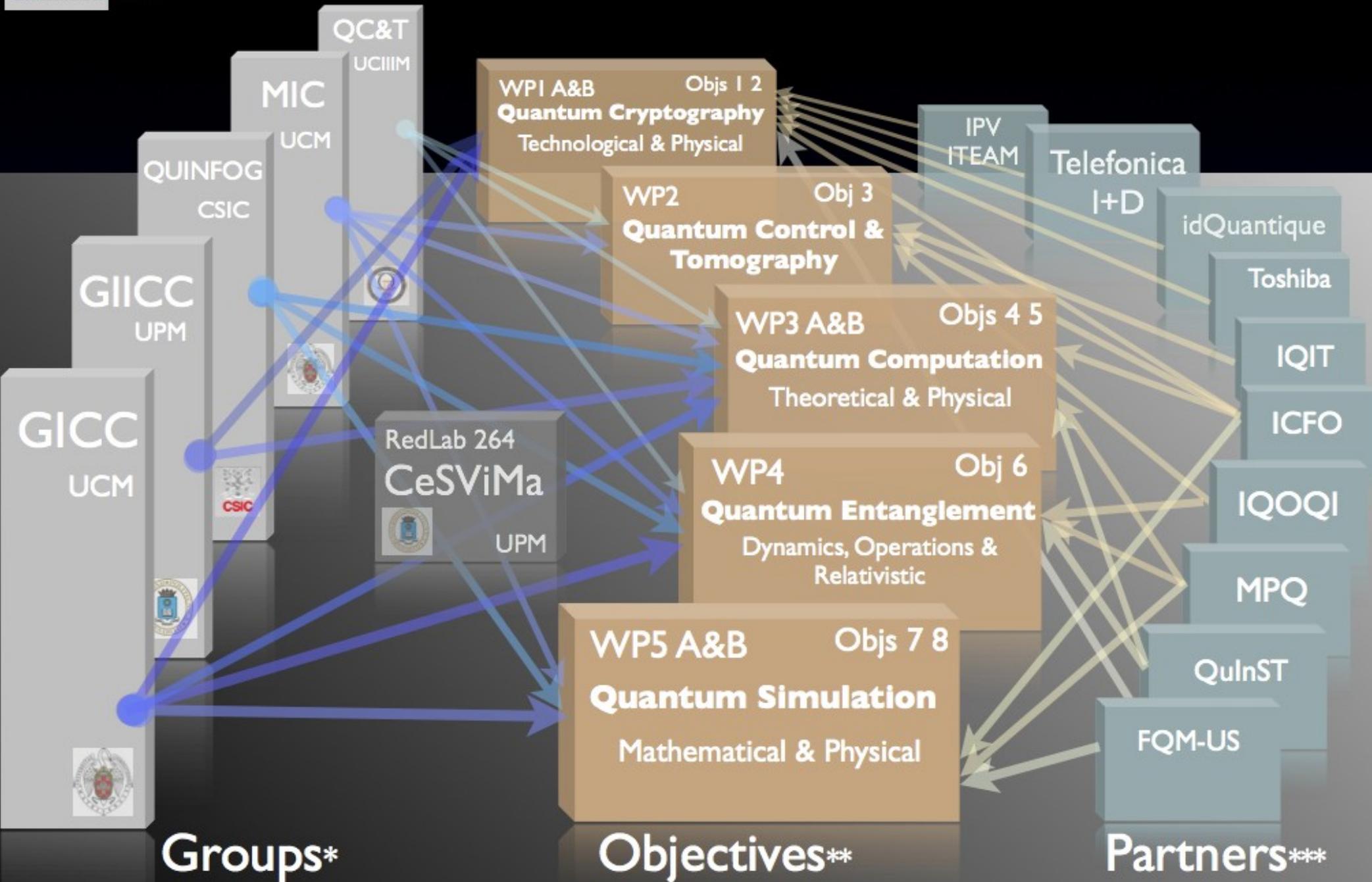


<http://quinfog.iff.csic.es>

*Brewing the best
quantum
information since
2005...*

Tres investigadores de plantilla,
6 doctorandos, 1 postdoc Marie Curie

QUITEMAD



Groups*

Objectives**

Partners***

*See the memory for the detailed composition of the groups

**Find objectives description Obj 1-8 at the attached memory

***Associated partners and laboratories



IDEAS



ESQUEMA

Información

Criptografía

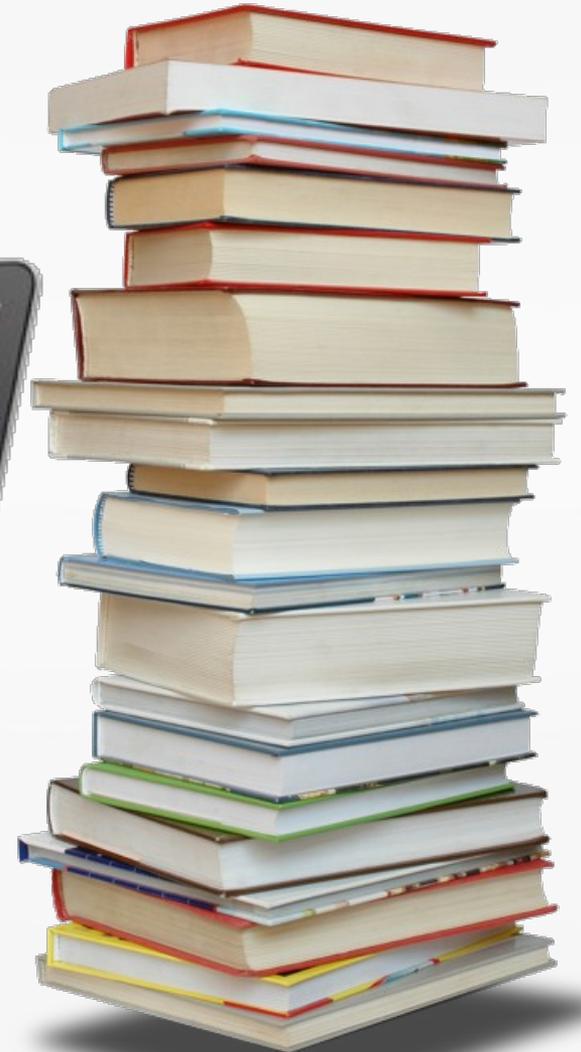
Computación Cuántica

Implementaciones

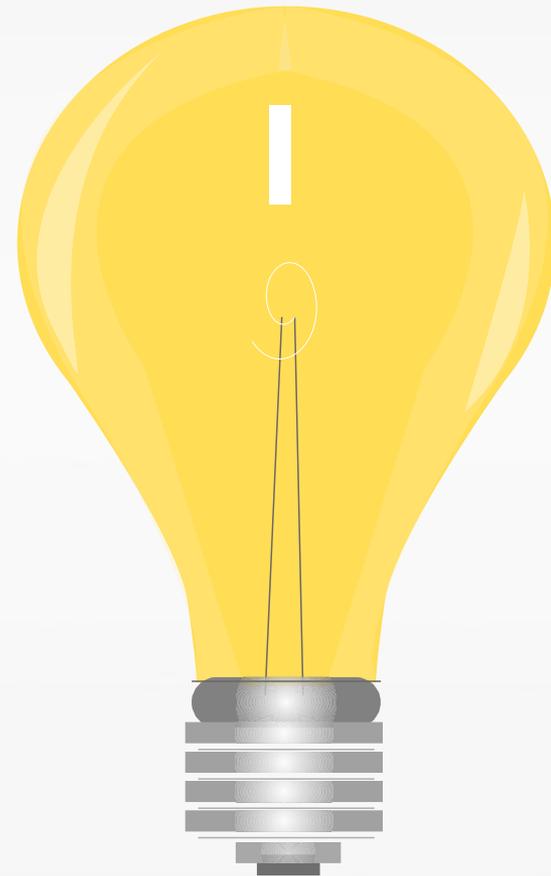
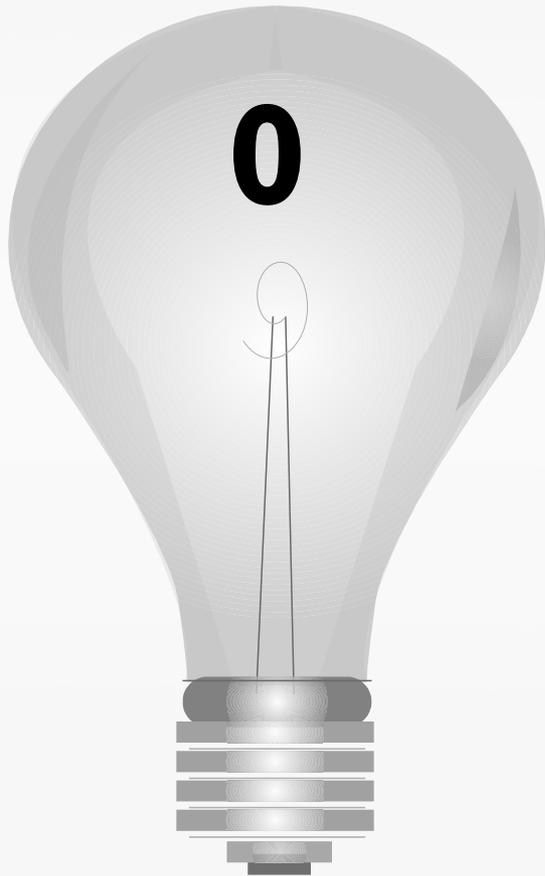
Circuitos cuánticos



INFORMACIÓN



INFORMACIÓN



INFORMACIÓN



= "4"



= "1"



= "EOT"



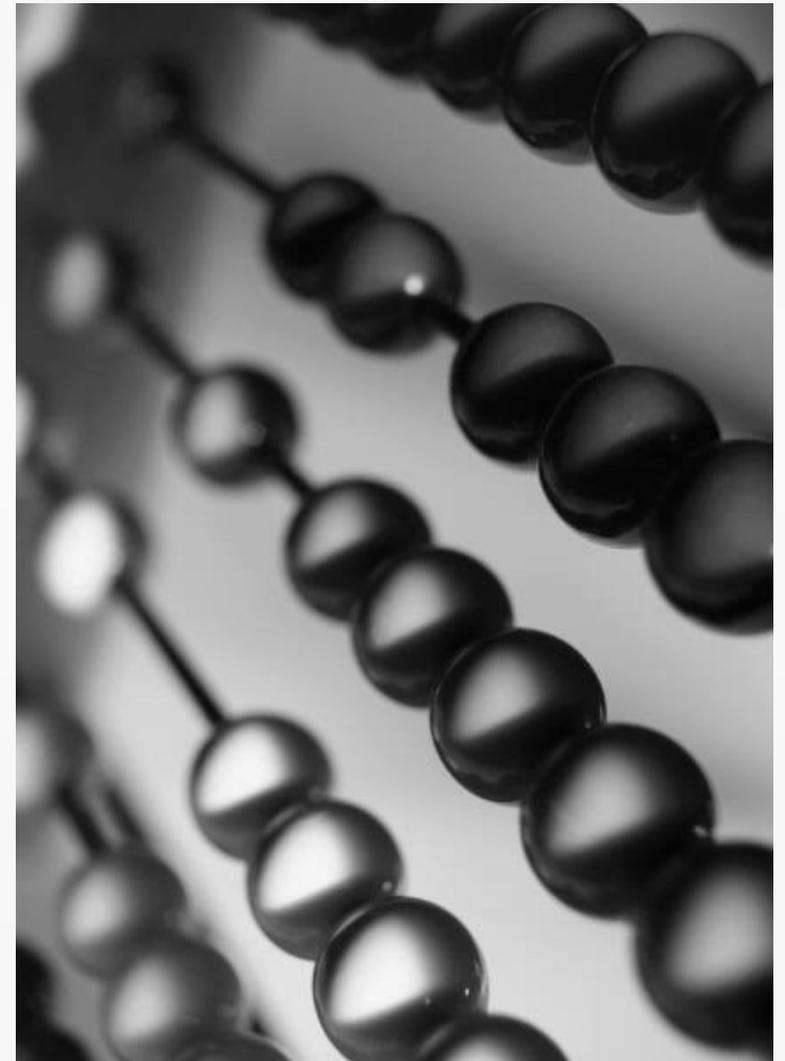
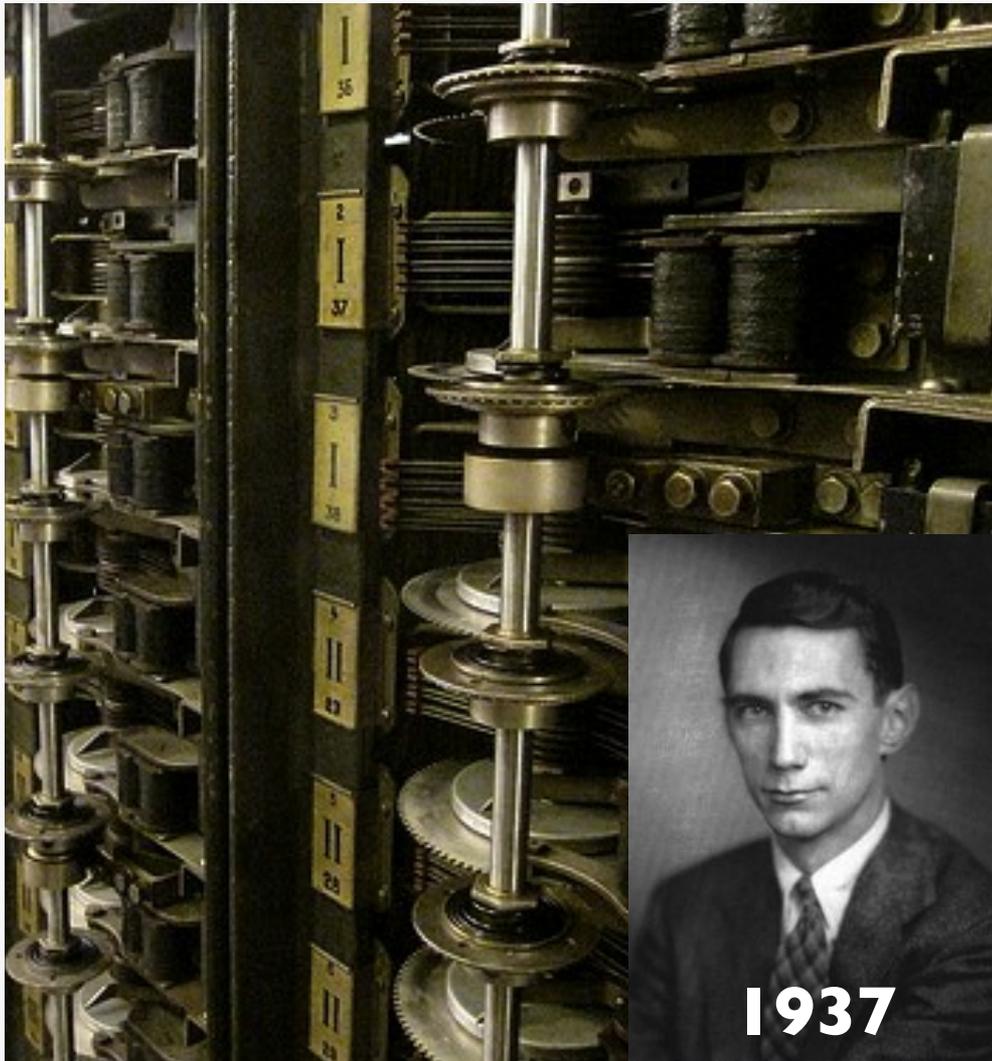
= "A"

INFORMACIÓN & FÍSICA



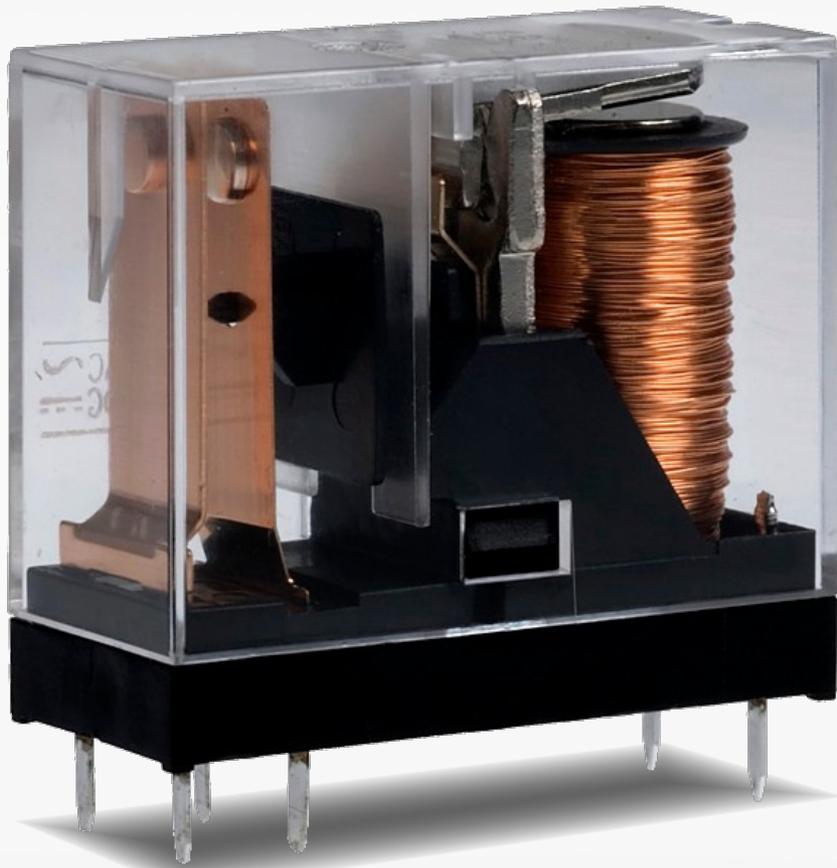
- La información es el soporte y sus estados.
- El soporte es físico.
- La información es física
- La física es información.

COMPUTACIÓN

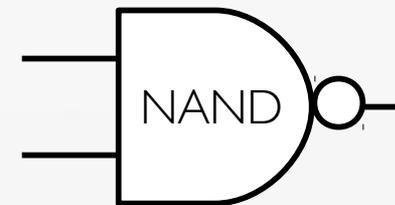


COMPUTACIÓN

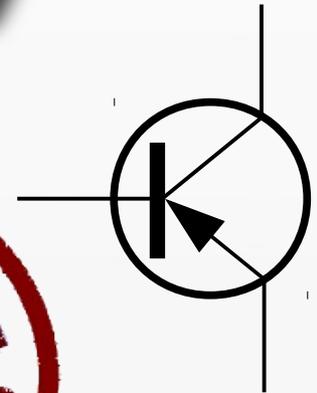
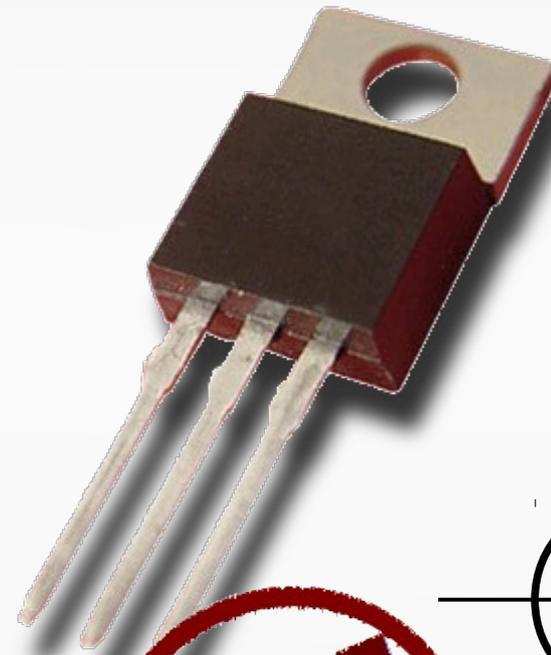
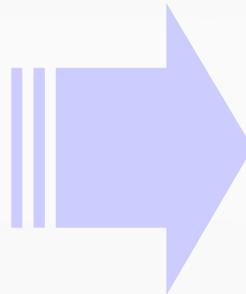
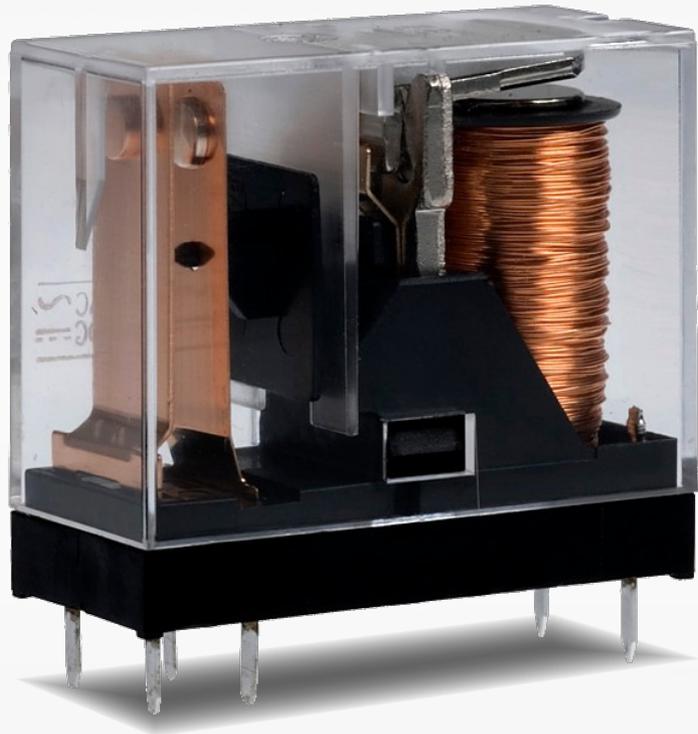
- Elemento de computación básico, puerta NAND



| A | B | C |
|---|---|---|
| 0 | 0 | 1 |
| 0 | 1 | 1 |
| 1 | 0 | 1 |
| 1 | 1 | 0 |

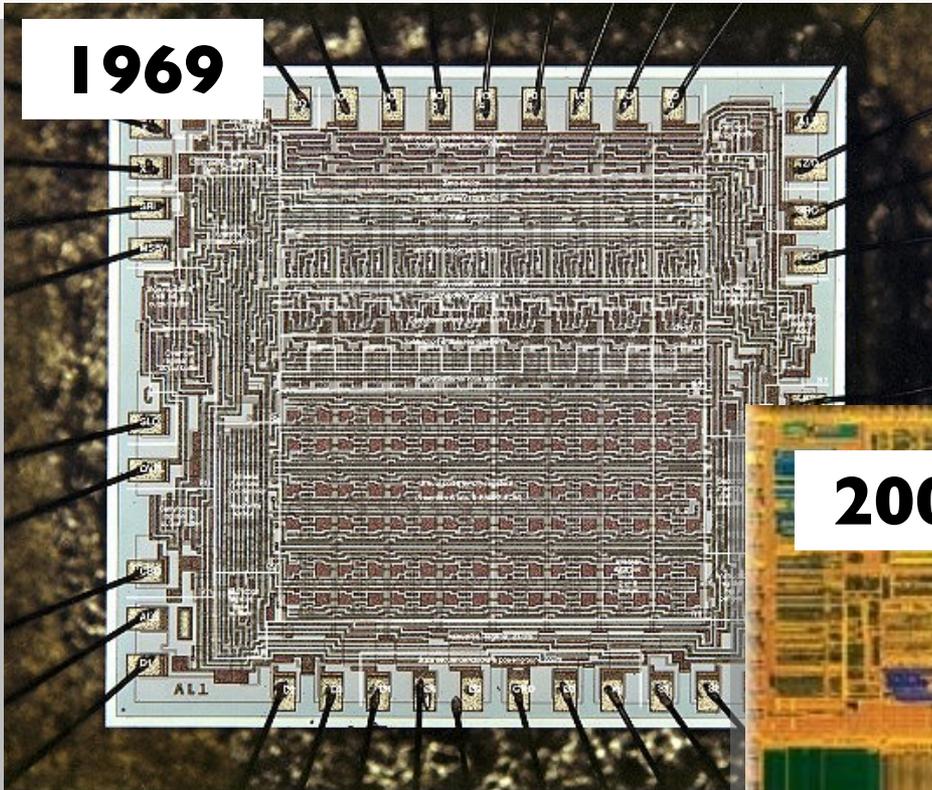


TRANSISTOR

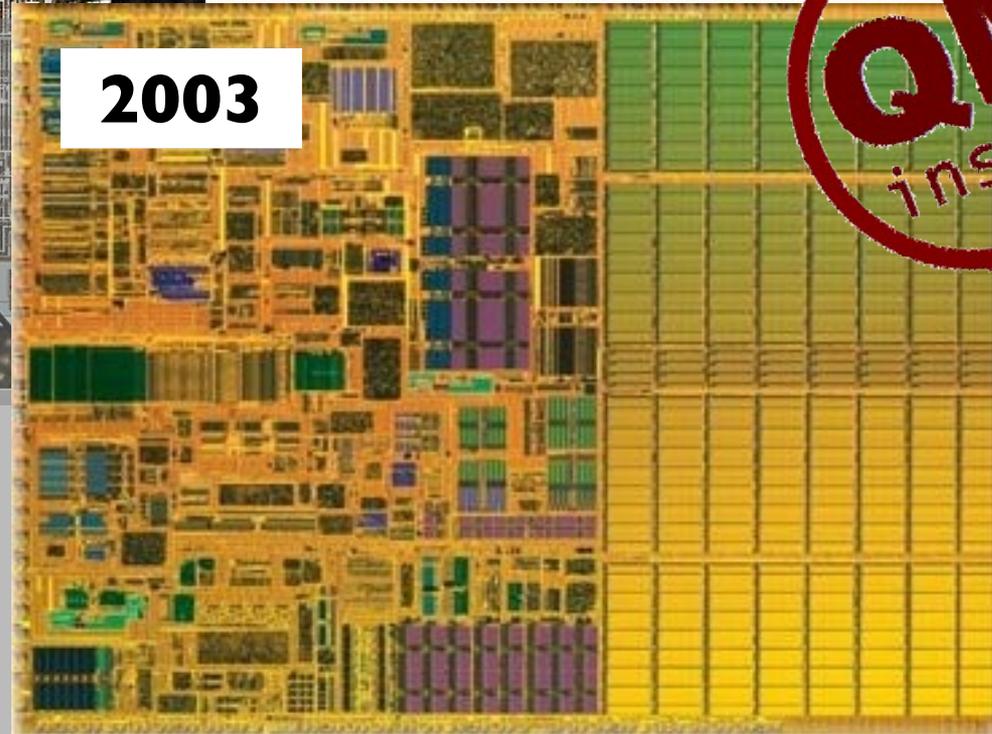


CIRCUITOS INTEGRADOS

1969



2003



LEY DE MOORE

Transistors
Per Die

10^{10}

10^9

10^8

10^7

10^6

10^5

10^4

10^3

10^2

10^1

10^0

1960

1965

1970

1975

1980

1985

◆ 1965 Actual Data

■ MOS Arrays ▲ MOS Logic 1975 Actual Data

● 1975 Projection

■ Memory

▲ Microprocessor

1K

4K

16K

4004

8080

8086

80286

i386™

1M

i486™

4M

16M

64M

128M

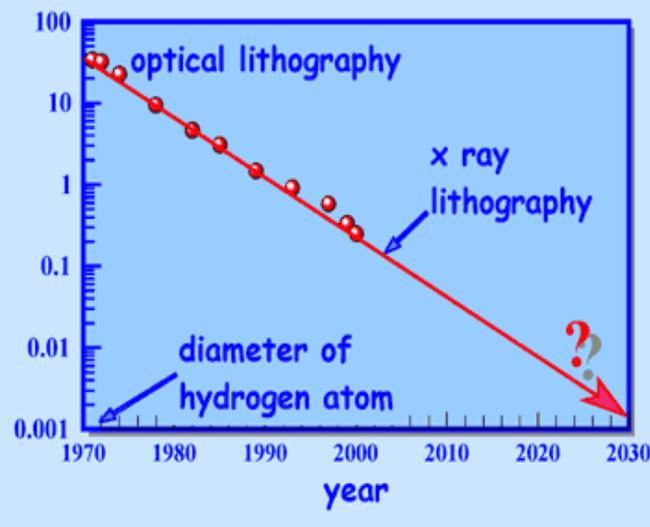
256M

512M

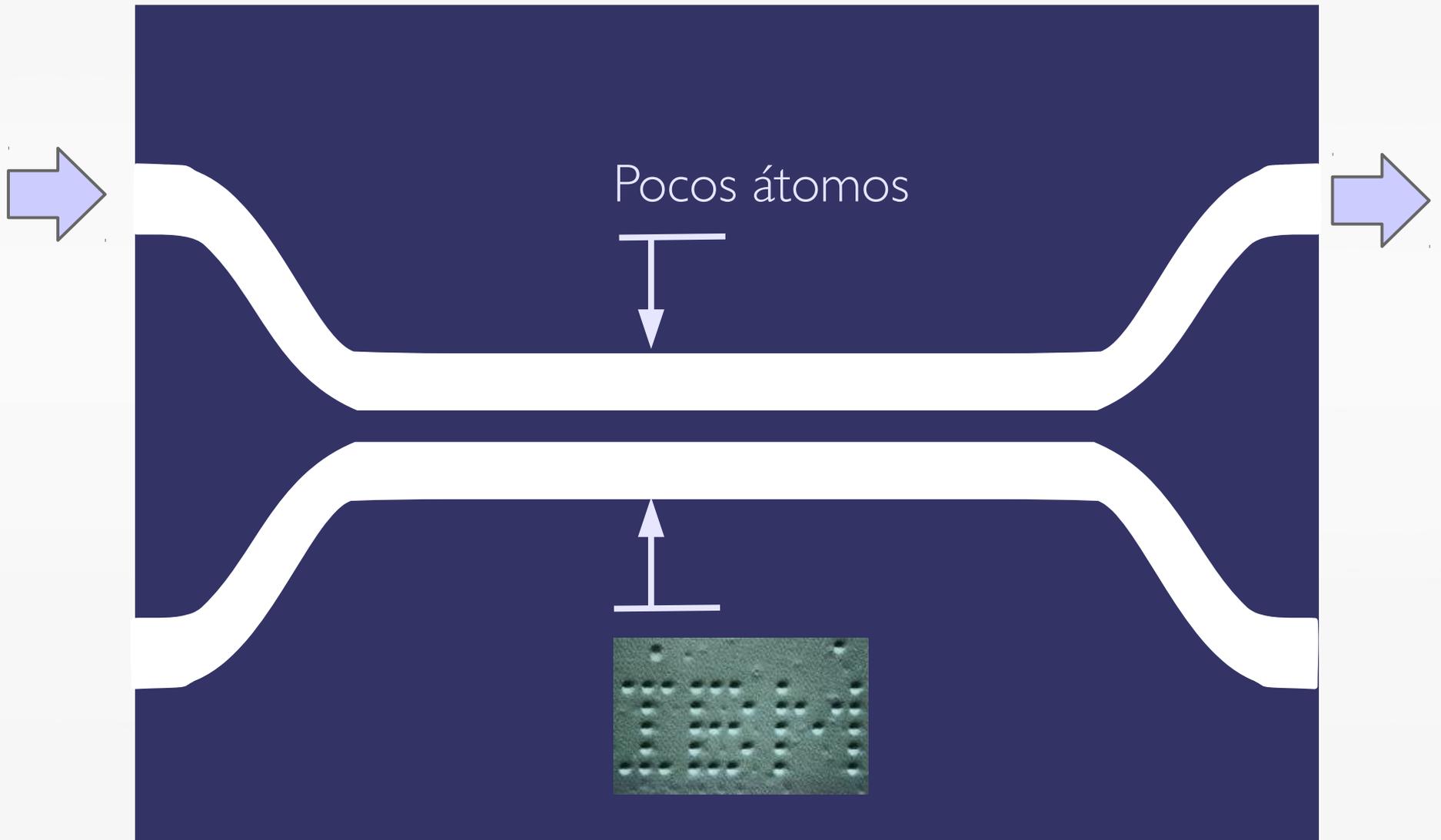
1G

2G

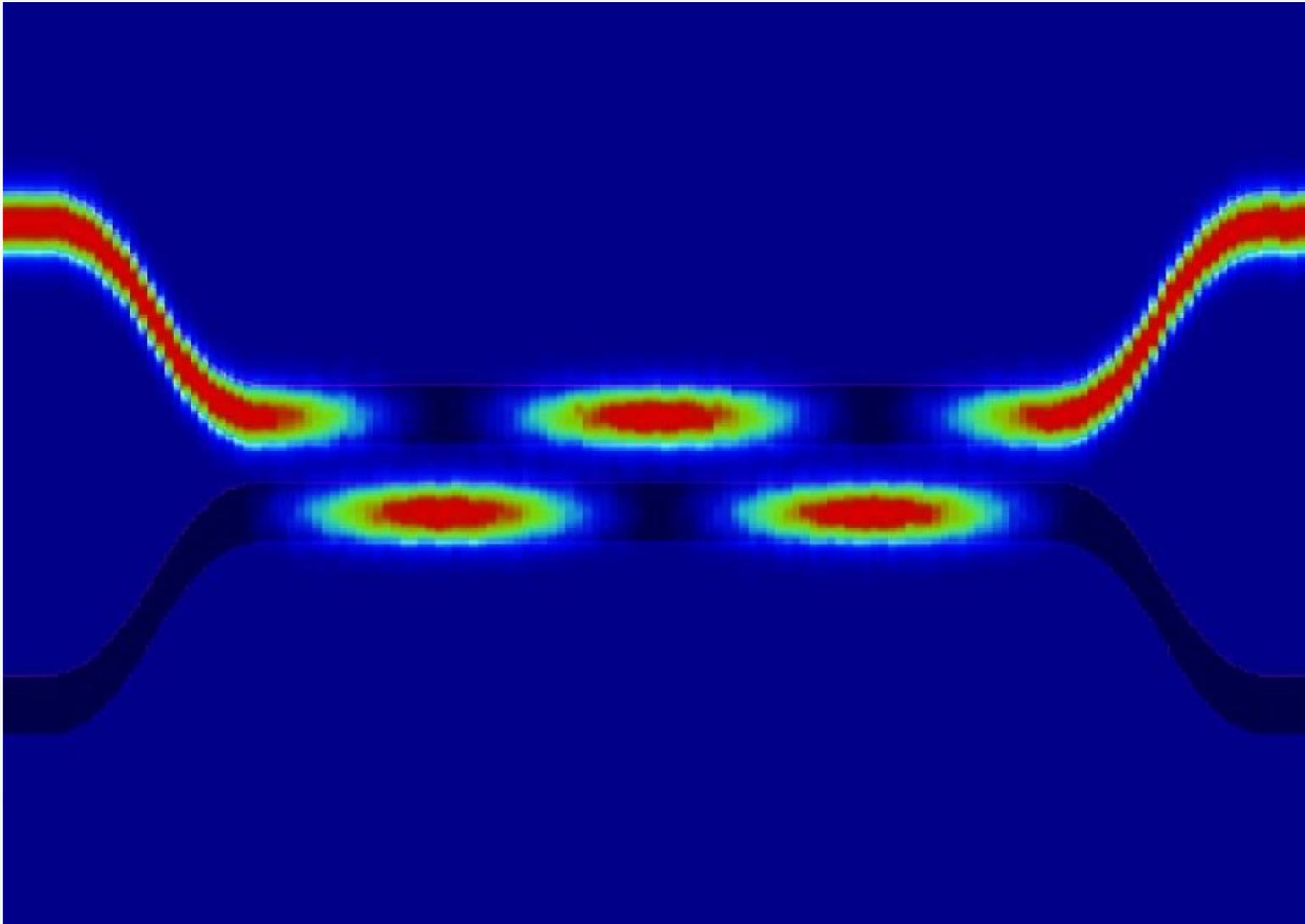
4G



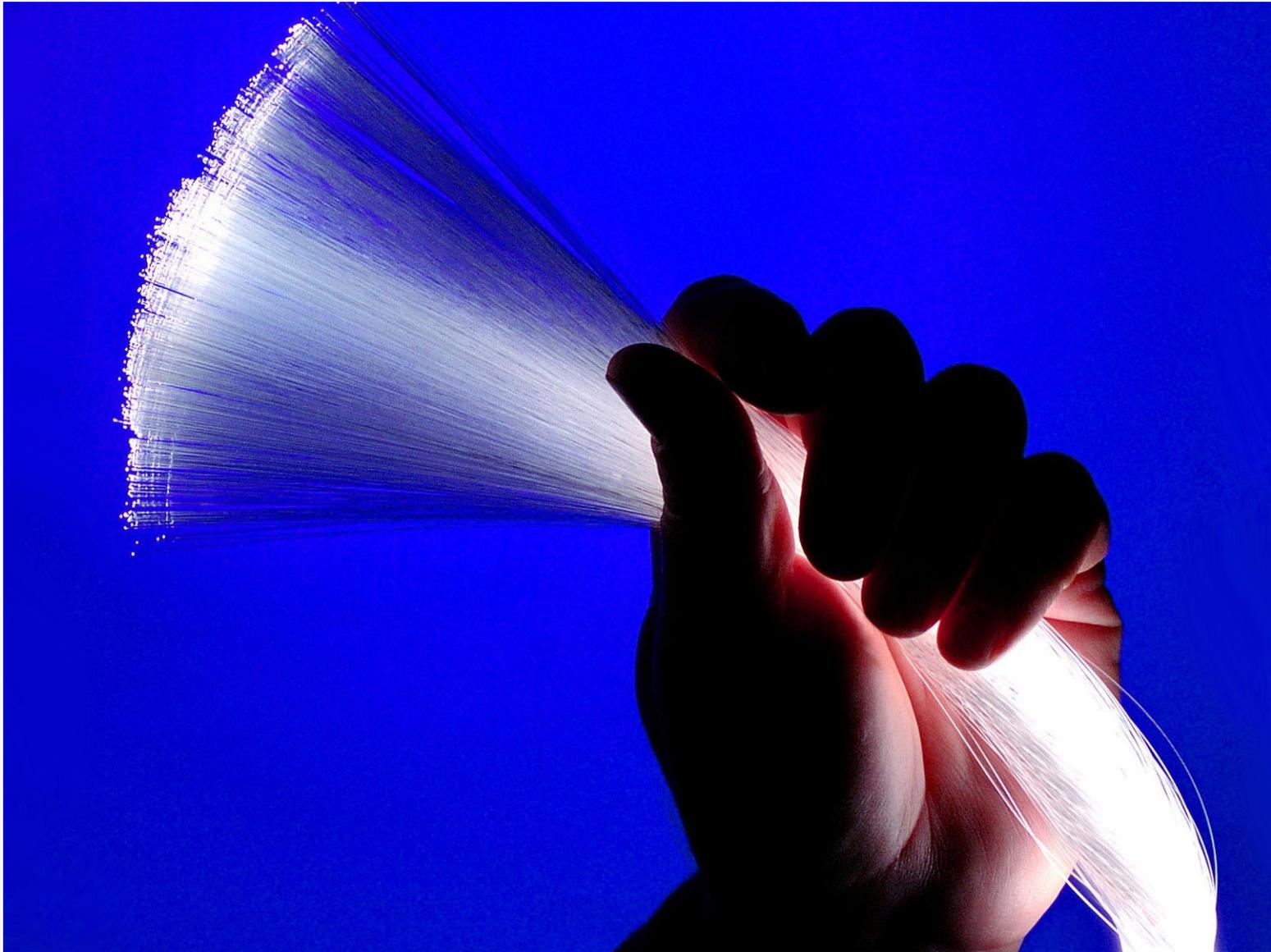
NANOCIRCUITOS



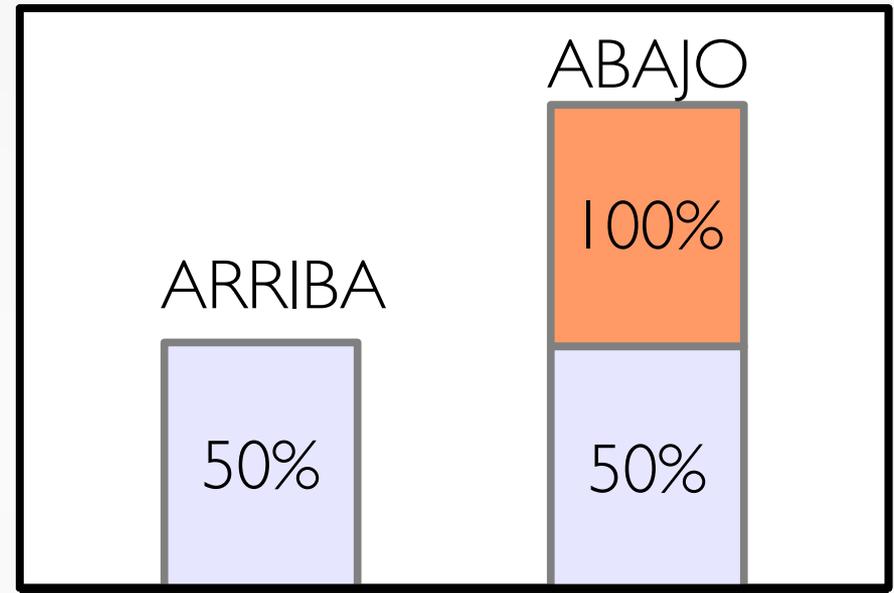
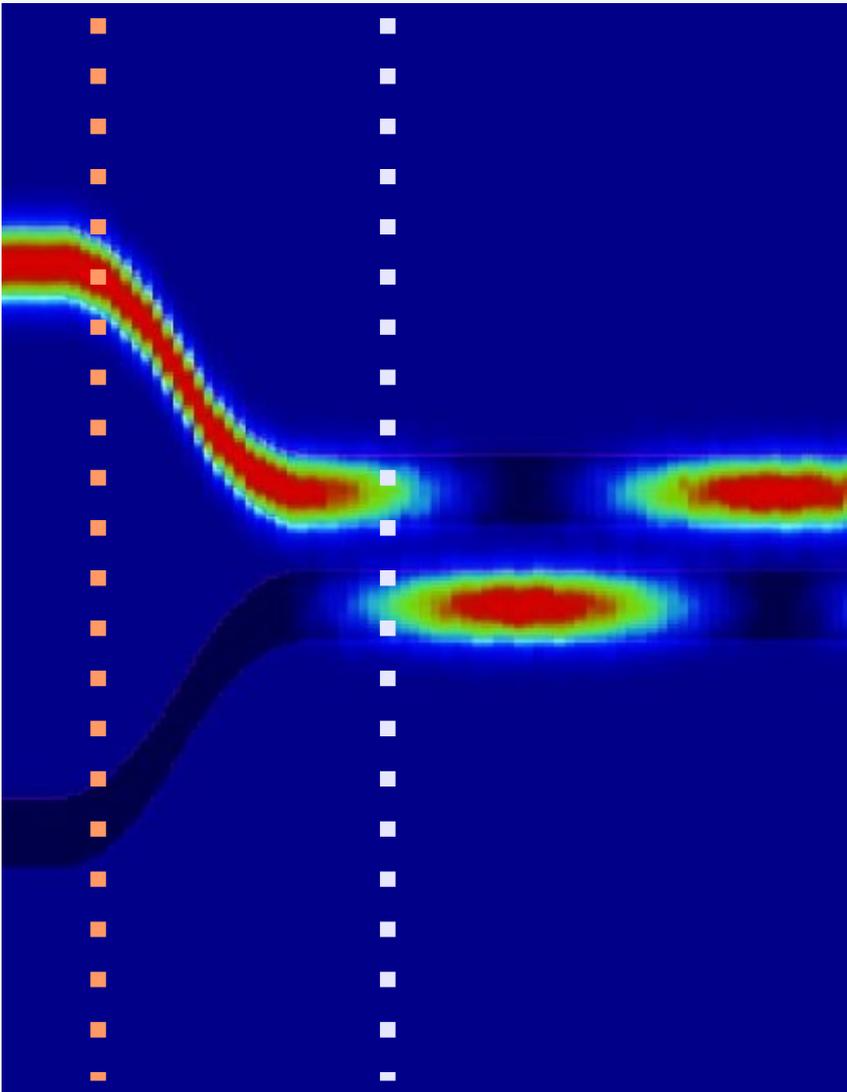
TUNEL CUÁNTICO



ONDAS



INCERTIDUMBRE

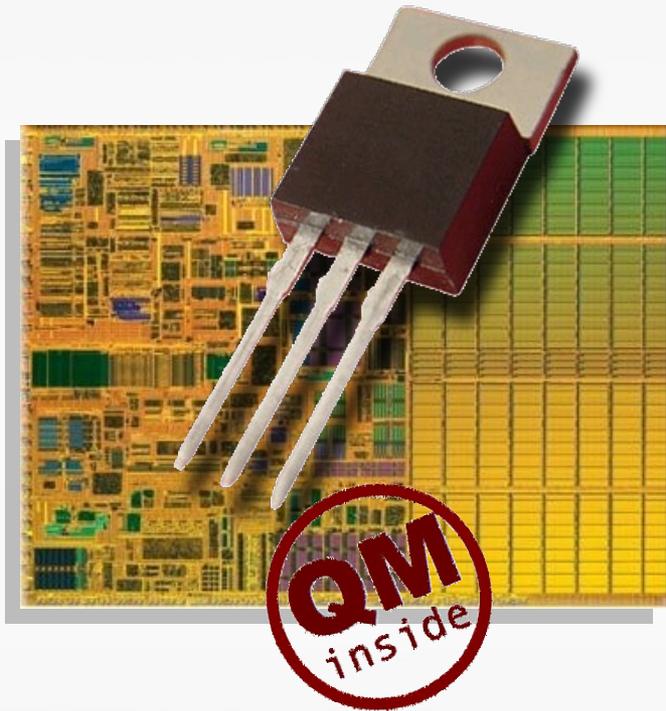


Los estados cuánticos se definen a partir de distribuciones de probabilidad.

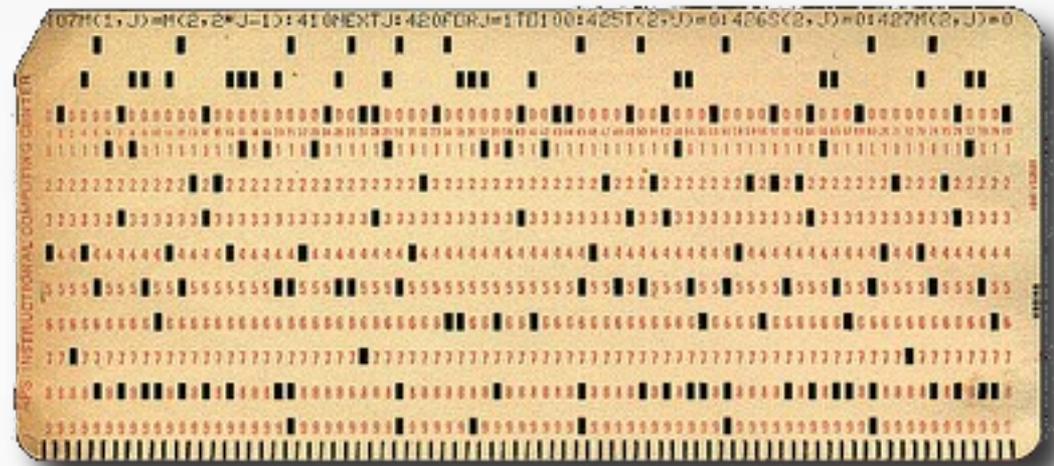
~~PROBLEM~~

OPPORTUNITY

ORDENADORES



ORDENADORES



Tratamos a nuestros dispositivos cuánticos como objetos clásicos.

Mecánica Cuántica

Criptografía Cuántica

Comunicación Cuántica

Computación Cuántica

Simulación Cuántica

Modelos de circuitos

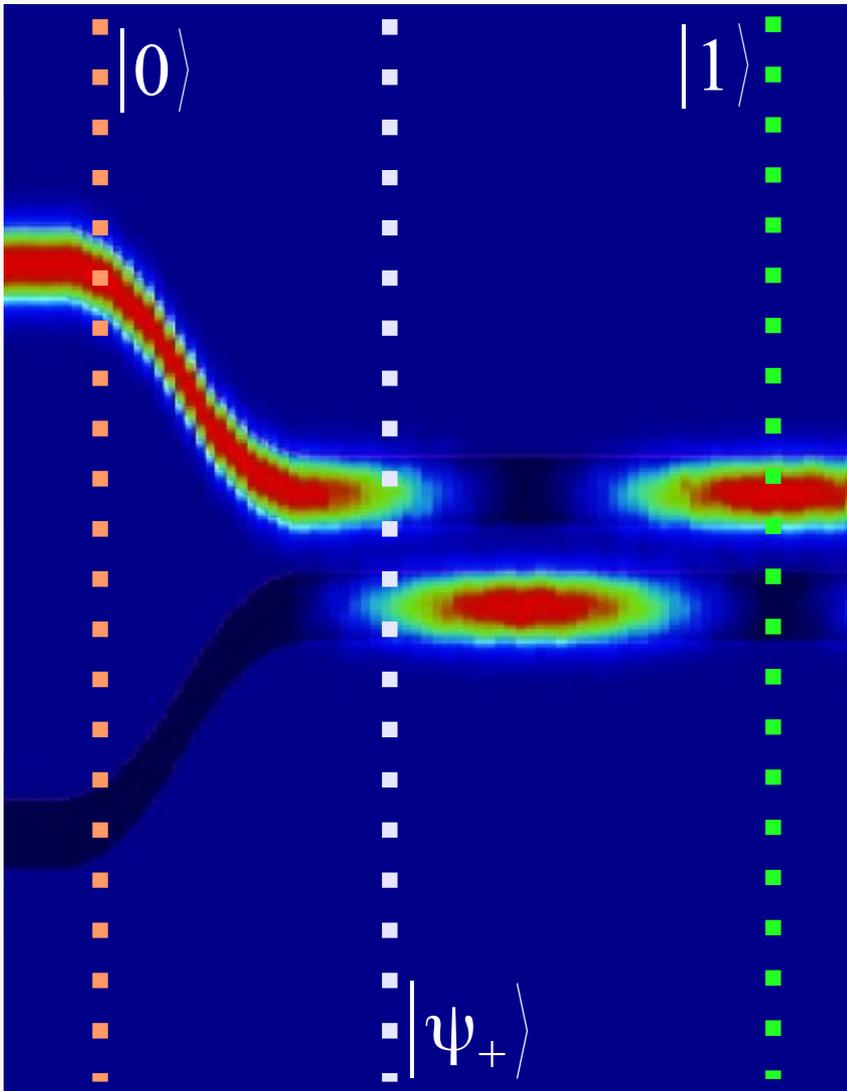
Computación topológica

Computación adiabática

Computación con medidas

Información cuántica

QUBIT



- Un sistema con dos estados disponibles, 0 y 1
- Se pueden crear los estados puros y superposición

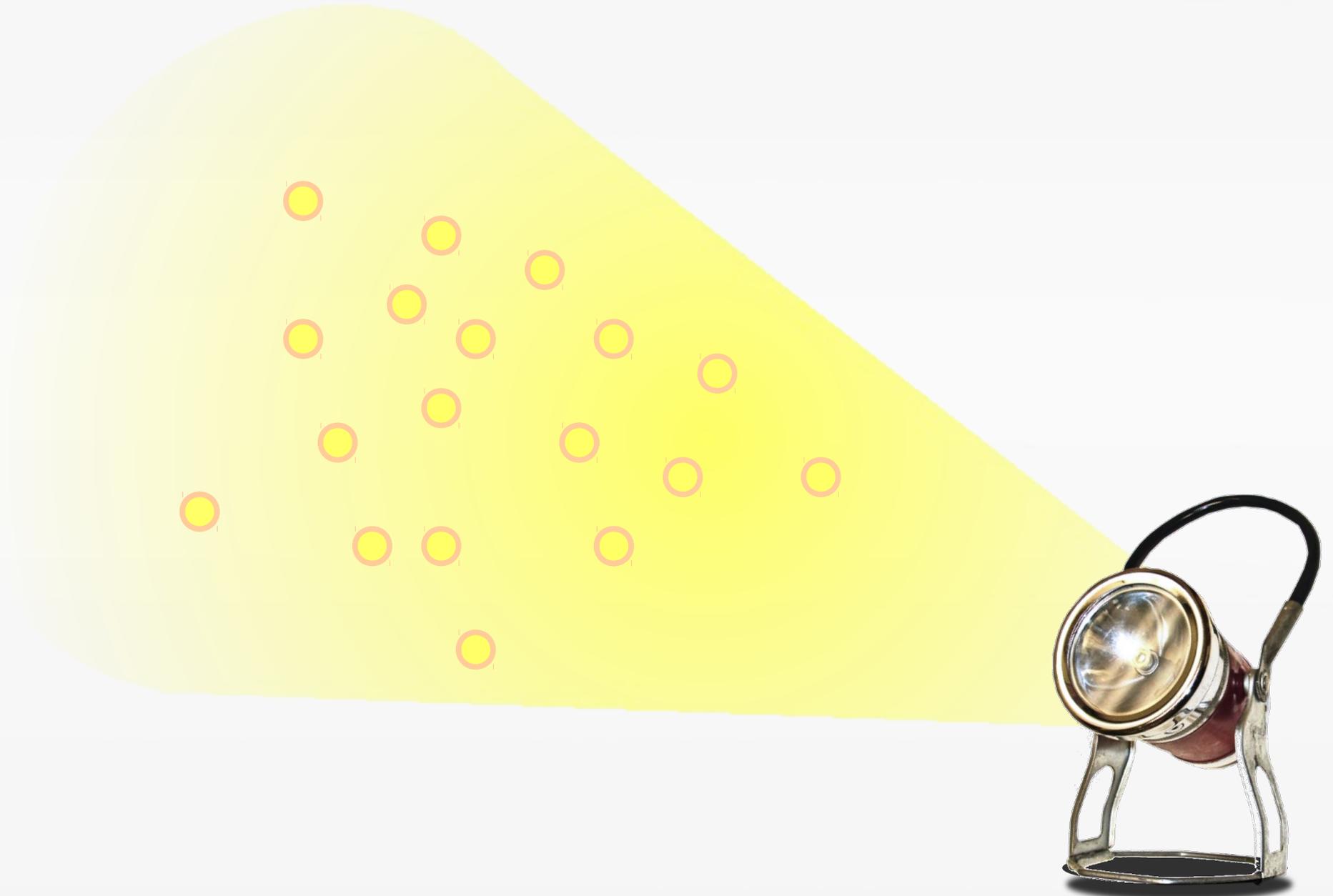
$$|\psi_+\rangle = \frac{1}{\sqrt{2}}|0\rangle + \frac{1}{\sqrt{2}}|1\rangle$$

$$|\psi_-\rangle = \frac{1}{\sqrt{2}}|0\rangle - \frac{1}{\sqrt{2}}|1\rangle$$

$$\frac{1}{\sqrt{2}} \times \frac{1}{\sqrt{2}} = \frac{1}{2} = 50\%$$

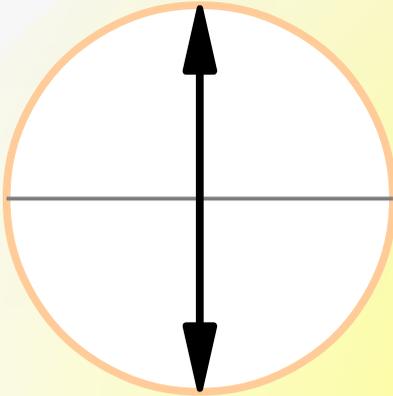
An arrow points from the 50% result to the $|\psi_-\rangle$ equation above.

FOTONES

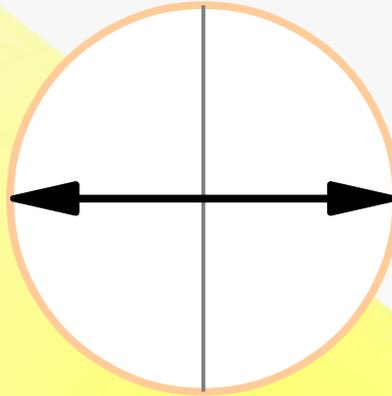


FOTONES

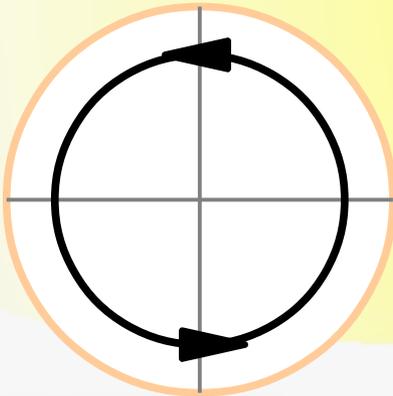
Vertical



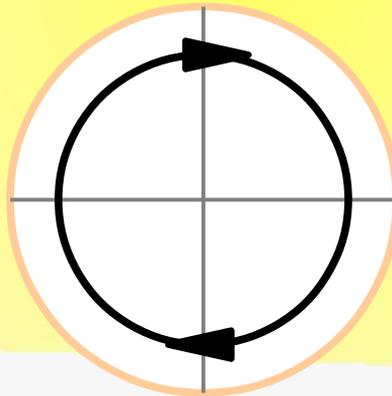
Horizontal



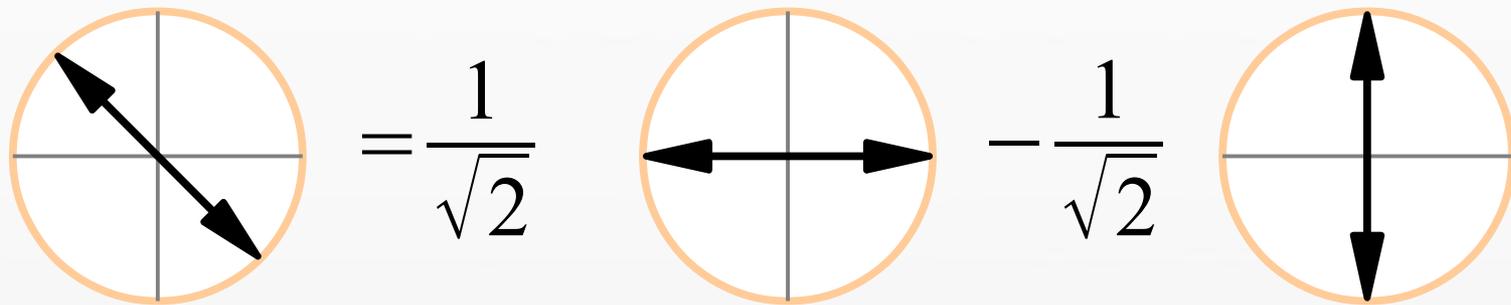
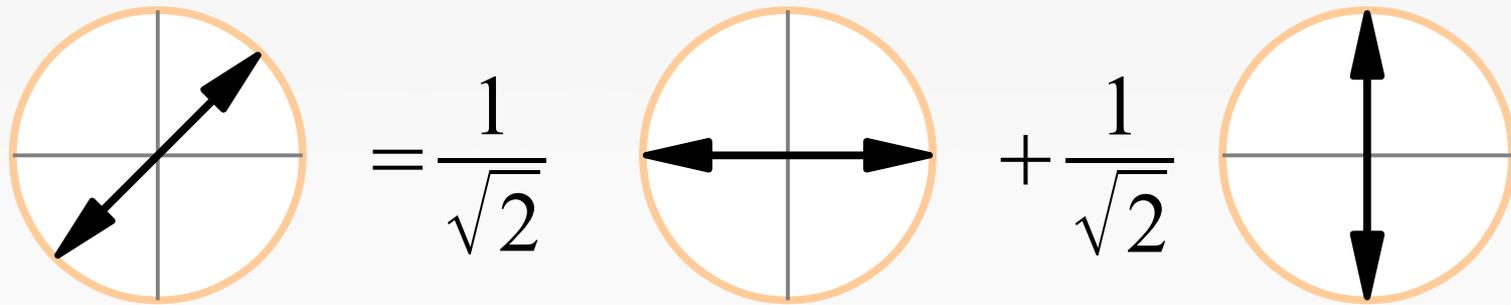
Izquierda



Derecha

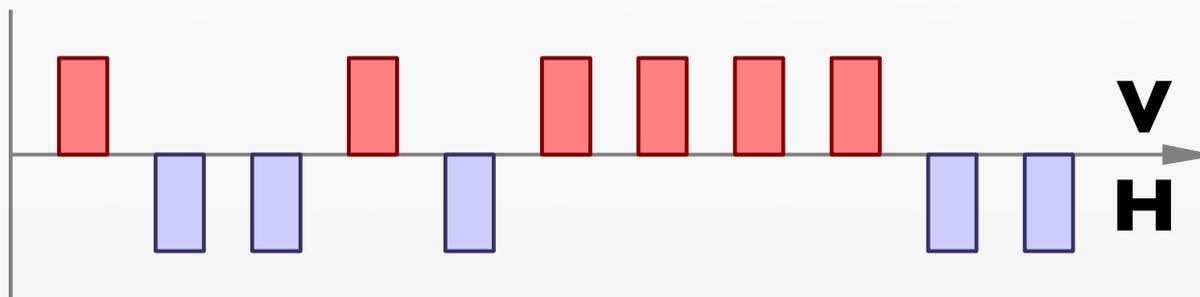
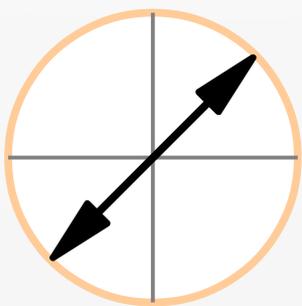
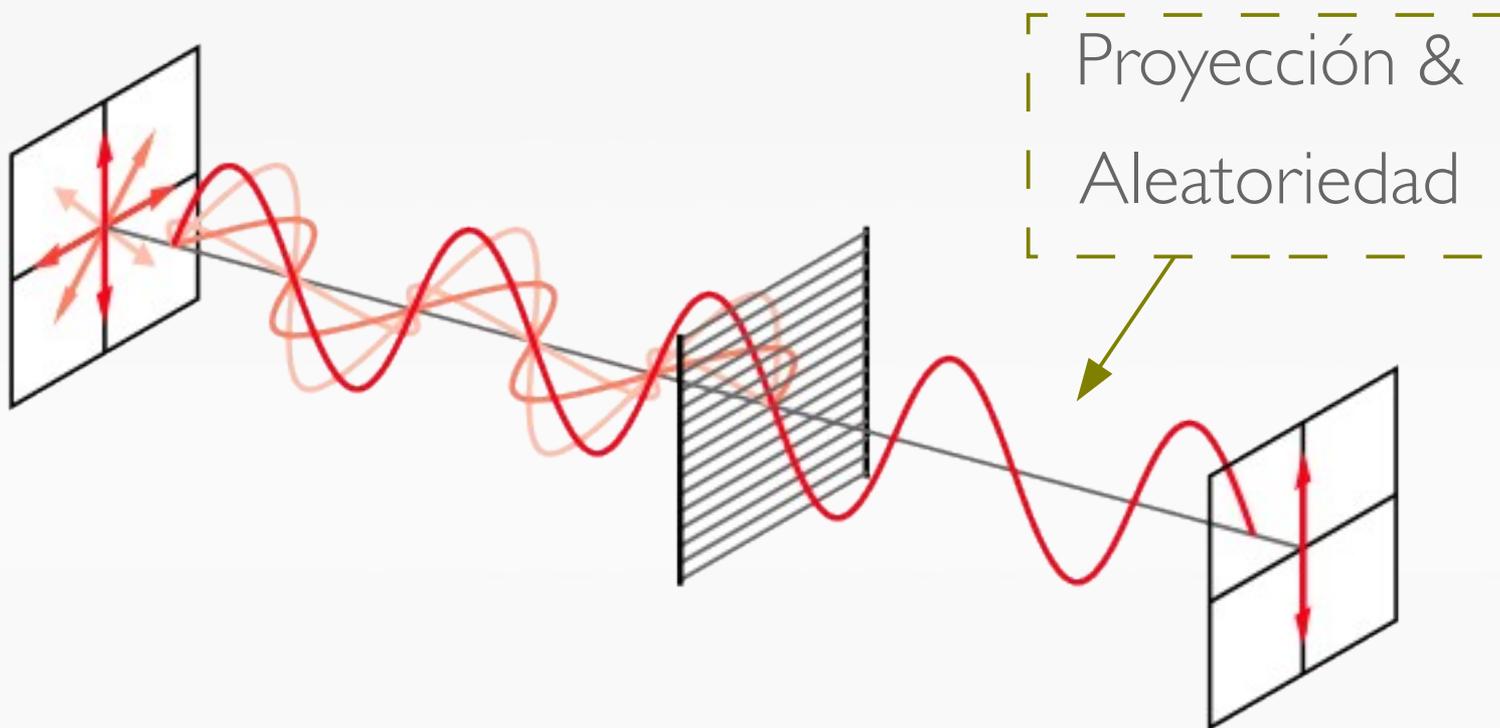


FOTONES



Superposición “cuántica”

MEDIDA

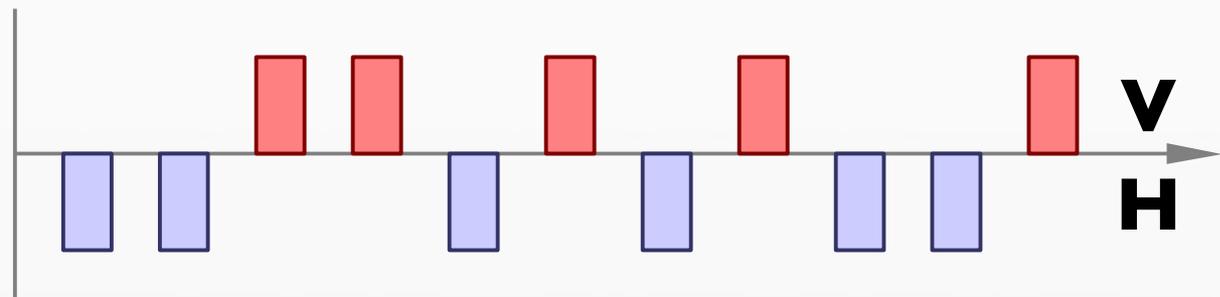
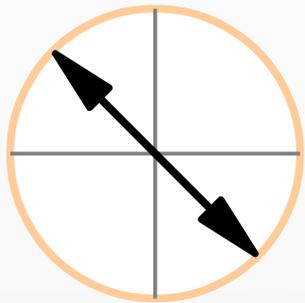
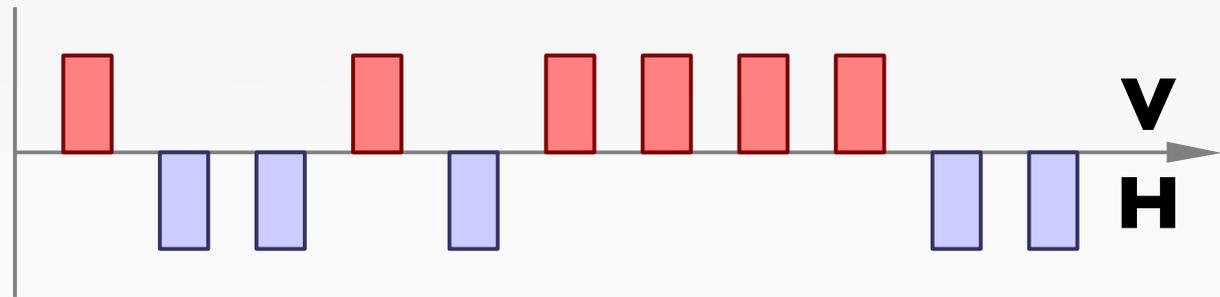
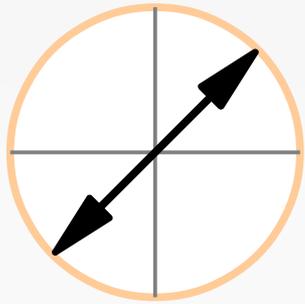


QM CHURCH



- Quantum phenomena do not occur in a Hilbert space, they occur in a laboratory.
- Quantum theory needs no 'interpretation'.
- Unperformed experiments have no results.
- Never underestimate the ingenuity of experimental physicists.

INDETERMINACIÓN



Medidas en una “base” no sirven para distinguir estados creados en otra base

Criptografía cuántica

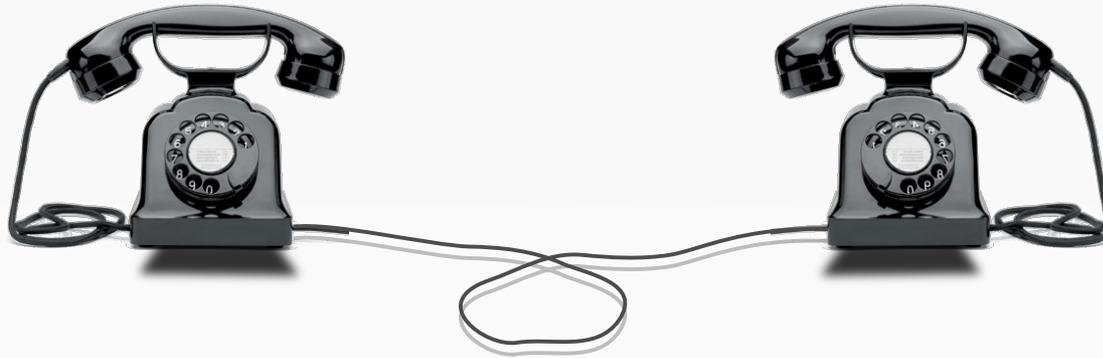
CRIPTOGRAFÍA



CRIPTOGRAFÍA



CRIPTOGRAFÍA



CLAVE PRIVADA



0 0 0 1 0 0 1 0 0 0 0 ...

Mensaje

1 0 1 1 1 0 0 1 1 0 1 ...

Q Key



1 0 1 0 1 0 1 1 1 0 1 ...

Transmisión



0 0 0 1 0 0 1 0 0 0 0 ...

0 0 0 1 0 0 1 0 0 0 0 ...



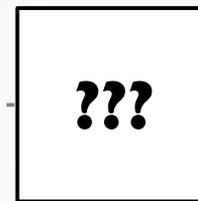
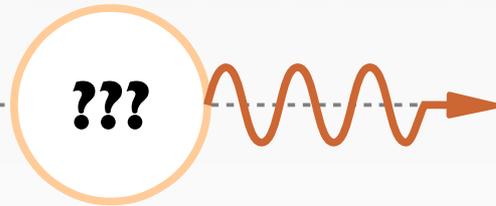
1 0 1 0 1 0 1 1 1 0 1 ...



1 0 1 1 1 0 0 1 1 0 1 ...



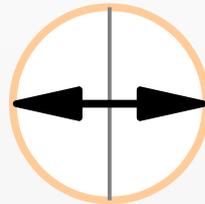
CRIPTOGRAFÍA



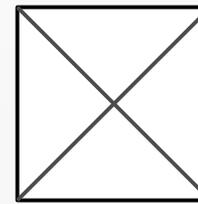
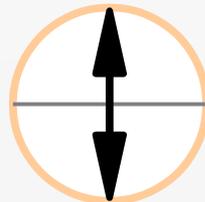
Base A

Base B

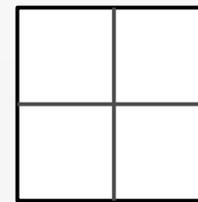
Valor 0



Valor 1



Medida A



Medida B

CRIPTOGRAFÍA

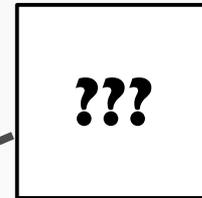
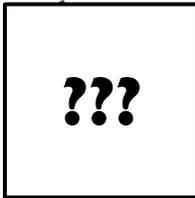
- Angela escoge una base (A/B) y un valor (0/1) aleatoriamente.
- Sarko escoge una base (A/B) aleatoriamente
- El fotón se envía y mide.
- Se repite muchas veces.
- A y S comunican las bases.
- Se guardan los bits sólo cuyas bases coinciden.



CRIPTOGRAFÍA

| Base A | Base S. | Emitid o | Recibi do | OK? |
|-------------------|--------------------|---------------------|----------------------|------------|
| A | A | | | ✓ |
| A | B | 0 | | ✗ |
| B | A | | 0 | ✗ |
| A | A | | | ✓ |
| B | A | 0 | 0 | ✗ |
| B | B | 0 | 0 | ✓ |
| B | A | | 0 | ✗ |
| A | A | | | ✓ |
| B | A | 0 | 0 | ✗ |

SEGURIDAD

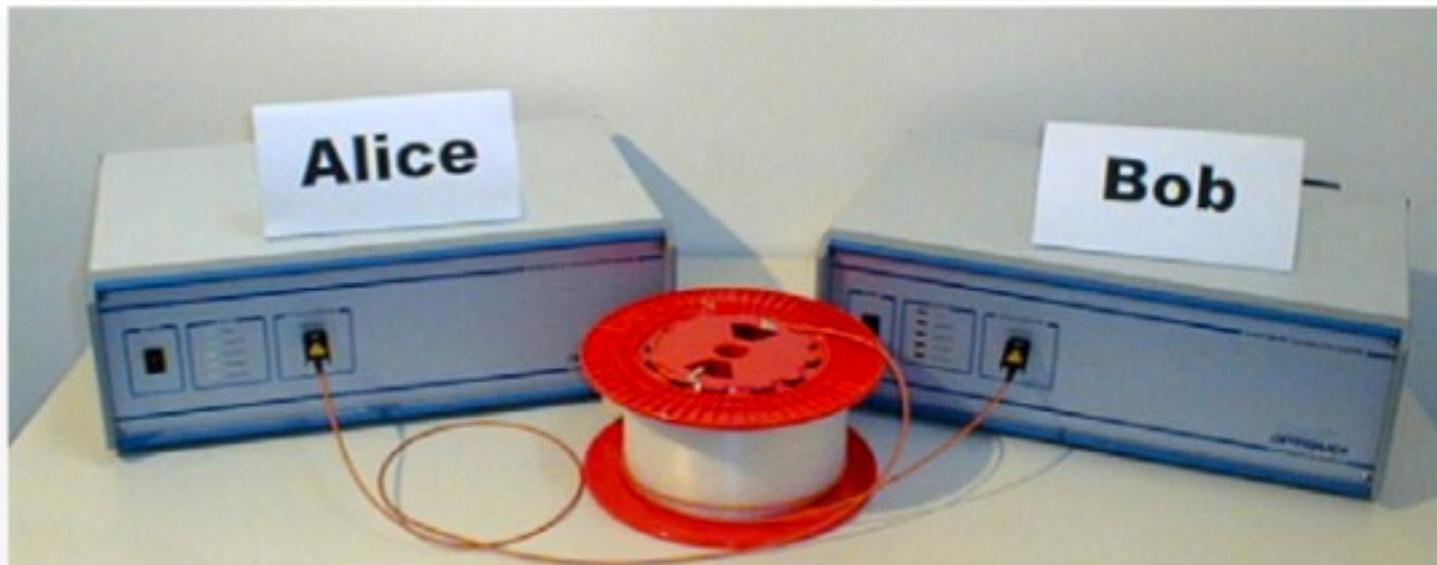
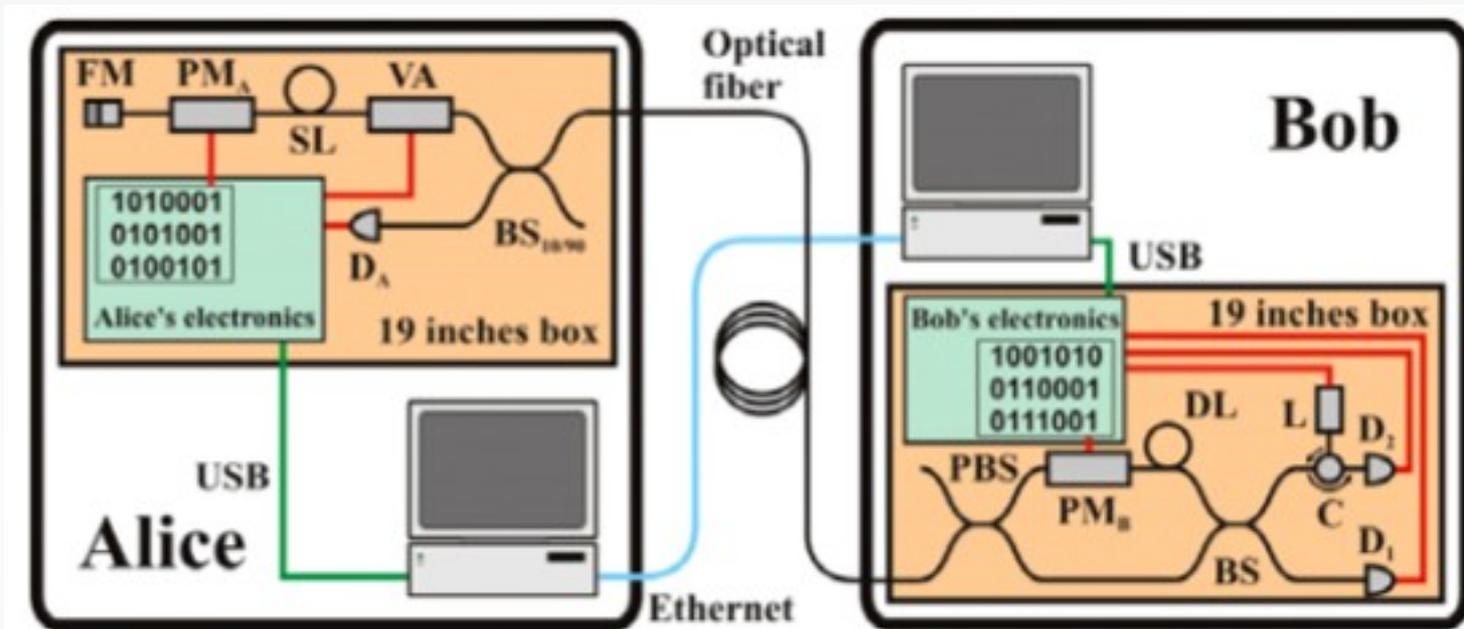


Cualquier medida destruye el estado original.



A y S reciben bits descorrelacionados: ruido blanco.

DISPOSITIVOS



DISPOSITIVOS





USER CASE

REDEFINING SECURITY

Geneva Government

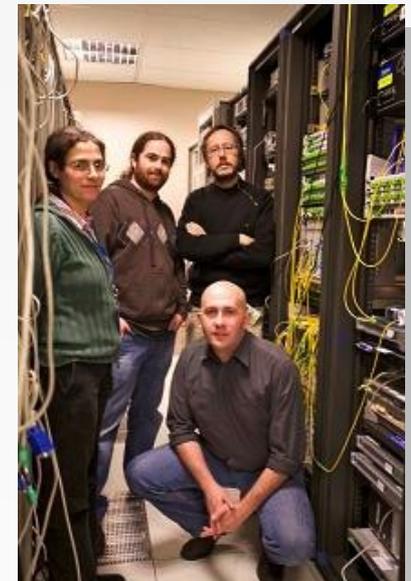
Secure Data Transfer for Elections

Gigabit Ethernet Encryption with Quantum Key Distribution



REPUBLIC
AND STATE
OF GENEVA

POST TENEBRAS LUX



USER CASE

REDEFINING SECURITY

Global Bank

IDQ Secures Global Wide Area Network

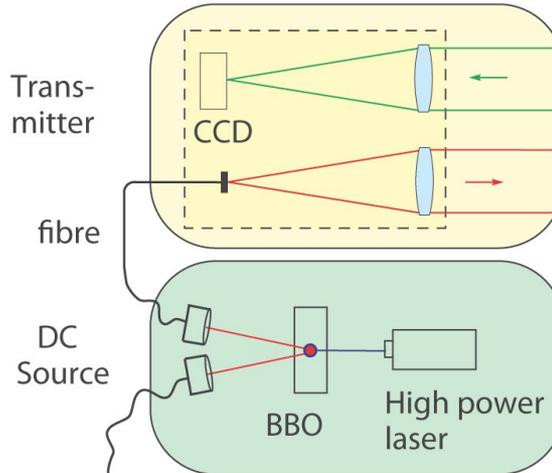
Multipoint 100 Megabit Ethernet Encryption



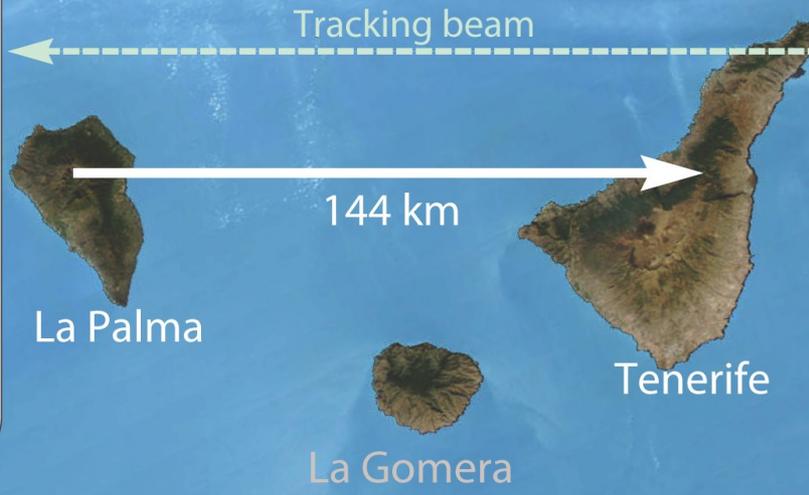
POLITÉCNICA

Telefonica

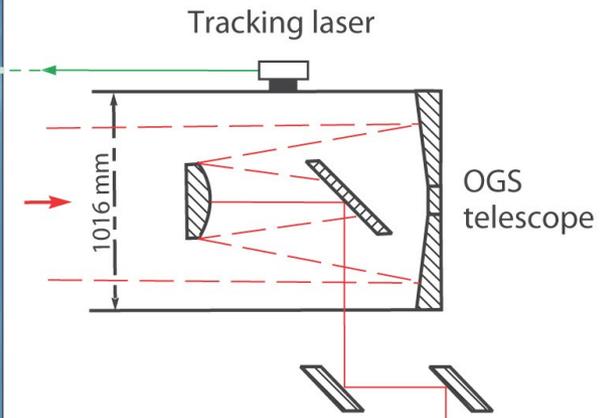
Source and Transmitter



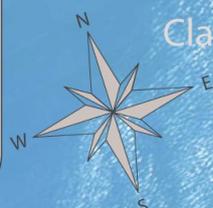
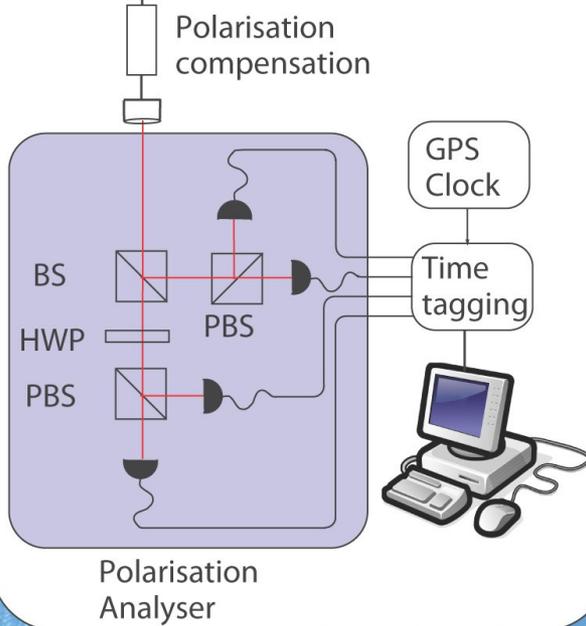
Tracking beam



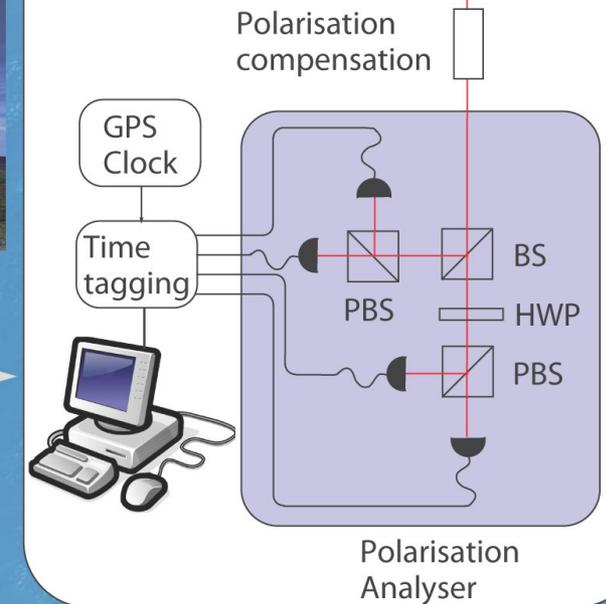
Optical Ground Station



Alice on La Palma



Bob on Tenerife

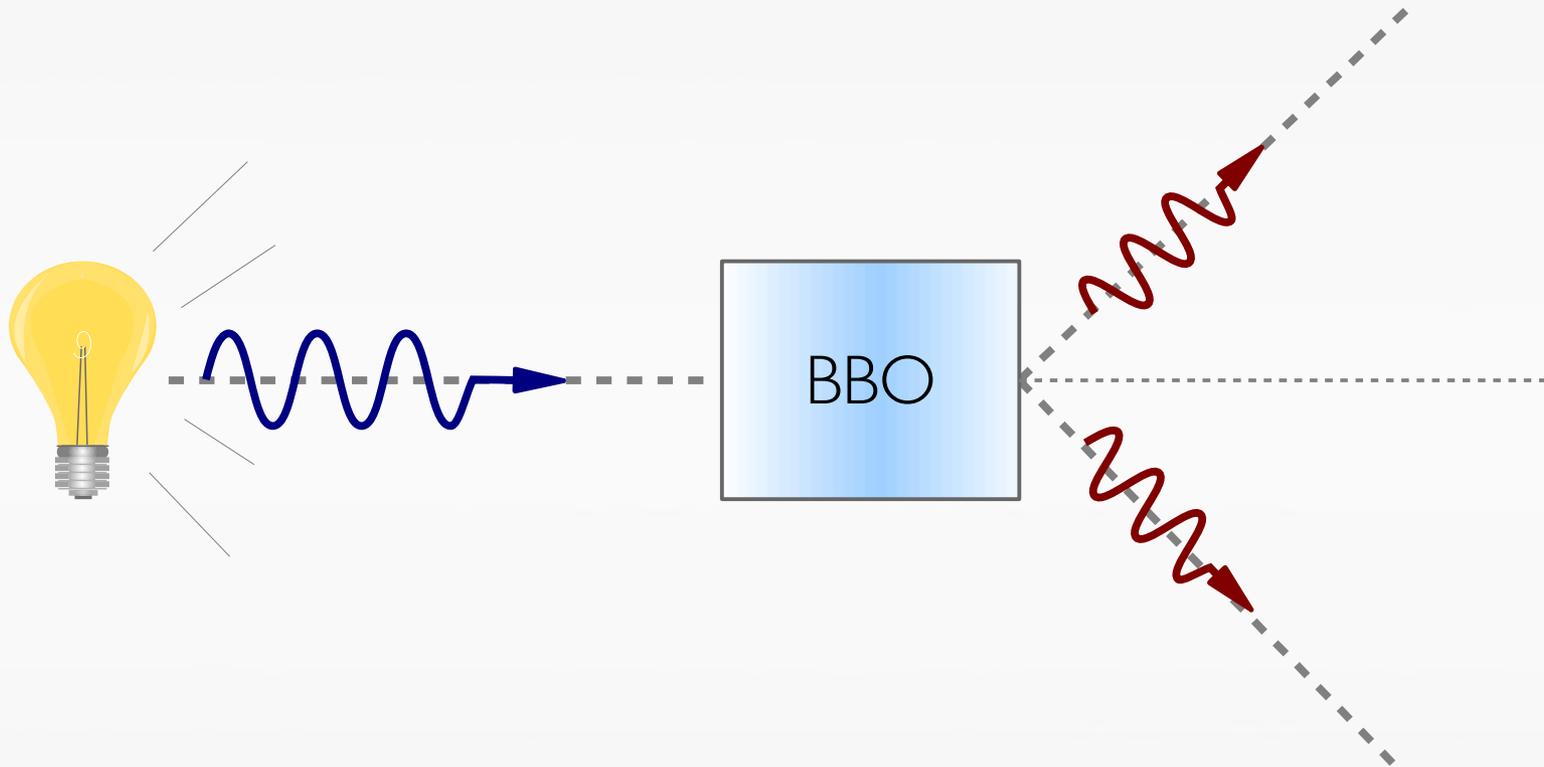


Entrelazamiento

CORRELACIONES

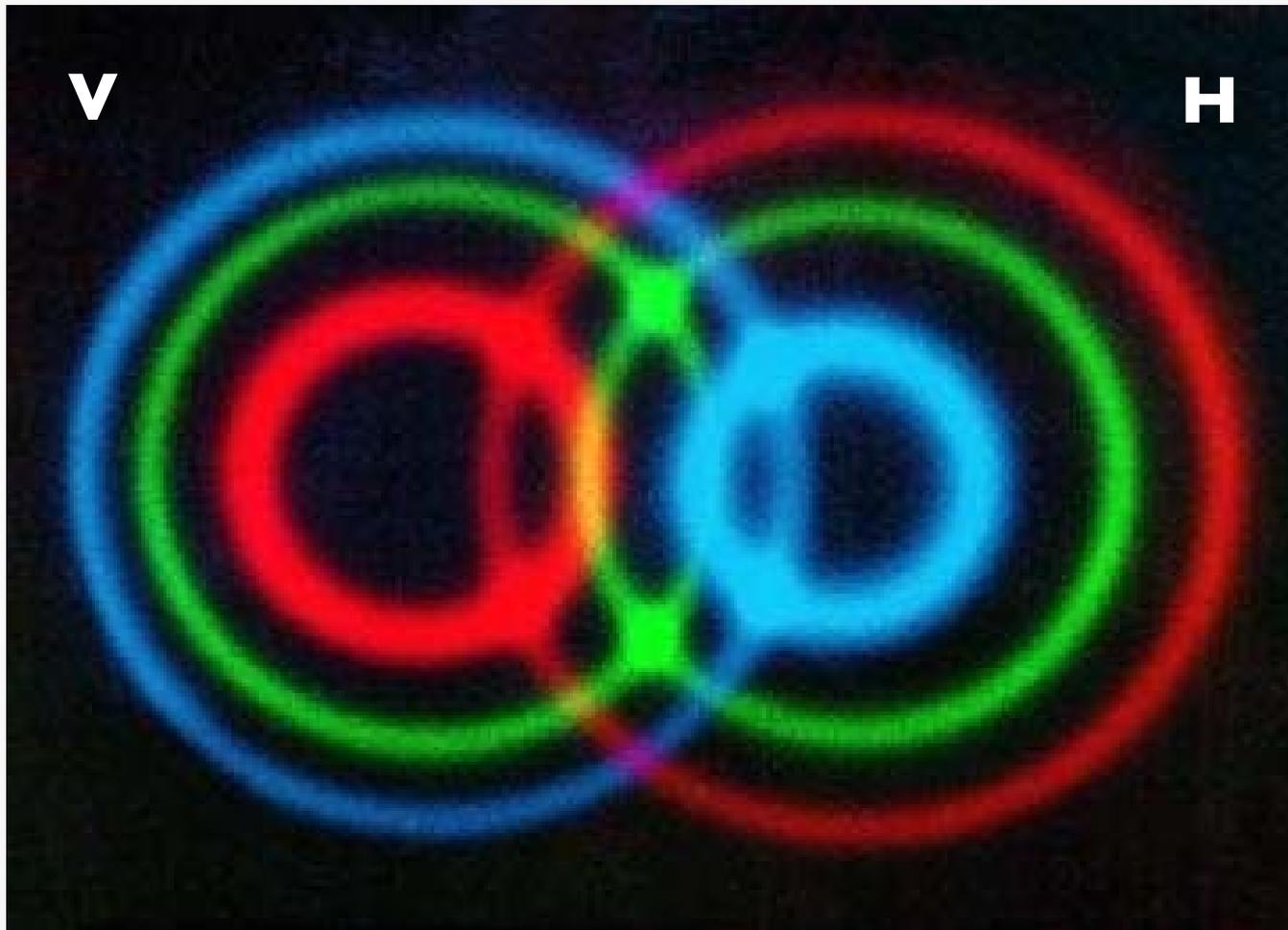


PARES DE FOTONES

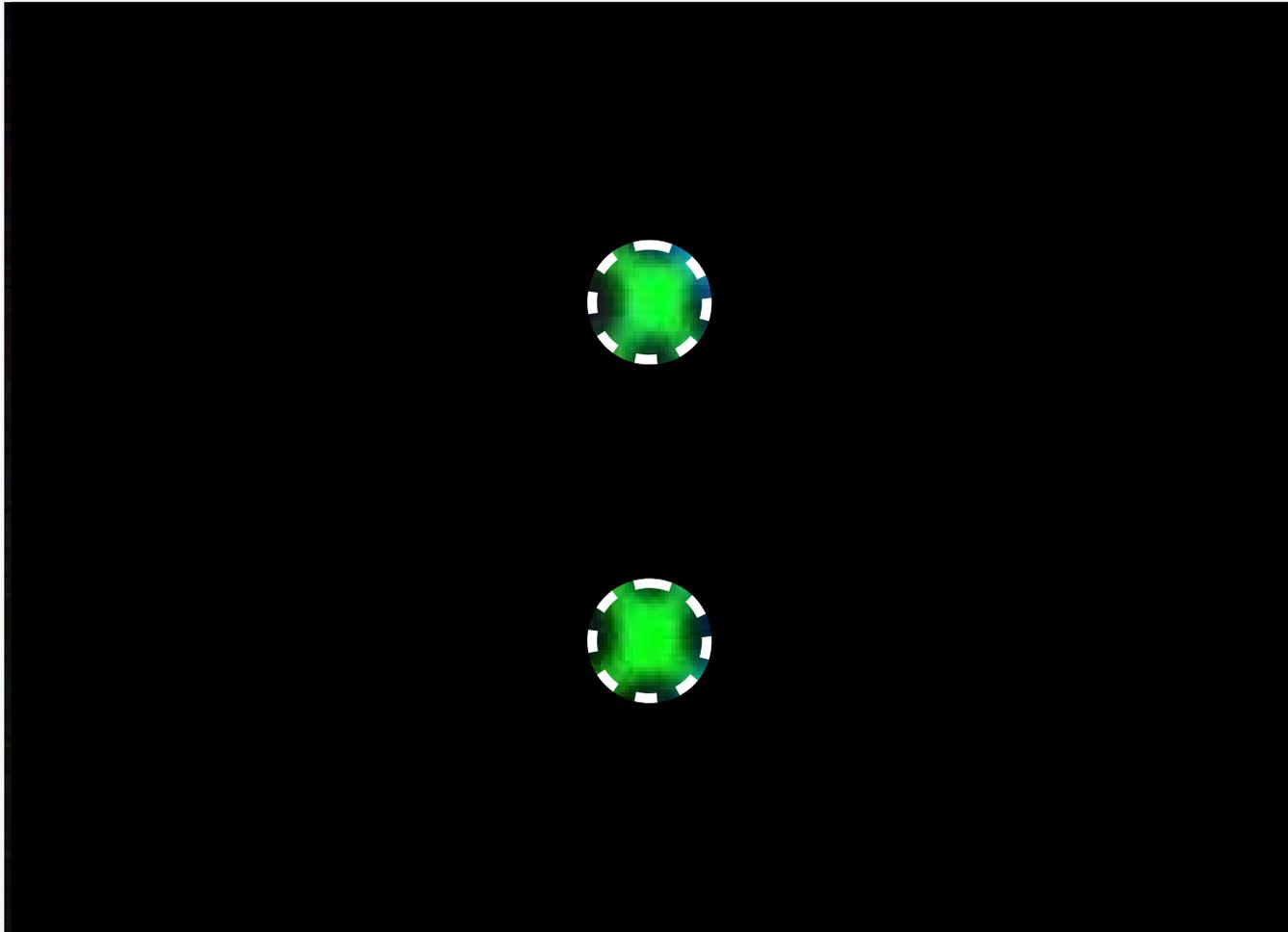


“Parametric down conversion” =
“doblado de fotones”

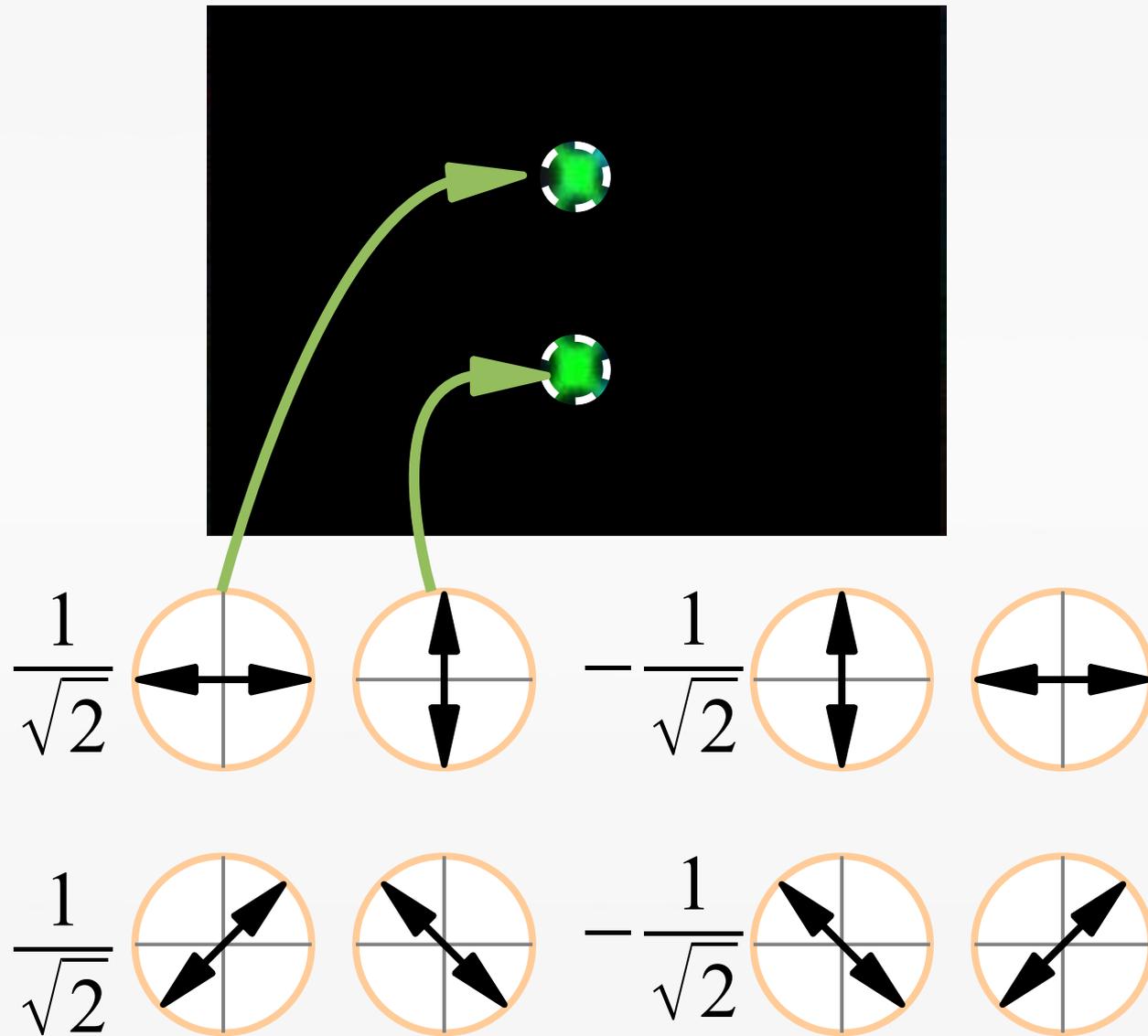
POLARIZACIÓN



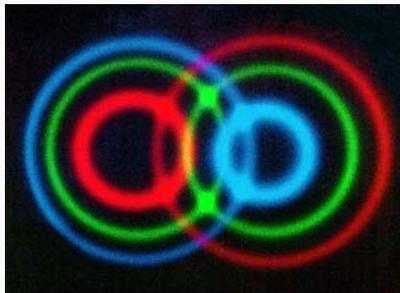
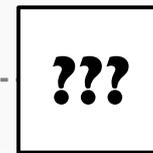
ENTRELAZAMIENTO



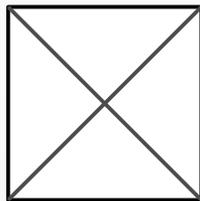
ENTRELAZAMIENTO



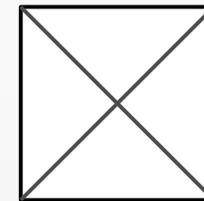
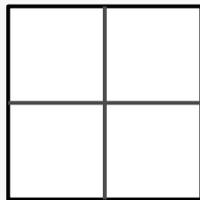
CRIPTOGRAFÍA



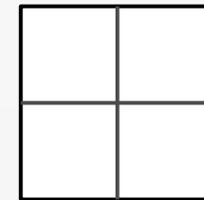
Medida A



Medida B



Medida A

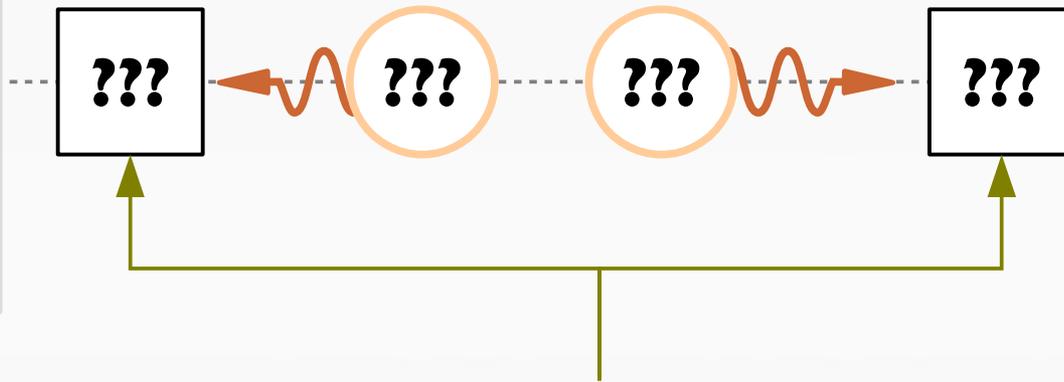


Medida B

CRIPTOGRAFÍA

| Base A | Base S | Bit A | Bit B | OK? |
|---------------|---------------|--------------|--------------|------------|
| A | A | 1 | 0 | ✓ |
| A | B | 0 | 1 | ✗ |
| B | A | 1 | 0 | ✗ |
| A | A | 0 | 1 | ✓ |
| B | A | 0 | 0 | ✗ |
| B | B | 0 | 1 | ✓ |
| B | A | 1 | 0 | ✗ |
| A | A | 1 | 0 | ✓ |
| B | A | 0 | 0 | ✗ |

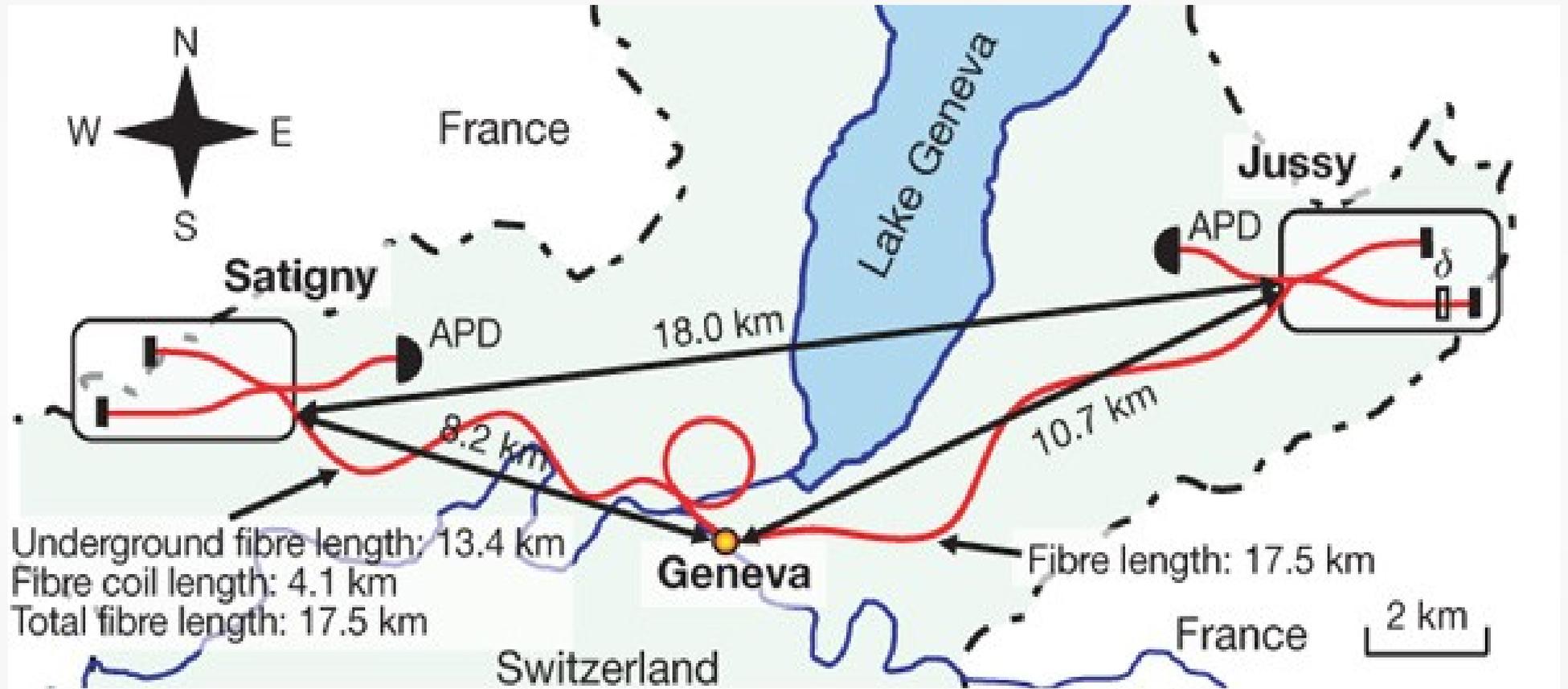
ACCIÓN A DISTANCIA?



Correlaciones mayores que clásicamente:
independientes de la base.

“Influencia mutua”?
Se hablan los fotones?

NO!

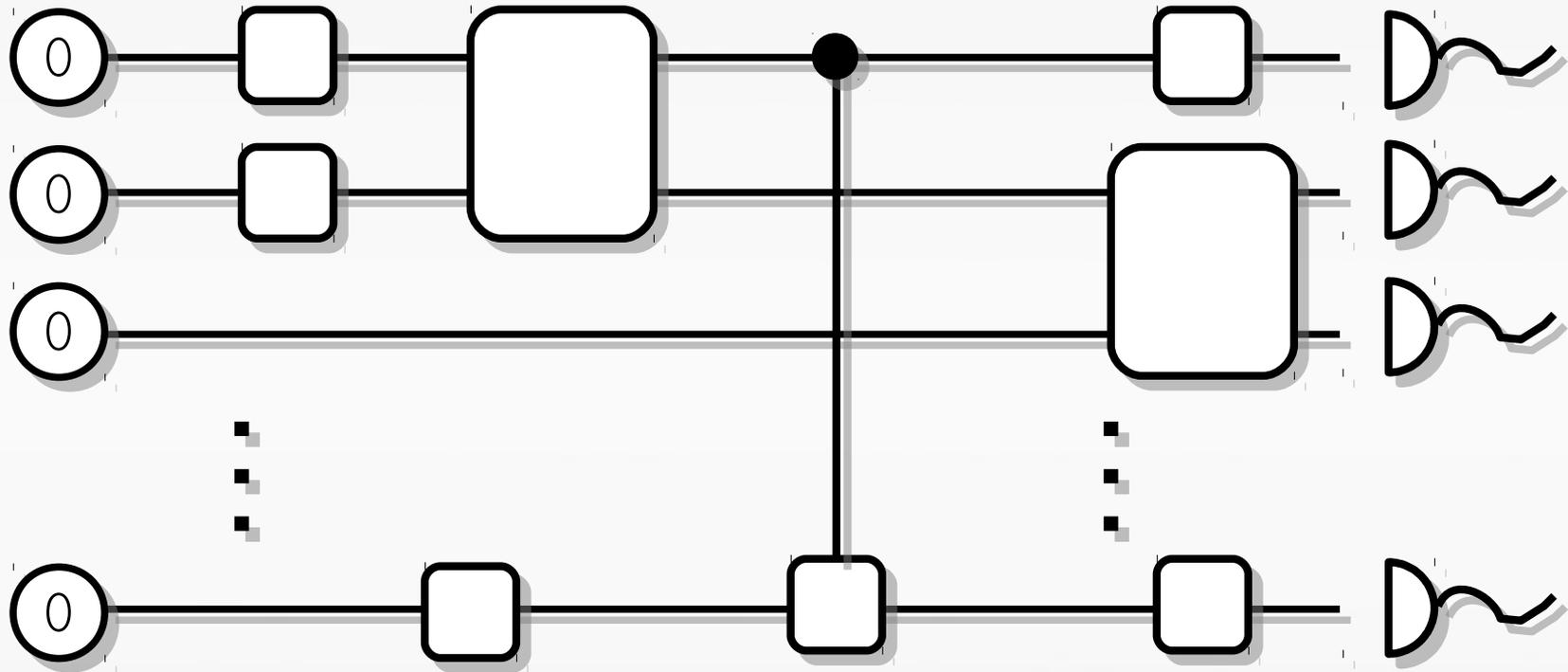


$100.000 \times c$???

Computación

¿PROBABILISTA
=
IMPRECISO?

ALGORITMOS



Qubits

Operaciones

Medidas

POTENCIAL

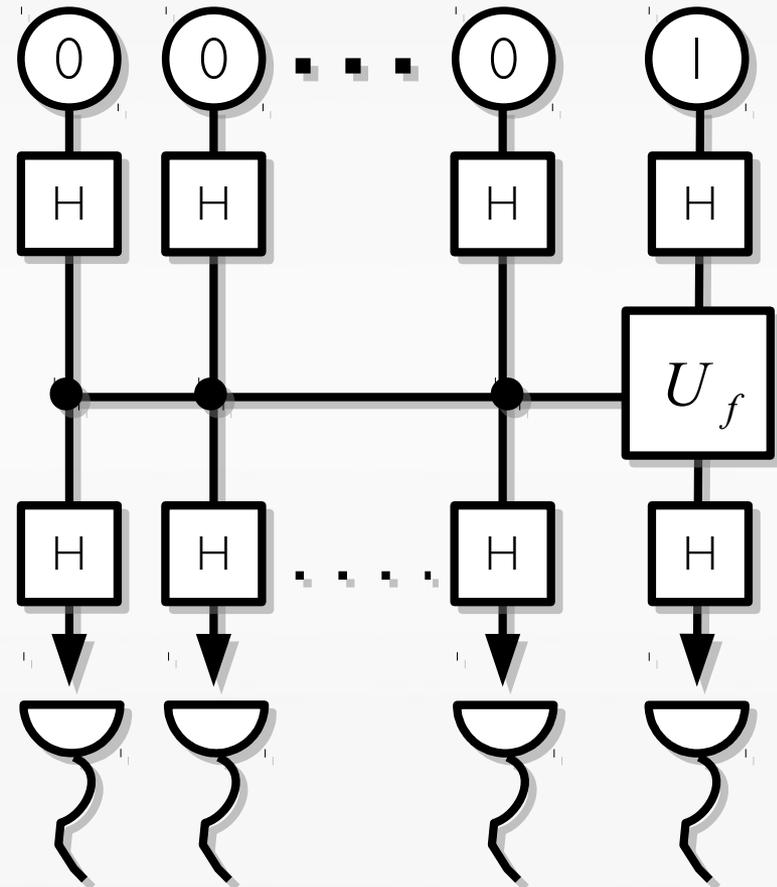
$$|\psi\rangle = c_{000\dots 0}|000\dots 0\rangle + c_{000\dots 1}|000\dots 1\rangle + \dots + c_{111\dots 1}|111\dots 1\rangle$$

Paralelismo implícito

Complejidad exponencial

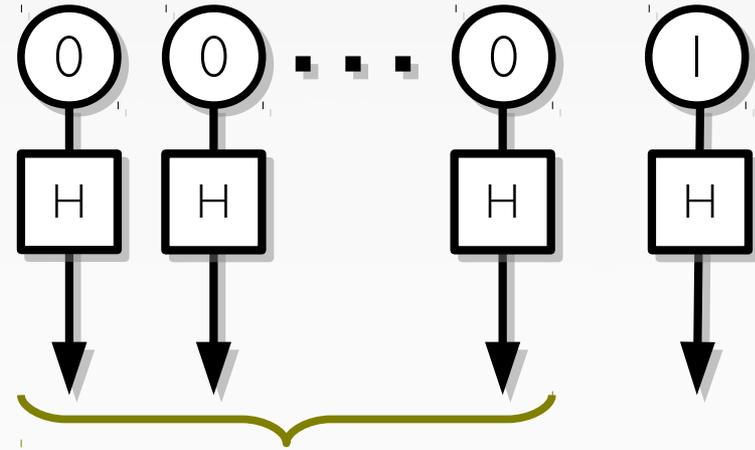
ALGORITMOS

- Determinar si una función de varias variables está “balanceada”
 - 0 bien es constante
 - 0 emite el mismo número de 0 y 1
- Clásicamente necesitamos hasta $2^{N/2}$ operaciones
- Cuánticamente, sólo 3 pasos.



PARALELISMO

Con una sola operación,
preparamos todos los números
posibles

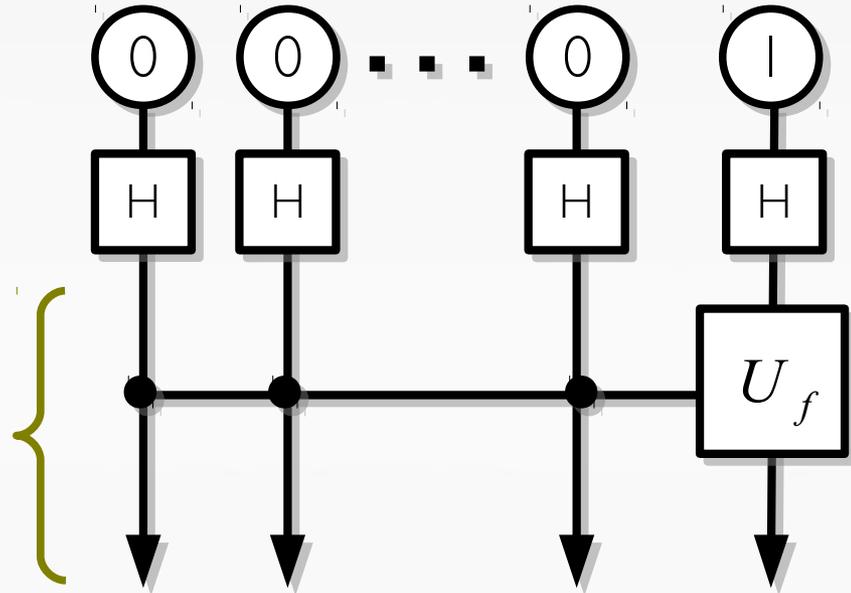


$$\frac{1}{\sqrt{N}} |000\dots 0\rangle +$$
$$\frac{1}{\sqrt{N}} |000\dots 1\rangle + \dots$$
$$\frac{1}{\sqrt{N}} |111\dots 1\rangle$$

PARALELISMO

El testigo extrae información sobre todos los cálculos posibles.

$$\begin{array}{c} |abc\dots z\rangle|1\rangle \\ \downarrow \\ |abc\dots z\rangle|f(a,b,c\dots z)\rangle \end{array}$$

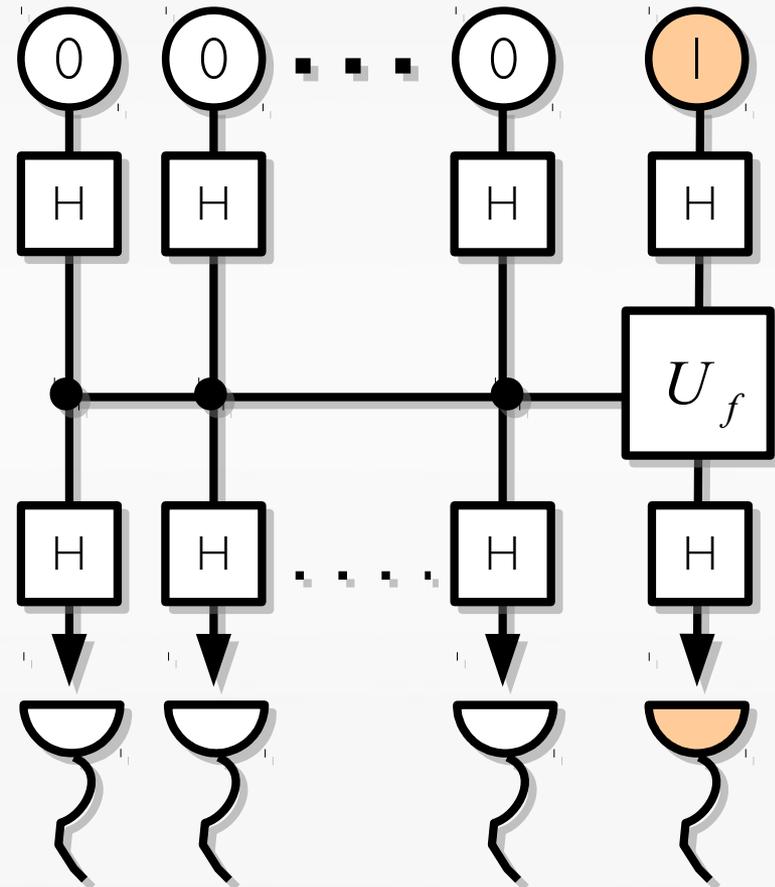


PARALELISMO

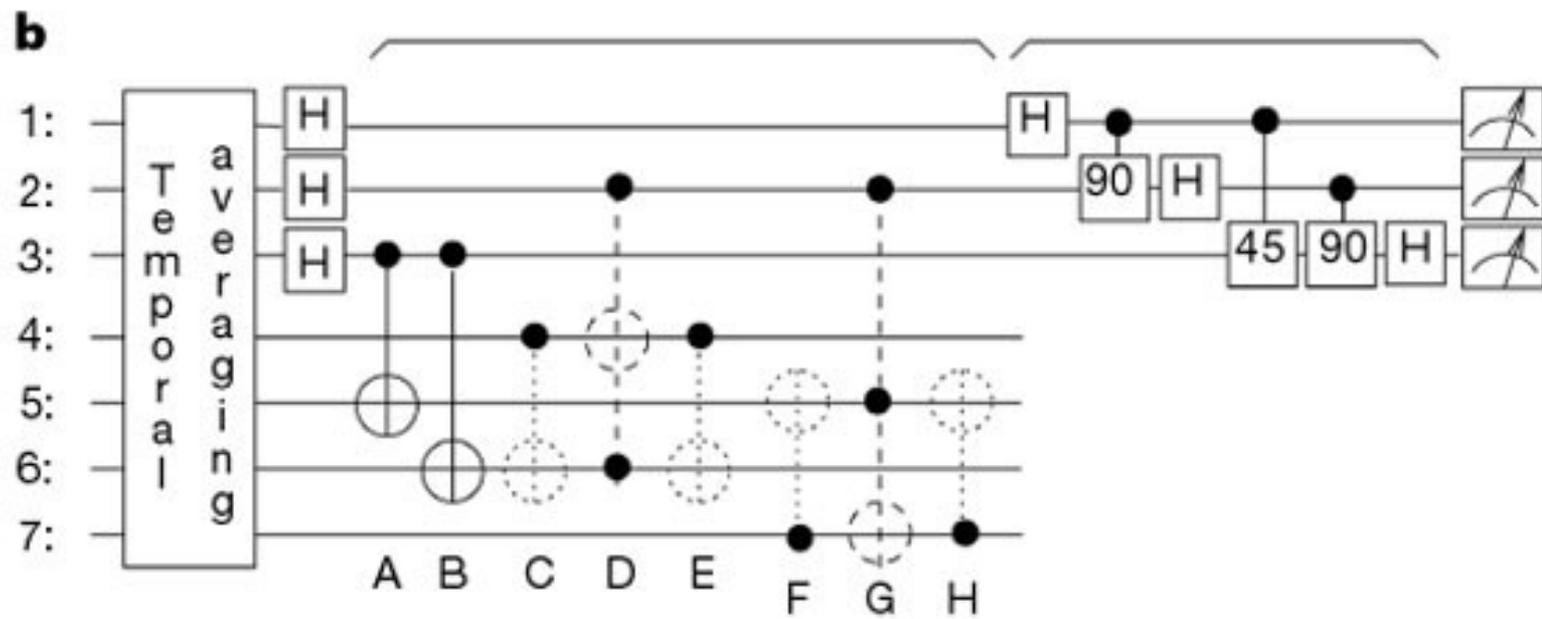
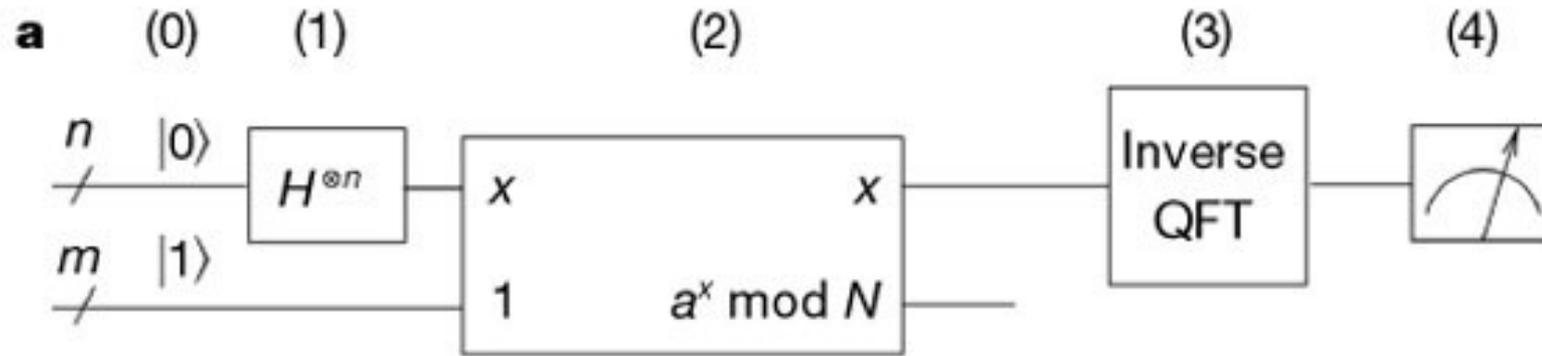
Al final el resultado en el testigo es

1 = la función es par

0 = la función es constante

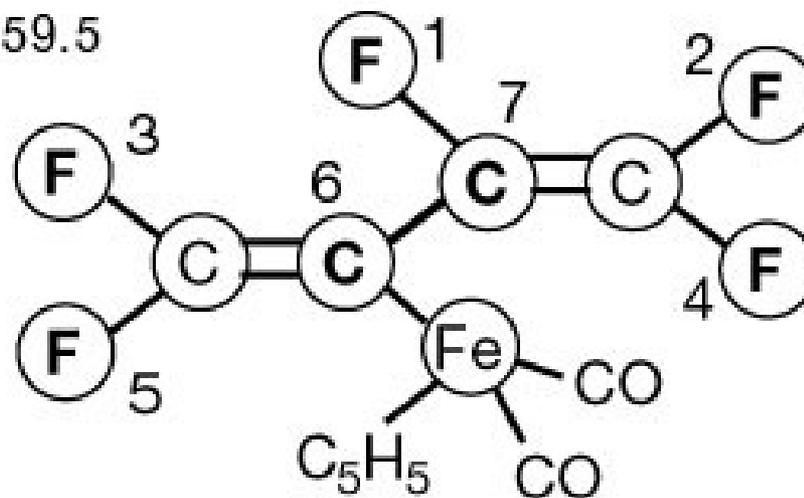


ALGORITMO DE SHOR

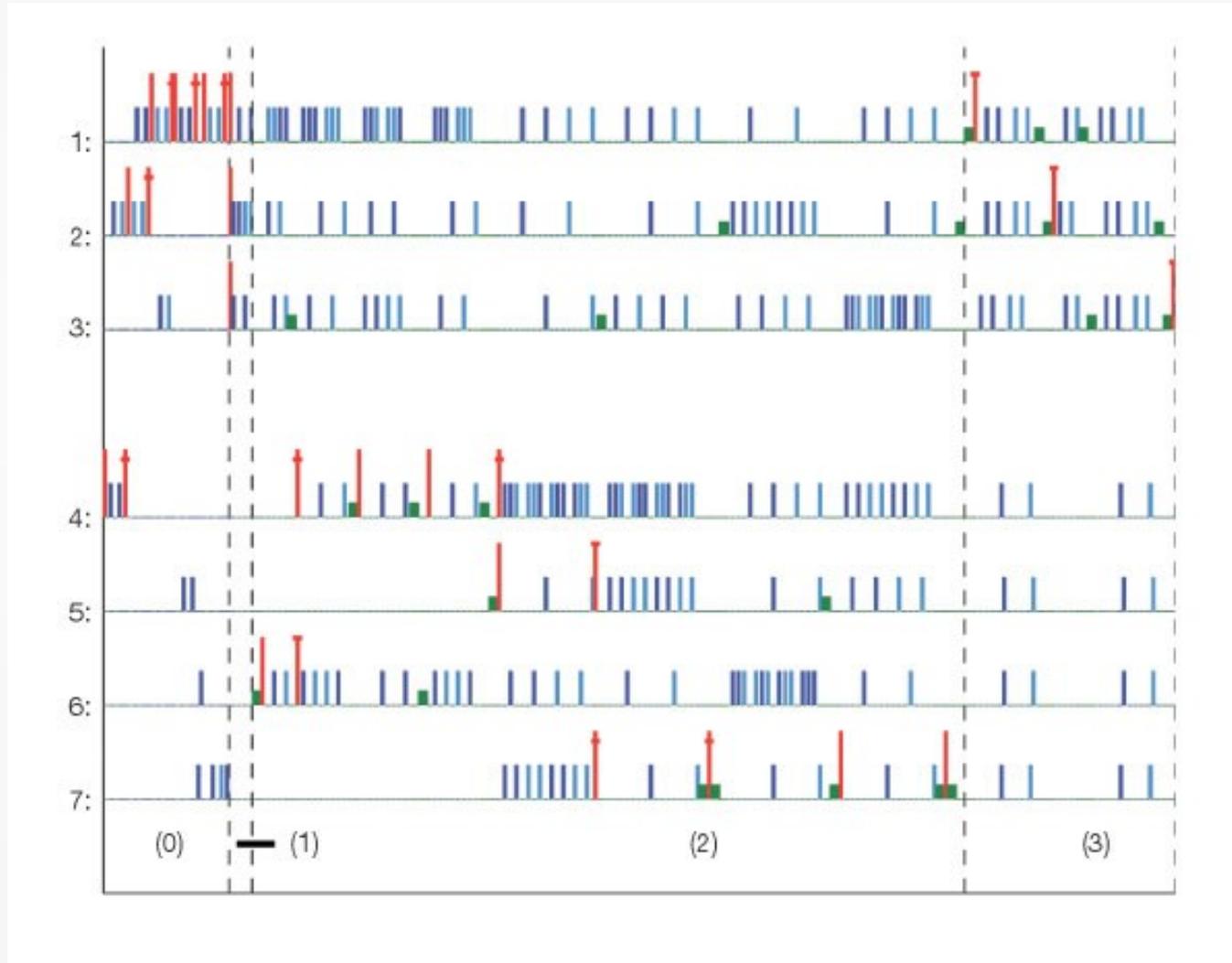


ALGORITMO DE SHOR

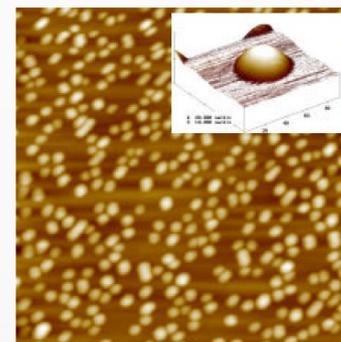
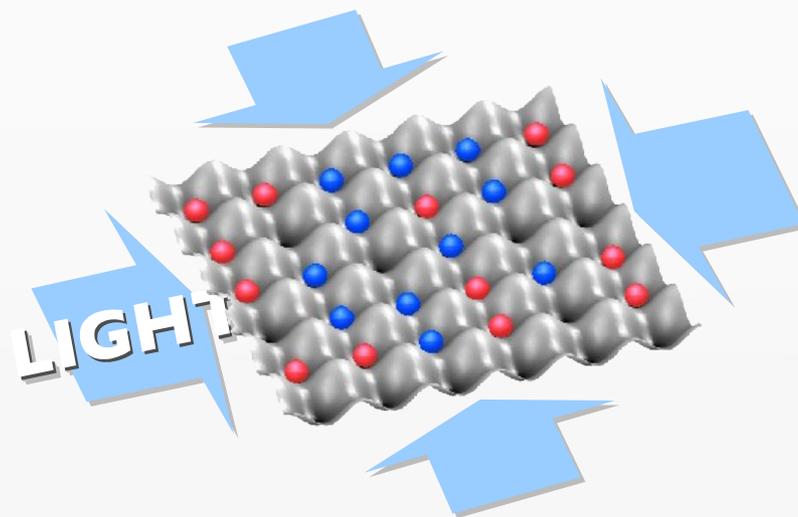
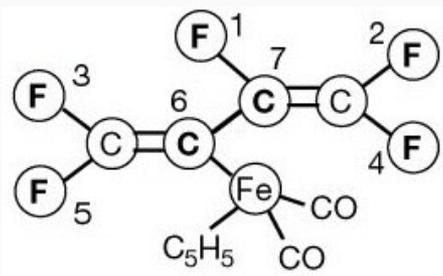
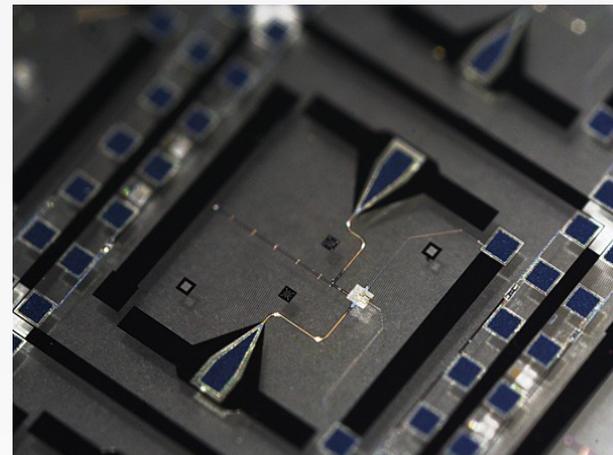
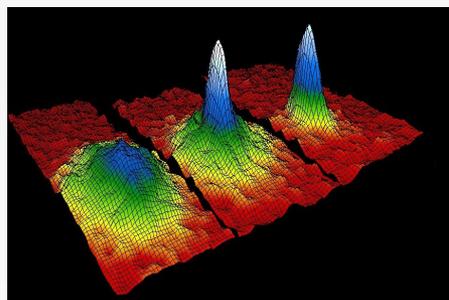
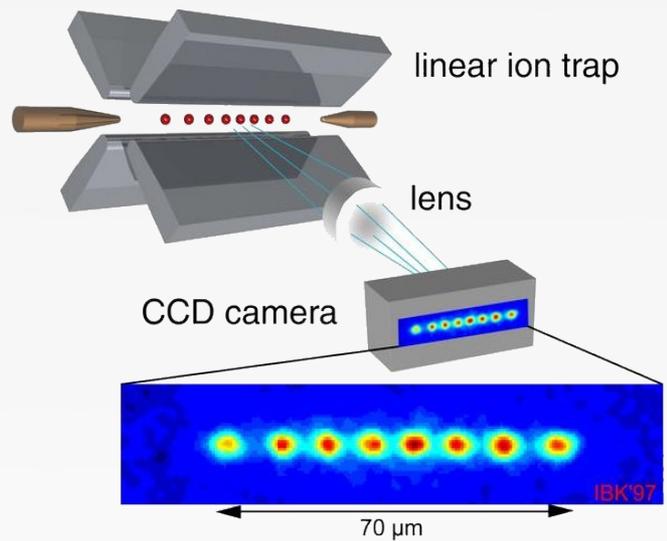
| i | $\omega_i/2\pi$ | $T_{1,i}$ | $T_{2,i}$ | J_{7i} | J_{6i} | J_{5i} | J_{4i} | J_{3i} | J_{2i} |
|-----|-----------------|-----------|-----------|----------|----------|----------|----------|----------|----------|
| 1 | -22052.0 | 5.0 | 1.3 | -221.0 | 37.7 | 6.6 | -114.3 | 14.5 | 25.16 |
| 2 | 489.5 | 13.7 | 1.8 | 18.6 | -3.9 | 2.5 | 79.9 | 3.9 | |
| 3 | 25088.3 | 3.0 | 2.5 | 1.0 | -13.5 | 41.6 | 12.9 | | |
| 4 | -4918.7 | 10.0 | 1.7 | 54.1 | -5.7 | 2.1 | | | |
| 5 | 15186.6 | 2.8 | 1.8 | 19.4 | 59.5 | | | | |
| 6 | -4519.1 | 45.4 | 2.0 | 68.9 | | | | | |
| 7 | 4244.3 | 31.6 | 2.0 | | | | | | |



ALGORITMO DE SHOR

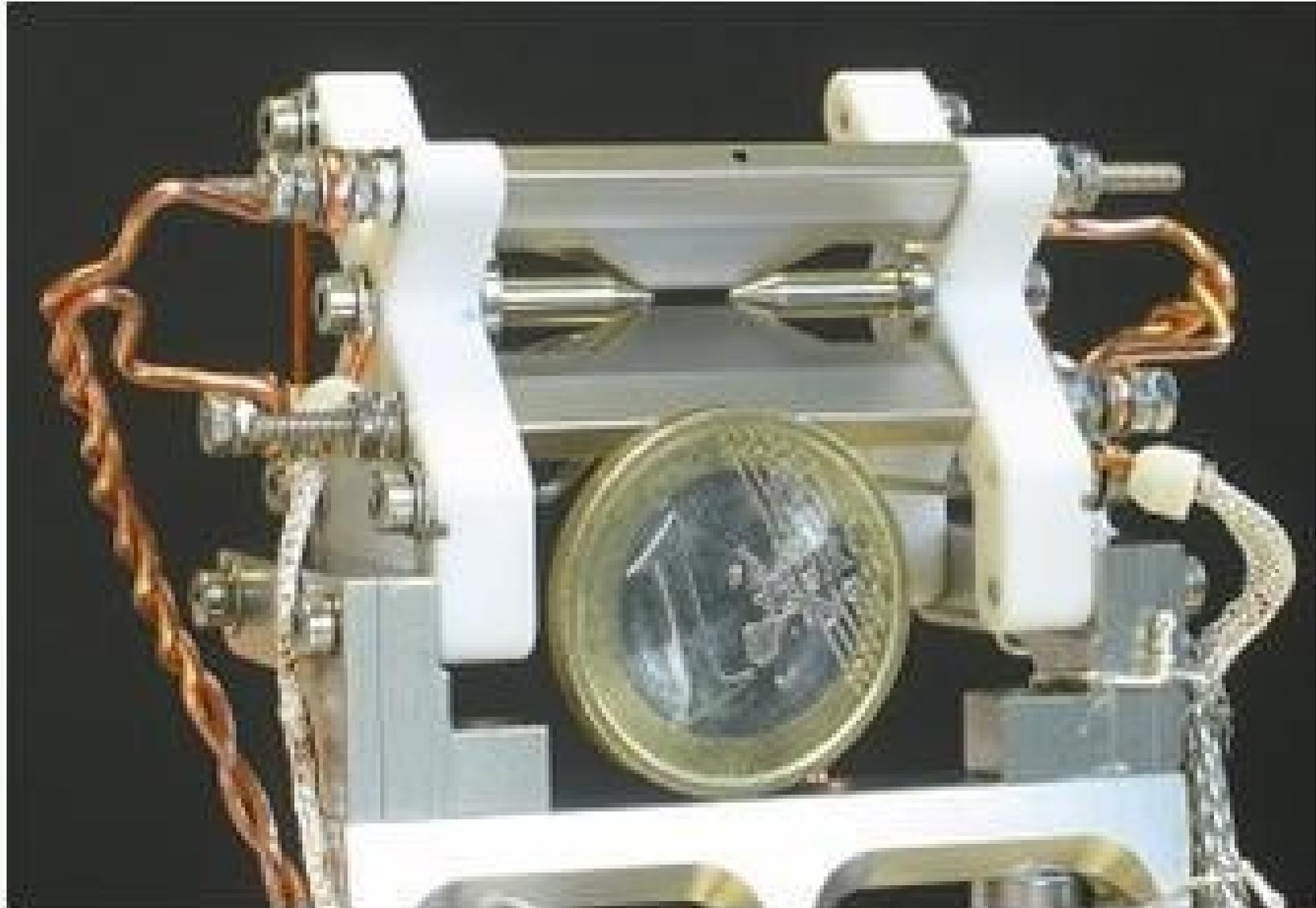


Implementaciones

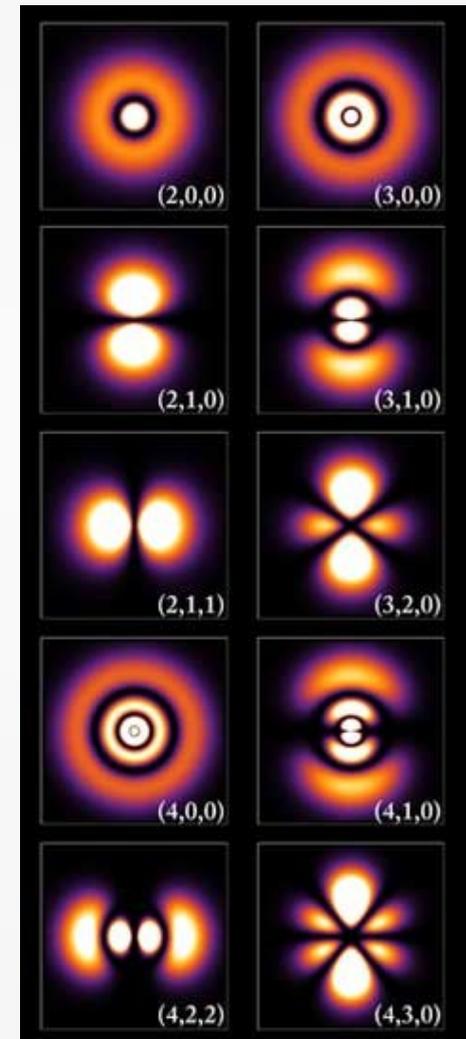
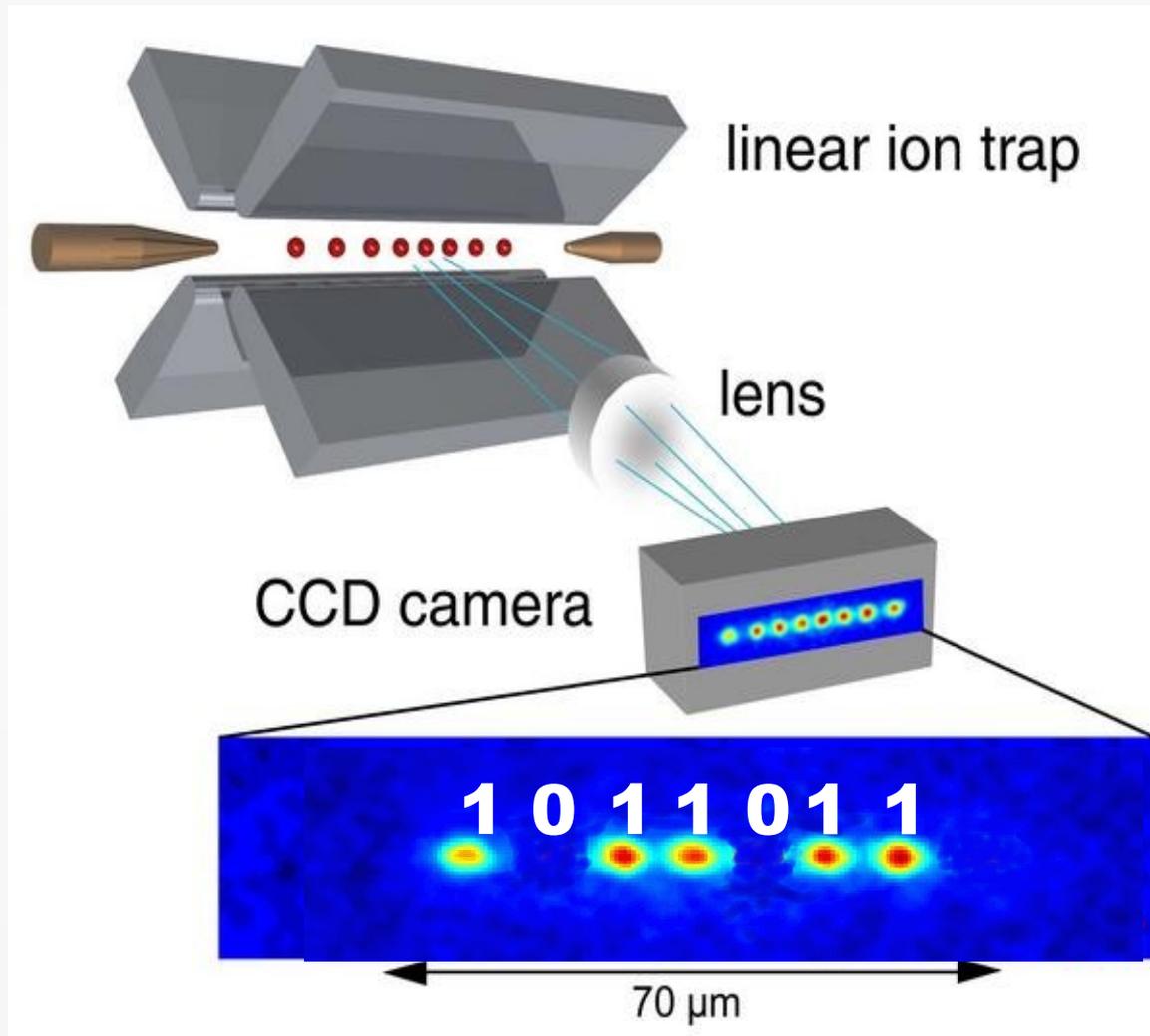


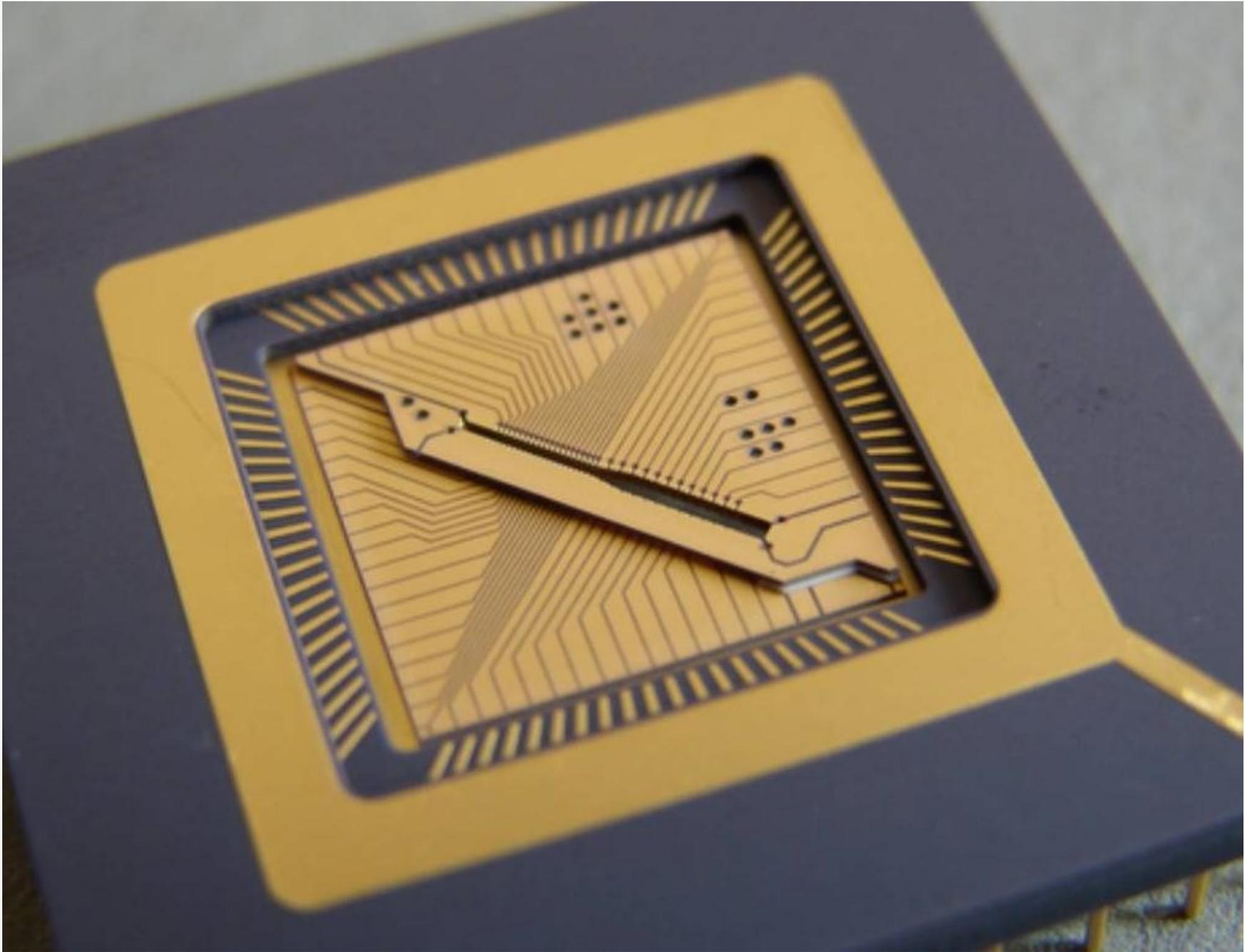
OTROS QUBITS

IONES



IONES

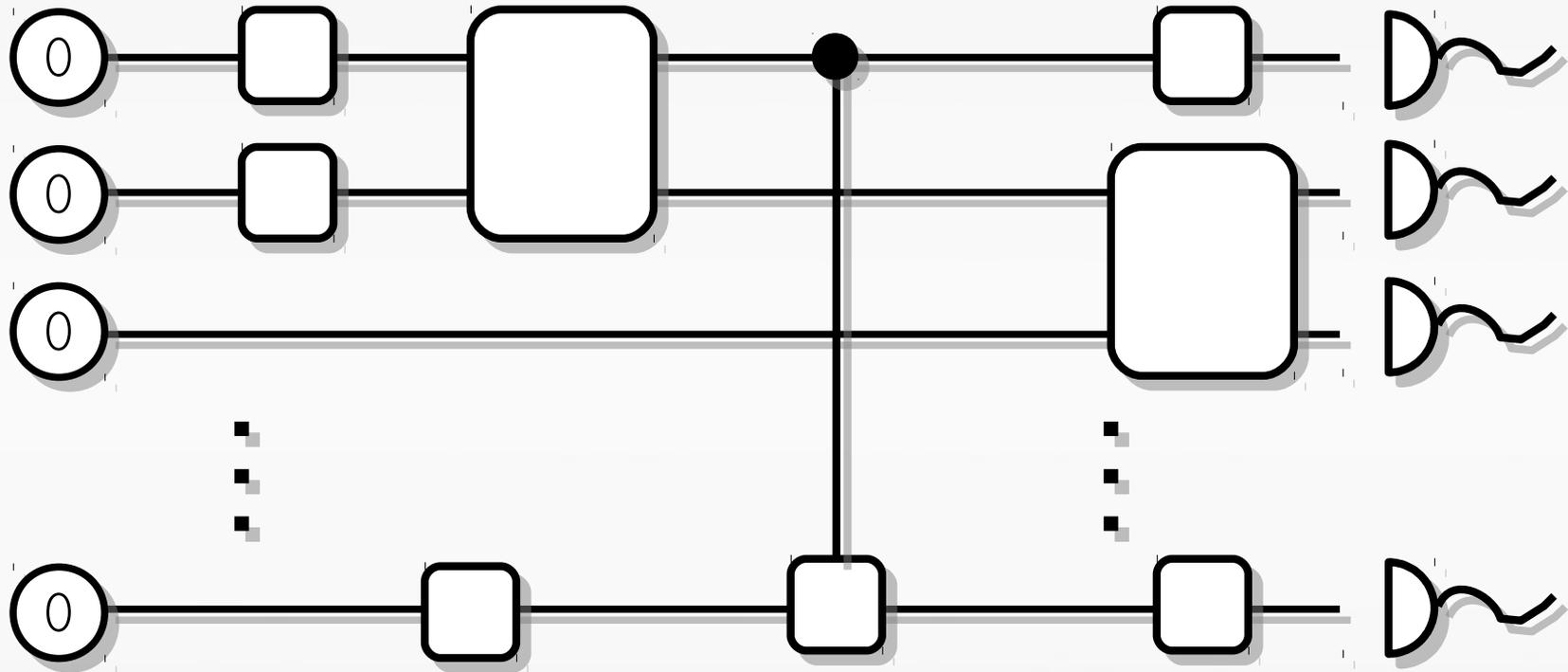




Pulsar aquí:

<http://www.youtube.com/watch?v=OECq7epKHLE>

OPERACIONES

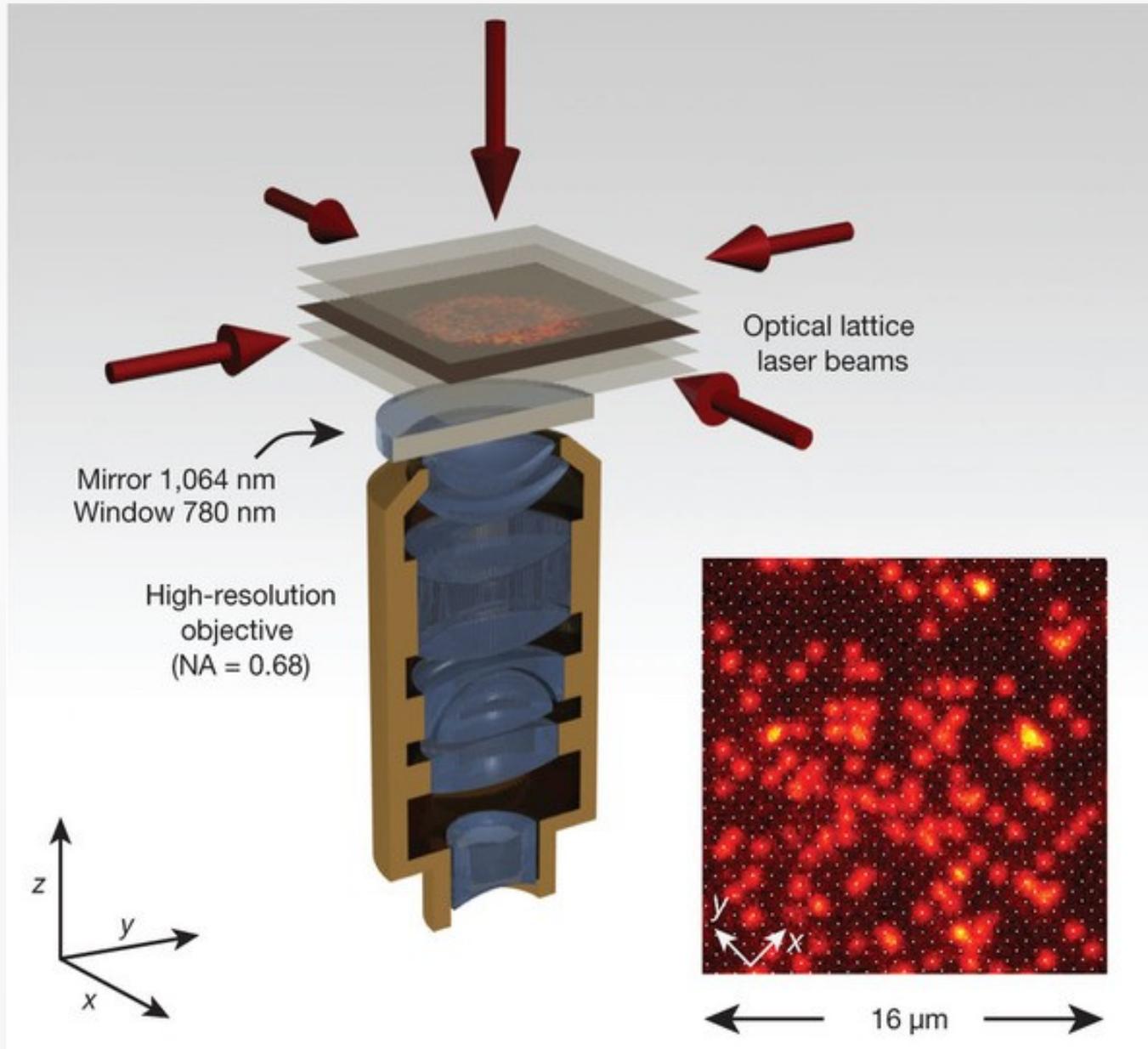


Qubits

Operaciones

Medidas

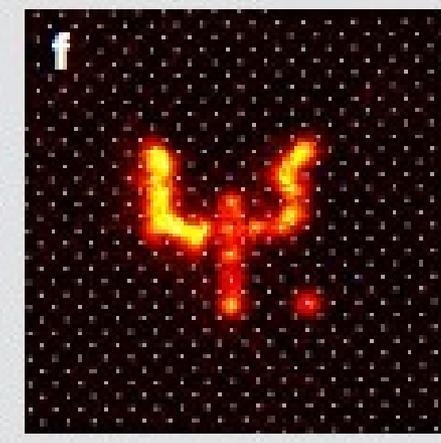
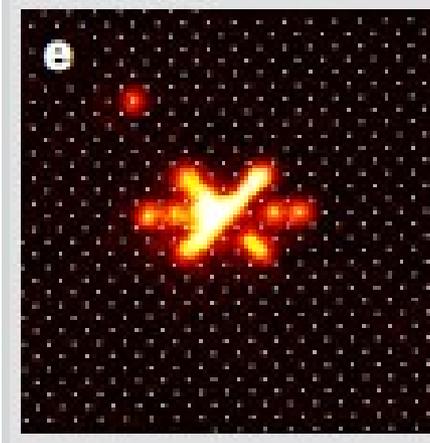
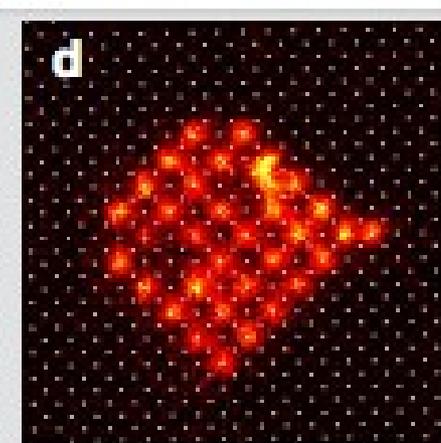
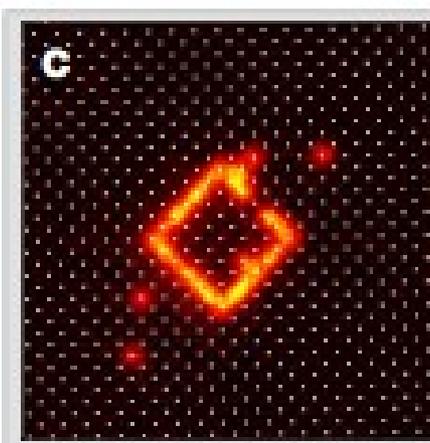
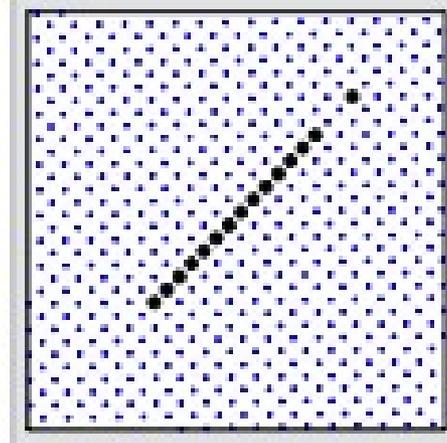
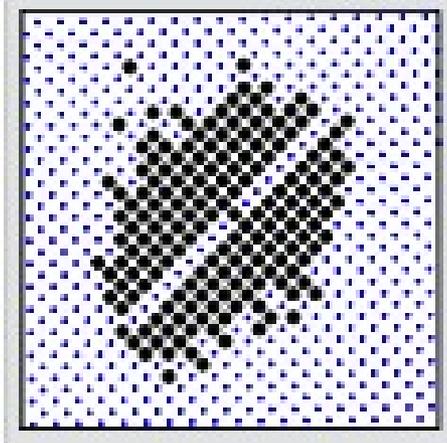
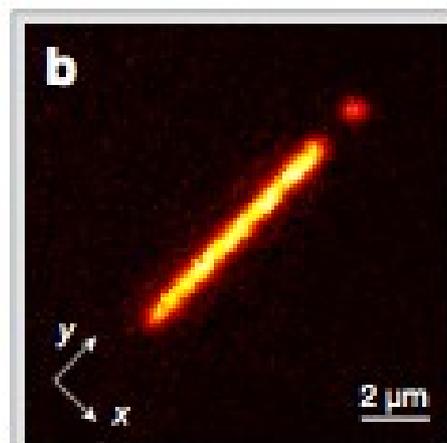
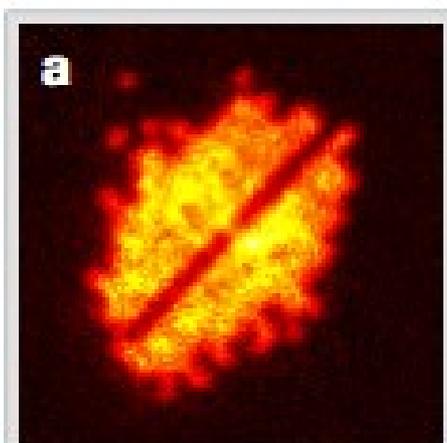
ÁTOMOS FRÍOS



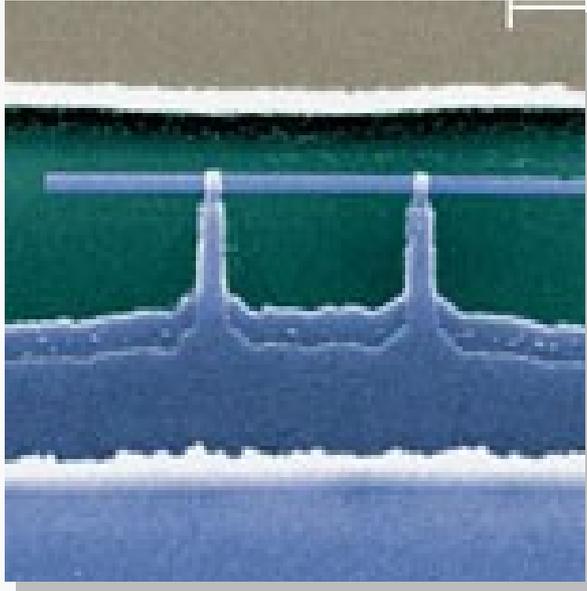
Pulsar aquí:

<http://greiner.physics.harvard.edu/Videos/hopping.mpeg>

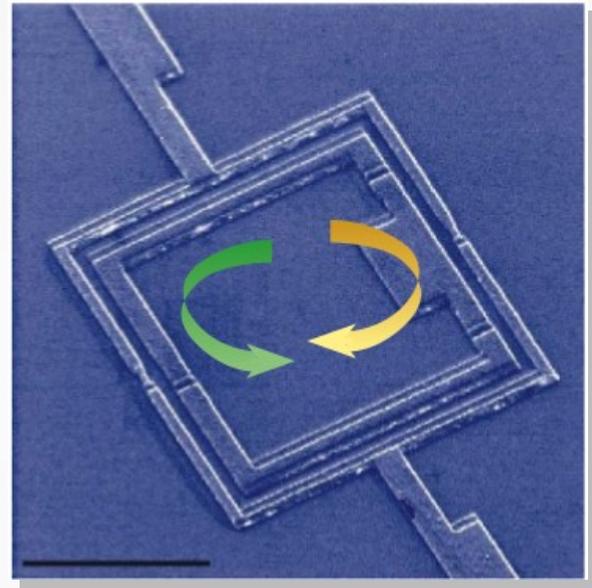
CONTROL



CIRCUITOS

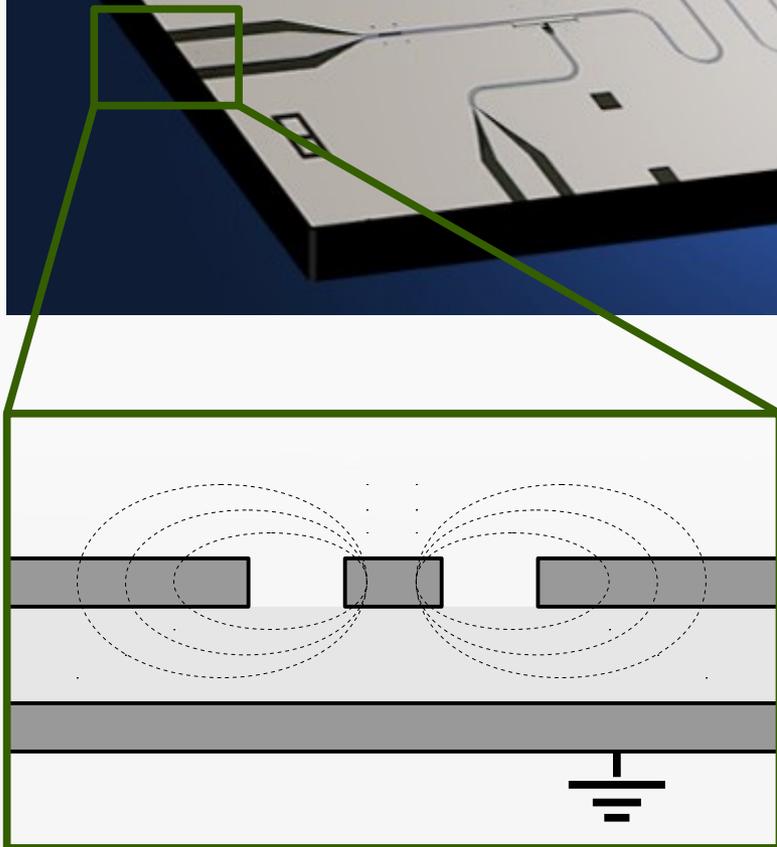
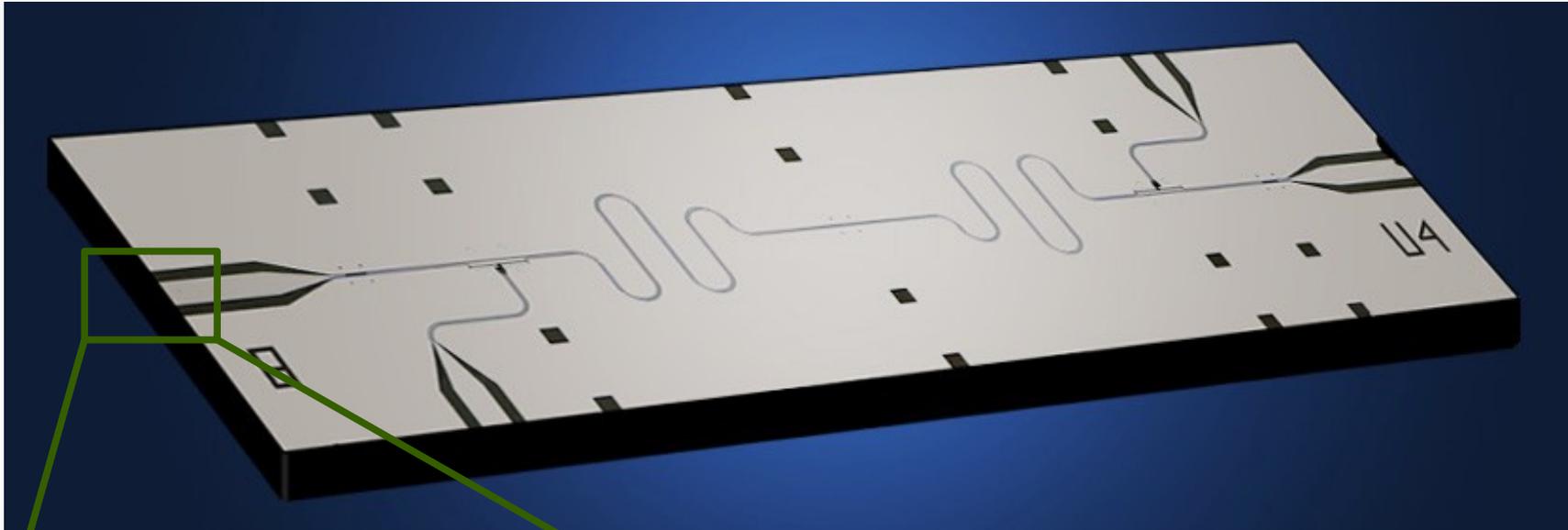


Qubit de carga



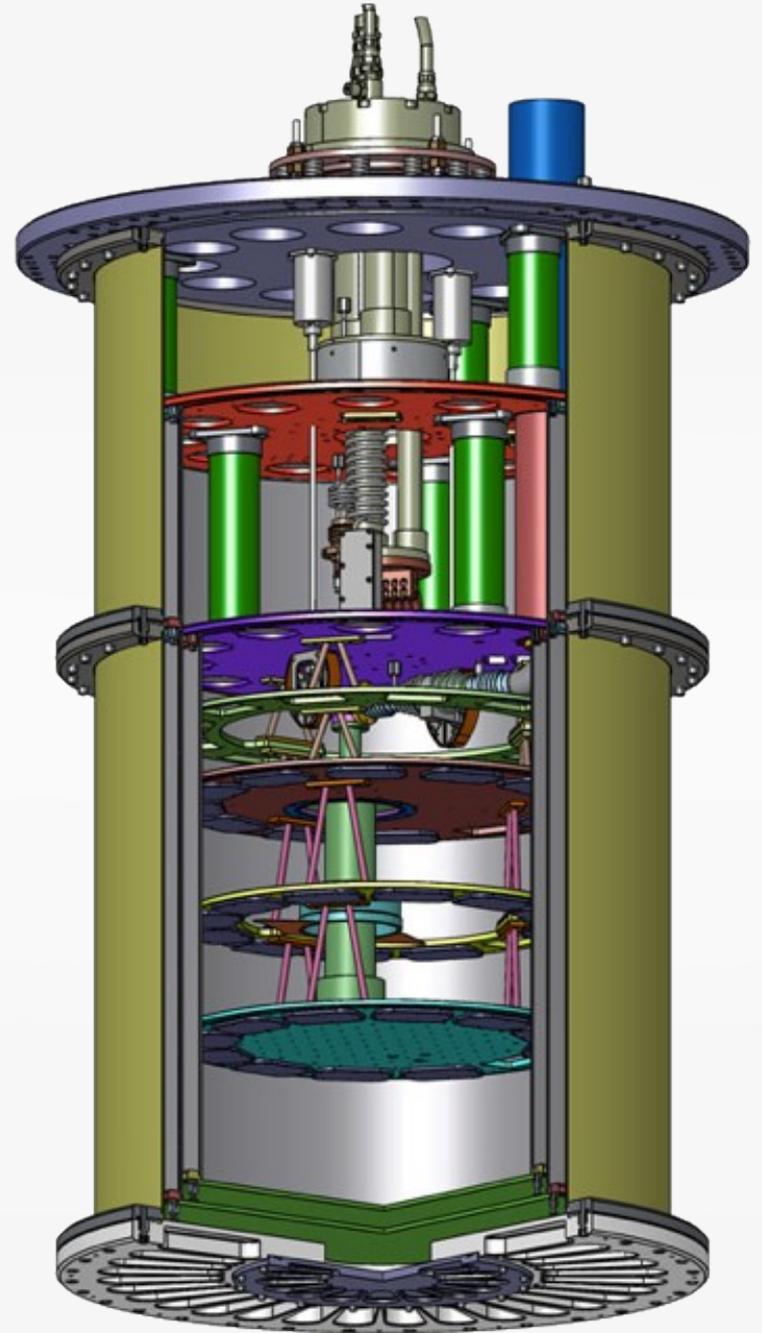
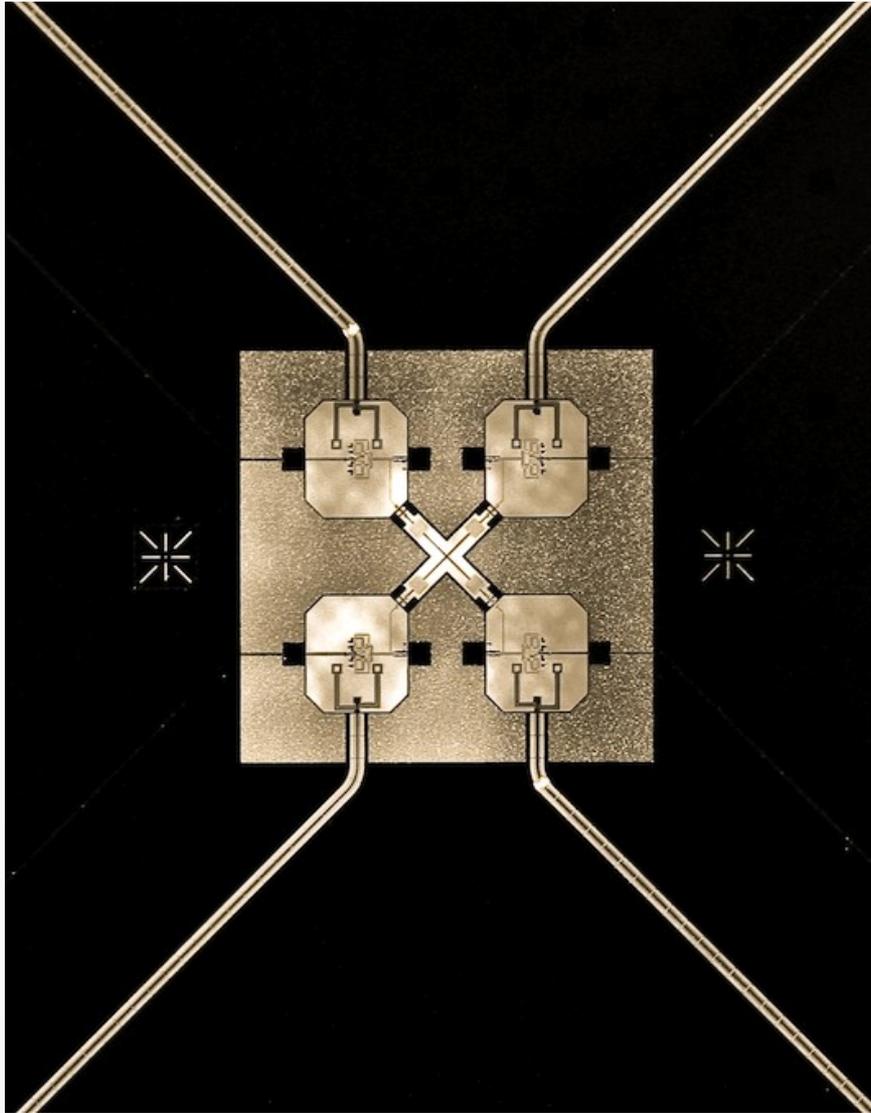
Qubit de flujo

CIRCUITOS

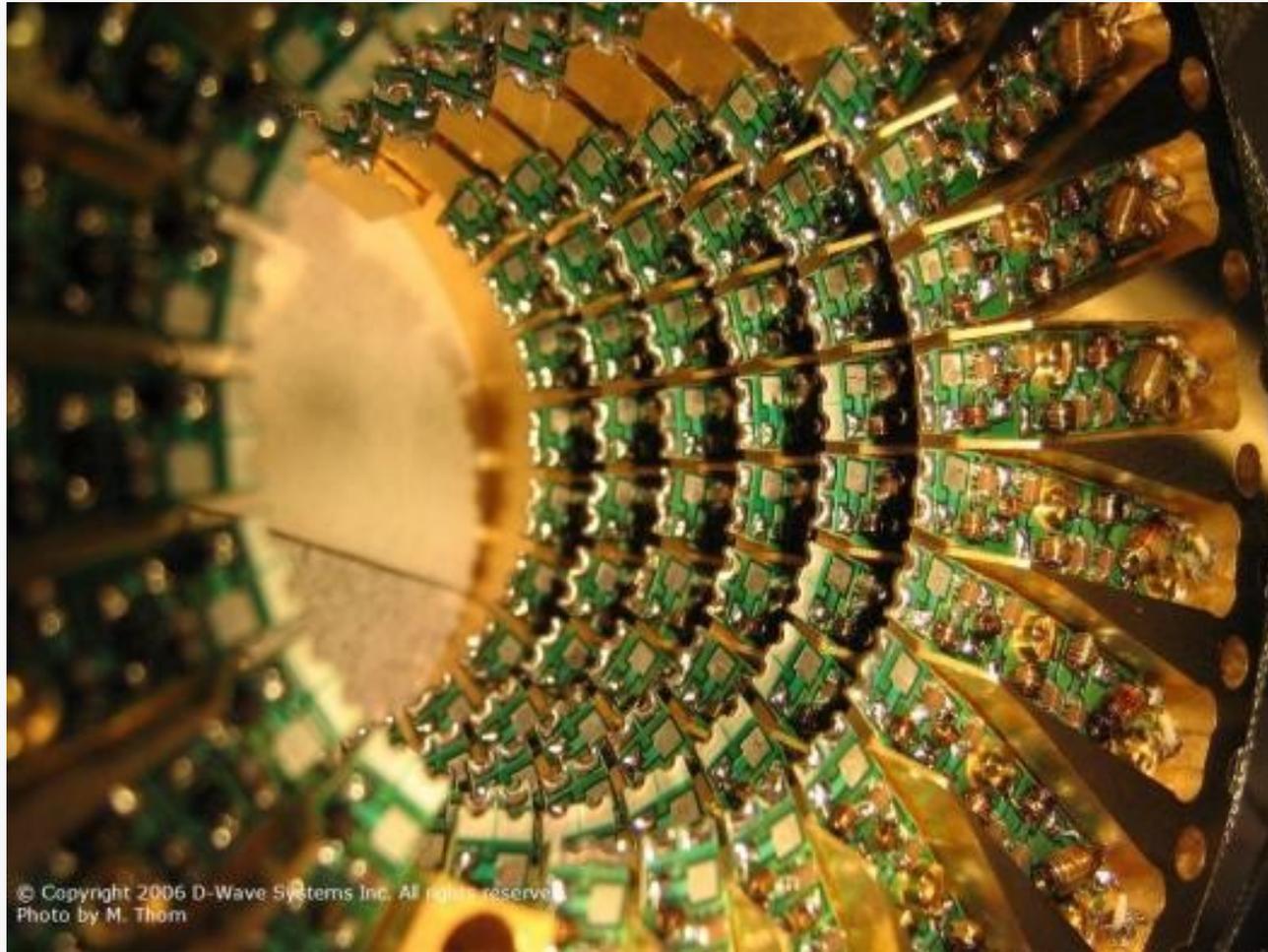


Guías de onda

- Transportan fotones de microondas.
- Permiten a los qubits interactuar entre sí.

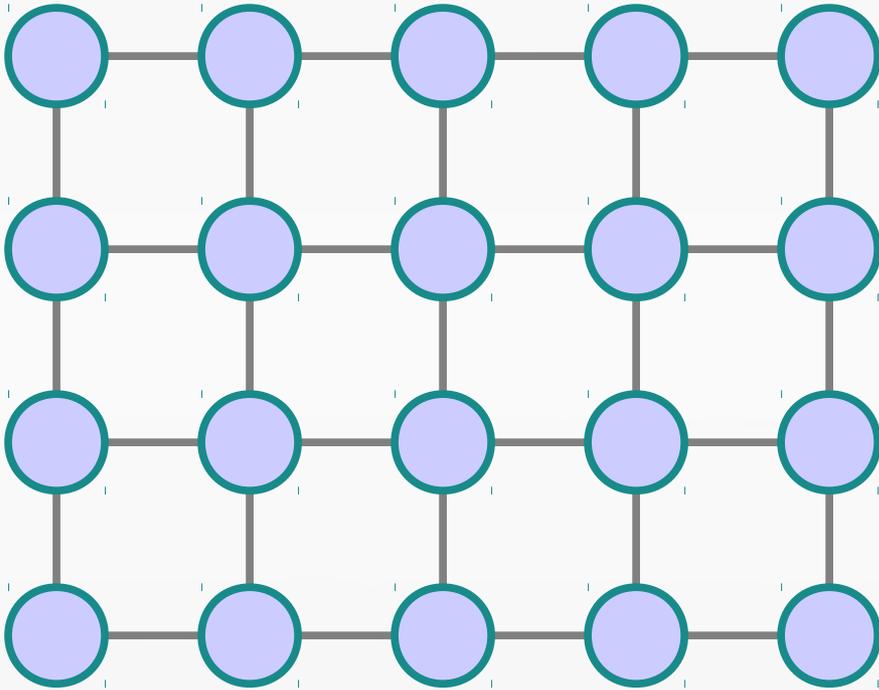


CIRCUITOS



Simulaciones clásicas

SIMULACIÓN CLÁSICA



$$\sum_{ab\dots z} c_{ab\dots z} |ab\dots\rangle$$

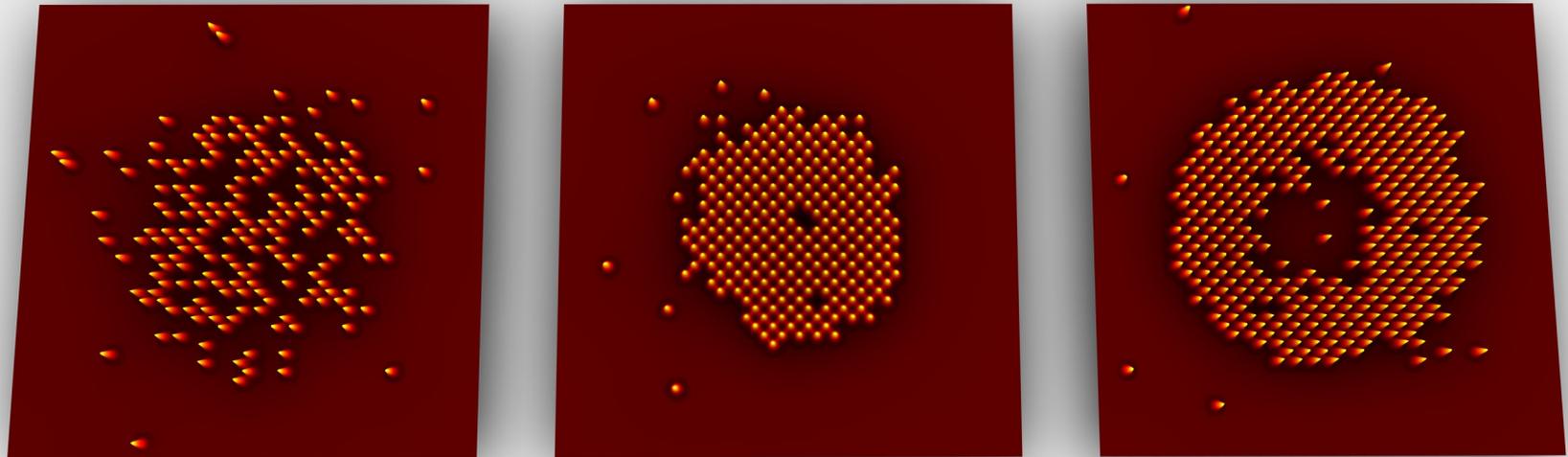
Exponentially large
vector of numbers



$$c_{ab\dots z} = F(A_a, A_b, \dots, A_z)$$

N times some complex
object "A"

SIMULACIÓN CUÁNTICA



Simulate some quantum mechanical system with the same components of a quantum computer.

